

# Mathematical Methods with TI-Nspire™ CX CAS

## Antidifferentiation and Integration

Revision Worksheet with solutions – may be completed after viewing the webinar

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Each of the questions included here can be solved using either the TI-Nspire CX or CX CAS.

### Question 1

- a. Find the rule of the function  $f : R \rightarrow R$  if  $f'(x) = 4x^3 - 6x + 2$  and the point with coordinates  $\left(-1, -\frac{5}{2}\right)$  is on the graph of  $f$ .

Response:

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### Question 2

For the functions  $f'$  and  $f$  in Question 1 above, display on your TI-Nspire the graph of  $y = f'(x)$  and the graph of  $y = f(x)$ .

Hence describe the relation between key features of the graph of the antiderivative function,  $f$ , and the graph of the original function,  $f'$ .

Response:

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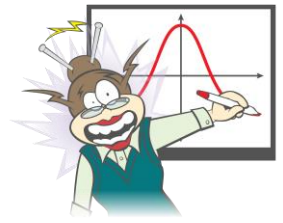
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### Question 3

Consider the function  $f : \left(\frac{1}{2}, \infty\right) \rightarrow R$ ,  $f(x) = \frac{3}{(2x-1)^{\frac{3}{2}}}$ .

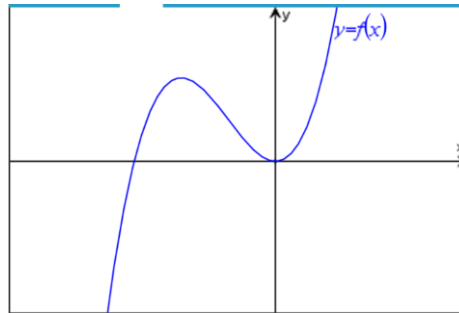
If the graph of an antiderivative, with equation  $y = F(x)$ , where  $F'(x) = f(x)$ , intersects the  $x$ -axis at  $x = 1$ , then  $F(x)$  is equal to

- A.  $\frac{-9}{(2x-1)^{\frac{5}{2}}}$     B.  $\frac{-9}{(2x-1)^{\frac{1}{2}}}$     C.  $\frac{-3}{(2x-1)^{\frac{5}{2}}} + 3$     D.  $\frac{-3}{(2x-1)^{\frac{1}{2}}}$     E.  $\frac{-3}{(2x-1)^{\frac{1}{2}}} + 3$

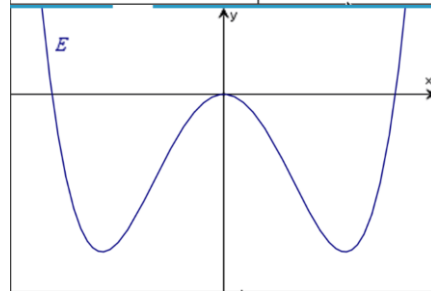
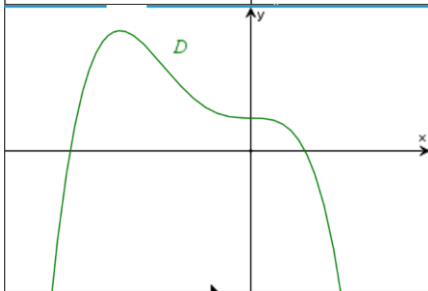
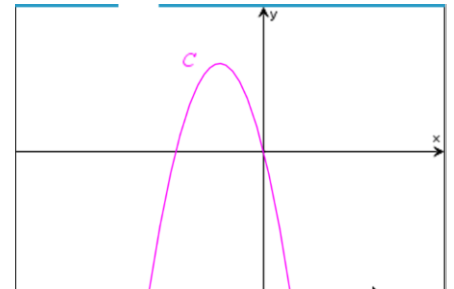
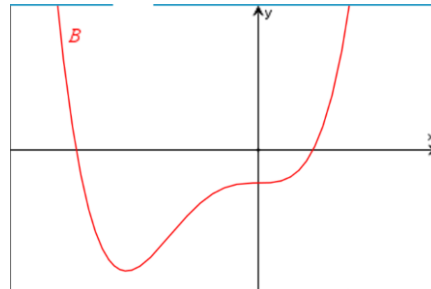
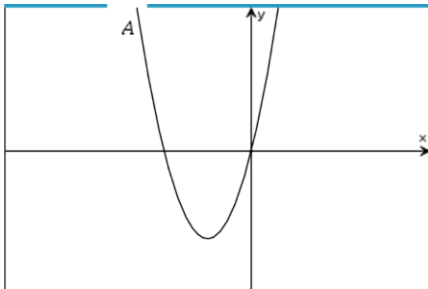


**Question 4**

A part of the graph of the function  $f$  is shown below.



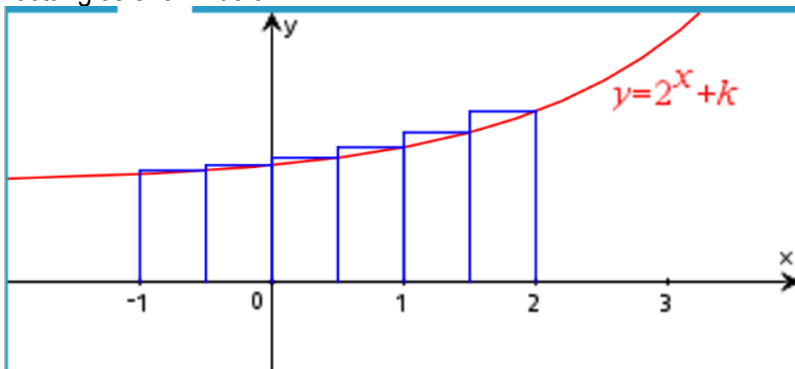
Which one of the following, A to E, could be a graph of an antiderivative of the function  $f$ ?

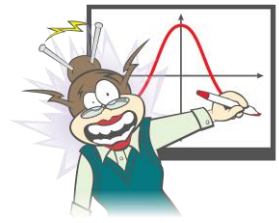


**Questions 5 and 6 refer to the following.**

The rule of the function  $g$  is  $g(x) = 2^x + k$ .

The area between the graph of  $g$  and the  $x$ -axis, over the interval  $[-1, 2]$ , is approximated using the six right rectangles shown below.





### Question 5

If the approximated area is  $\frac{80+7\sqrt{2}}{4}$ , the value of  $k$  is

- A. 4      B.  $\frac{9}{2}$       C. 5      D.  $\frac{11}{2}$       E. 6

Response:

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### Question 6

The exact area between the  $x$ -axis and the graph of  $g$ , over the interval  $[-1, 2]$  is closest to

- A. 21.00      B. 21.55      C. 22.00      D. 22.48      E. 23.56

Response:

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### Question 7

If  $\int_{-3}^3 a(x^2 + 1) dx = -2$ , then the value of  $a$  is

- A.  $\frac{1}{6}$       B.  $-\frac{1}{6}$       C.  $-\frac{1}{12}$       D.  $\frac{1}{12}$       E.  $-\frac{2}{33}$

Response:

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## Answers

### Question 1

$$f(x) = x^4 - 3x^2 + 2x + \frac{3}{2}$$

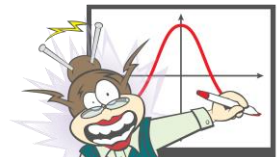
A screenshot of a math problem solution. It shows the function  $f(x) := \int (4 \cdot x^3 - 6 \cdot x + 2) dx + c$  and the result  $f(x)|_{c=\frac{3}{2}} = x^4 - 3 \cdot x^2 + 2 \cdot x + \frac{3}{2}$ . The word "Done" is visible in the top right corner of the screenshot.

© Question 1

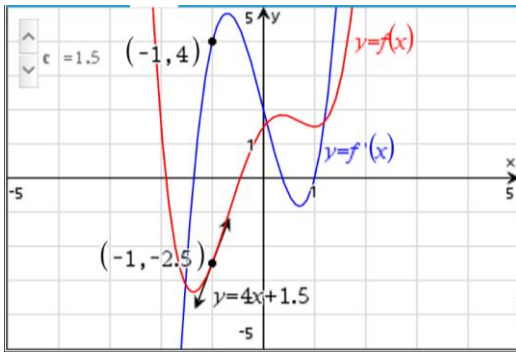
$f(x) := \int (4 \cdot x^3 - 6 \cdot x + 2) dx + c$  Done

solve  $\left( f(-1) = \frac{-5}{2}, c \right)$   $c = \frac{3}{2}$

$f(x)|_{c=\frac{3}{2}}$   $x^4 - 3 \cdot x^2 + 2 \cdot x + \frac{3}{2}$



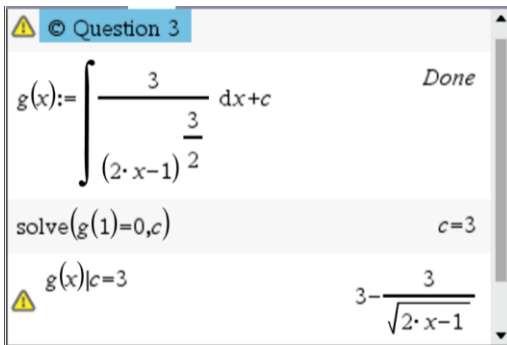
### Question 2



Original graph $y = f(x)$	Antiderivative graph $y = F(x)$
$f(x) < 0$ (below $x$ -axis)	Decreasing (negative slope)
$f(x) = 0$ (intersects $x$ -axis)	Stationary point (zero slope)
$f(x) > 0$ (above $x$ -axis)	Increasing (positive slope)
Turning point ( $f'(x) = 0$ )	Point of inflection

### Question 3

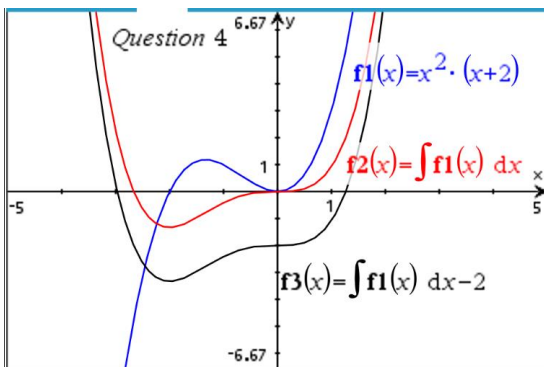
Answer: E  $\frac{-3}{(2x-1)^2} + 3$

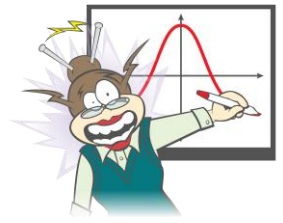


### Question 4

Answer: B.  $y = f(x)$  could be a positive cubic graph with a ‘double root’ at the origin. An antiderivative could therefore be a positive quartic graph with an inflection at  $x = 0$ .

Try graphing, for example,  $y = x^2(x+2)$  and an antiderivative,  $y = \int (x^2(x+2)) dx + c$  (with suitable  $c$ ).





### Question 5

Answer: D  $\frac{11}{2}$

5.1 6.1 7.1 \*Antidiffer...eet RAD

© Question 5

$g(x) := 2^x + k$  Done

$area := \sum \left( \frac{1}{2} \cdot g(x) \right) | x = \left\{ \frac{-1}{2}, 0, \frac{1}{2}, 1, \frac{3}{2}, 2 \right\}$

$3 \cdot k + \frac{7 \cdot \sqrt{2}}{4} + \frac{7}{2}$

$solve \left( area = \frac{80 + 7 \cdot \sqrt{2}}{4}, k \right)$   $k = \frac{11}{2}$

### Question 6

Answer: B 21.55 is closest to the exact answer

$solve \left( area = \frac{80 + 7 \cdot \sqrt{2}}{4}, k \right)$   $k = \frac{11}{2}$

© Question 6: Decimal ans: <ctrl>+<enter>

$\int_{-1}^2 g(x) dx | k = \frac{11}{2}$  21.5494

### Question 7

Answer: C  $-\frac{1}{12}$

© Question 7

$\int_{-3}^3 (a \cdot (x^2 + 1)) dx$   $24 \cdot a$

$solve(24 \cdot a = -2, a)$   $a = \frac{-1}{12}$