

Infinite series (16th and 17th century)

- Indian mathematician Nilakantha Somayaji (1444–1544)
- German mathematician Gottfried Wilhelm Leibniz (1646-1716)
- Scottish mathematician James Gregory (1638-1675)
- Swiss mathematician Leonard Euler (1707-1783)
- (science-math connection related to Basel problem <http://bit.ly/BaselPi>)

- $$\pi = 3 + \frac{4}{2 \times 3 \times 4} - \frac{4}{4 \times 5 \times 6} + \frac{4}{6 \times 7 \times 8} - \frac{4}{8 \times 9 \times 10} + \dots$$

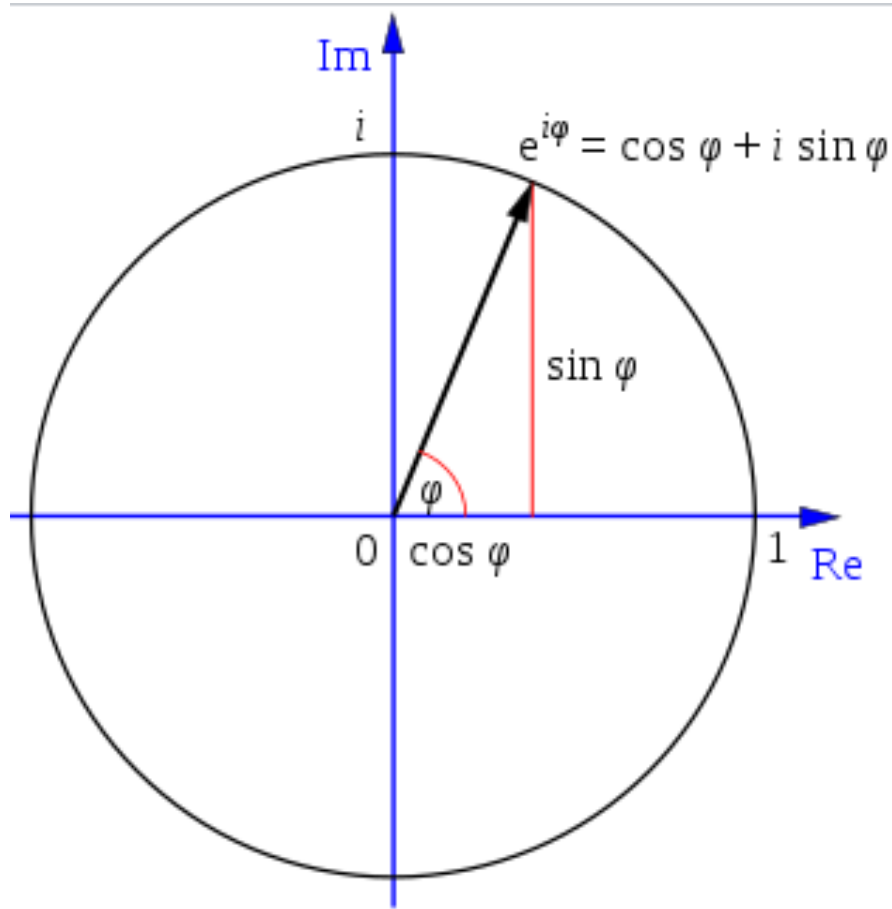
- $$\frac{\pi}{4} = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots$$

- $$\frac{\pi^2}{6} = \frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots$$

Nilakantha series

- $\pi = 3 + \frac{4}{2 \times 3 \times 4} - \frac{4}{4 \times 5 \times 6} + \frac{4}{6 \times 7 \times 8} - \frac{4}{8 \times 9 \times 10} + \dots$
- *Partial sum:*
- $u_n = 3 + \sum_{k=1}^n \frac{4(-1)^{k-1}}{(2k)(2k+1)(2k+2)} = 3 + \sum_{k=1}^n \frac{(-1)^{k-1}}{k(k+1)(2k+1)}$

Euler's formula



- $e^{i\pi} = \cos(\pi) + i \cdot \sin(\pi)$
- $e^{i\pi} = -1 + i \cdot 0$

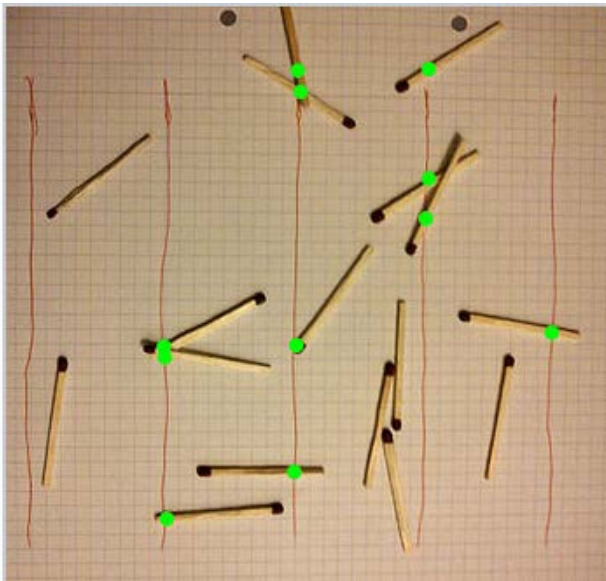
$$e^{i\pi} + 1 = 0$$

$$\pi = -i \cdot \ln(-1)$$

Buffon's Needle Problem

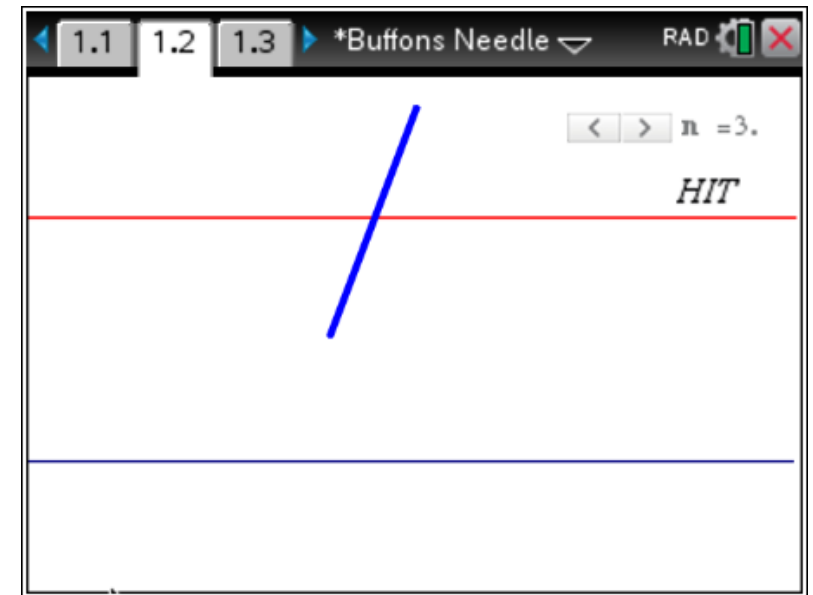
(French mathematician Georges-Louis Leclerc, Comte de Buffon, 18th century)

- Suppose we have a floor made of parallel strips of wood, each the same width, and we drop a needle onto the floor. What is the probability that the needle will lie across a line between two strips?
- Consider a special case when the length of the needle is equal to the distance between the strips.



Hands-on version of activity
shows 11 hits out of 17 throws

TI-Nspire simulation (available at
[Australian TI site](http://www.australianmaths.com.au/ti-nspire/buffons-needle/))



Estimating π from Buffon's needle problem

- P - is the probability that the needle crosses the line
- Region $x \leq L \cos(\theta)$ out of region $0 \leq x \leq l$ where $0 \leq \theta \leq \frac{\pi}{2}$,

$$P = \frac{\int_0^{\frac{\pi}{2}} l \cos(\theta) d\theta}{\int_0^{\frac{\pi}{2}} l d\theta} = \frac{\sin\left(\frac{\pi}{2}\right)}{\frac{\pi}{2}} = \frac{2}{\pi}$$

$$\pi = \frac{2}{P}$$

