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| **Math Objectives*** Students will find the solution to a system of linear equations by hand.
* Students will use the TI-Nspire CX II to graph a linear system in two variables and find the intersection point(s).
* Students will create and graph linear piecewise functions.
* Students will try to make a connection with how to understand these topics in IB Mathematics courses and on their final assessments.

**Vocabulary*** linear system • piecewise function

**About the Lesson*** This lesson is aligning with the curriculum of IB Mathematics Applications and Interpretations SL/HL and IB Mathematics Approaches and Analysis SL/HL
* This falls under the IB Mathematics Core Content Topic 2 Functions:

**2.4b** Finding the point of intersection of two curves or lines using technology.* As a result, students will:

 Apply this information to real world situations**HH_SW_iconsTI-Nspire™ Navigator™*** Transfer a File.
* Use Class Capture to examine patterns that emerge.
* Use Live Presenter to demonstrate.
* Use Teacher Edition computer software to review student documents.
* Use Quick Poll to assess students’ understanding

**Activity Materials*** Compatible TI Technologies: **Trail Blaszer:Users:ronblasz:Documents:WIP:CL947_Platform icons:Handheld_icon.png** TI-Nspire™ CX Handhelds, Trail Blaszer:Users:ronblasz:Documents:WIP:CL947_Platform icons:Tablet_icon.png TI-Nspire™ Apps for iPad®, Trail Blaszer:Users:ronblasz:Documents:WIP:CL947_Platform icons:Software_icon.png TI-Nspire™ Software
 | **Tech Tips:*** This activity includes screen captures taken from the TI-Nspire CX II handheld. It is also appropriate for use with the TI-Nspire family of products including TI-Nspire software and TI-Nspire App. Slight variations to these directions may be required if using other technologies besides the handheld.
* Watch for additional Tech Tips throughout the activity for the specific technology you are using.
* Access free tutorials at <http://education.ti.com/calculators/pd/US/Online-Learning/Tutorials>

**Lesson Files:***Student Activity*Which\_Garage\_is\_Better\_Student-Nspire.pdfWhich\_Garage\_is\_Better\_Student\_Nspire.docWhich\_Garage\_is\_Better.tns |
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| **Tech Tip:** Before beginning the activity, it may be beneficial to discuss with students how to graph a piecewise function on the handheld and where to find it under the math template button. |
| **Teacher Tip:** Students may also follow along with this activity on the handheld by downloading the file *Which\_Garage\_is\_Better.tns.* |

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| **1.** Complete the table.

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| **Length of time in the garage (hours)** | **Blue Street Garage total cost (dollars)** | **Red Street Garage total cost (dollars)** |
| 0 | **10** | **0** |
| 1 | **10** | **7** |
| 2 | **15** | **14** |
| 3 | **20** | **21** |
| 4 | **25** | **28** |
| 5 | **30** | **35** |
| 6 | **35** | **35** |
| 7 | **40** | **35** |
| 8 | **45** | **35** |
| 9 | **50** | **35** |

 **Answer:** Students may find it easier to compete the table for the Red Street Garage  first. Using the slope, students might build the table for the Blue Street Garage by adding 5 to the previous row of the table. |
| **2.** Joe parked in the Blue Street Garage and Flo parked in the Red Street Garage for the same length of time. After they checked out and paid, they asked each other which garage was cheaper, only to discover they paid the same amount for their stay.  Using the table above, answer the following questions: (a) Find the length of time each might have parked in the garage. Find all possible  answers. **Answer:** Each could have stayed 6 hours and paid $35, but that is not the only  possible answer. Red surpasses Blue between 2 and 3 hours. Using  proportional reasoning, for each half hour the cost of the Blue Street  Garage increases by ½ of 5 or $2.50, and the cost of the Red Street  Garage increases by ½ of 7 or $3.50. (b) Find what their fee would have been. Find all possible answers. **Answer:** Each could have stayed only 2.5 hours and paid $17.50. This will be more apparent with the graph. |
| **3.** Write the equations of piecewise functions that model the cost of staying in each of the garages. Blue Street Garage: *B*(*x*) =  **Answer:**  Red Street Garage: *R*(*x*) = **Answer:**  |
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| **Teacher Tip:** If your students are new to writing piecewise functions, a scaffolding idea is to give them the structure and have them fill in the rest of it. For example, give them the first line and let them figure out the second part. |

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| **4.** Move to **page 1.4**. To graph a piecewise function on your TI-Nspire CX II, on a graph page, press **tab** if the entry line is not showing, press the **math template button** and select the **two piece piecewise function template** (one to the right of the log template). Enter your equations and inequalities into the four empty boxes. You will repeat this for the Red Street Garage as well. Your graph should look like the one to the right using the viewing window shown. **Answer:**  |  |
| **5.** Find when the costs for using each garage will be equal to each other. Write down the equations you would set equal to each other to find when the costs are equal. Solve these equations below. Verify your answer by examining the intersection on the handheld. Press **menu**, **6 Analyze Graph**, **4 Intersection**. Equation 1: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ **Answer:**     Equation 2: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_**Answer:**     |
| **6.** Move to **page 1.5**. Use the table, formula, or graph to answer the following. Press **ctrl t** for the **table**. a. Find which garage costs less for a short stay. For example, you enter the garage, park, realize you forgot your wallet, and end up having to leave only 15 minutes later. **Answer:** Students may need to be reminded of units. They can evaluate each function at x = 0.25 hours or just use the graph. The Red Street Garage is cheaper since the blue Street Garage is $10 and the Red Street Garage is $1.75.b. Move to **page 1.6**. Suppose after a 2.5-hour movie you decide to go out to a restaurant and stay an additional 2 hours. Find which garage will cost less. State how much less. **Answer:** If you stay 4.5 hours, the Blue Street Garage ($25 + $2.50 = $27.50) is cheaper than the Red Street Garage (4.5 x $7 = $31.50) by $4. You can also use the table feature on the handheld.c. Move to **page 1.7**. Suppose you needed to park your car for 12 hours in the garage. State which garage will cost less. State how much less. **Answer:** If you stay 12 hours, the Red Street Garage ($35) is cheaper than the Blue Street Garage ($10 + $55 = $65) by $30. You can also use the table feature on the  handheld. |
| **7.** Move to **page 1.8**. Use the graph to solve when . Interpret the solution in real-world practical terms. **Answer:** In terms of the context of parking  garages, the Blue Street Garage is cheaper  than the Red Street Garage if you stay more  than 2.5 hours but less than 6 hours.  |  |
| **8.** Move to **page 1.9**. Over the length of a day, find what duration the Blue Street Garage is better. Find what duration the Red Street Garage is better. **Answer:** The Blue Street Garage is better for a duration of 3.5 hours (when you stay more than 2.5 hours but less than 6 hours). The Red Street Garage is better for the remaining 20.5 hours of the day (for hours 0 to 2.5 and 6 to 24). |
| **Problem 2 – Music Sales** |
|  Move to **page 2.1**. In recent years, the numbers of CDs sold in the United States has  declined while digital music has become the new method for purchasing music. The table below, and on **page 2.2**, shows data of the sales, in millions, of CDs, digital albums (**DA**), and individual songs (**IS**) for the first three months of the year.

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| --- | --- | --- | --- |
| **Year** | **CD** | **DA** | **IS** |
| 2006 | 112 | 119 | 24.2 |
| 2007 | 89 | 99 | 28.8 |
| 2007 – 2006  | -23 | -20 | 4.6 |

9**.** Move to **page 2.3**. Describe what the value of -23 (under CD) represents. **Answer:** The difference between the sales data for CDs and, since there is only a difference of one year, it is also equal to the slope of the line.10.Move to **page 2.4**. Discuss with a classmate and write down why you think it is negative. **Answer:** Because there was a decrease in sales of CDs from 2006 to 2007.11**.** Discuss with a classmate how the result in the final column (IS) is different from theother two (CD and DA) and explain why. **Answer:** The result is positive because the individual song sales went up for the same  time period. |
| **12.** Move to **page 2.5**. Use the data in the table above to find the equation for each of the  three lines in either slope‑intercept form or point-slope form and write them in the  spaces provided.* CDs \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

 **Answer:** * Digital Albums \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

 **Answer:** * Individual Songs \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

 **Answer:**  |
| Move to **page 2.6**. Use the lines to find and record the coordinates of the three intersection points. CDs and Digital Albums (\_\_\_\_\_\_\_\_\_\_\_\_ , \_\_\_\_\_\_\_\_\_\_\_\_\_\_) **Answer:** CDs and Individual Songs (\_\_\_\_\_\_\_\_\_\_\_\_ , \_\_\_\_\_\_\_\_\_\_\_\_\_\_) **Answer:**  Digital Albums and Individual Songs (\_\_\_\_\_\_\_\_\_\_\_\_ , \_\_\_\_\_\_\_\_\_\_\_\_\_\_) **Answer:**  |
| **13.**  Move to **page 2.7**. Find when the sales of digital albums overtakes the CDs. **Answer:** The later part of 2003.**14.**  Move to **page 2.8**. Find when the graph projects that the sales of individual songs  overtakes CDs. **Answer:** The beginning part of 2009.**15.**  Move to **page 2.9**. Find when the graph projects that the sales of individual songs overtakes digital albums. **Answer:** The later part of 2009.**16.**  Move to **page 2.10**. As time goes on according to the graph, it indicates the CD sales becoming zero. Discuss with a classmate if you think this is possible. Explain why or why not. **Answer:** The sales of CDs will continue to go down but probably will not go away, untilthe industry decides to stop making CDs. |
| **IB Further Extension**To further instruction, finding where two functions are equal should not be limited to linear functions. In this extension, you will be exploring where two exponential functions are equal.Luca purchases a new bike for himself at a cost of $355. He also purchases a professional racing bike for his sister Christine for $1815. Luca’s bike will depreciate in value 5% per year, while Christine’s will depreciated at a rate of 12% per year. Luca and Christine’s bikes will have the same value *p* years after they were purchased. (a) Estimate the value of Luca’s bike after 6 years. **Answer:** Students will first have to write the given information as an exponential equation. Luca:   (b) Using your handheld, find *p*. **Answer:** Christine:   Set the exponential equations equal to solve for *p.*  Finding their point of intersection using the graphs on their handheld,  After approximately years, their bikes will have an approximate value of  $118.94.(c) Explain why or why not the answer to part (b) is valid.  **Answer:** Depreciation rates are not constant from year to year, especially over long periods of time. |

**TI-NspireTM NavigatorTM Opportunities**

***Quick Poll***

Since every question is part of the tns file, you may choose to use Quick Poll to assess student understanding. The worksheet questions can be used as a guide for possible questions to ask.

***Class Capture***

You may want to use Class Capture from time to time to verify that students are understanding the process, especially the process involving piecewise functions.

*\*\*Note: This activity has been developed independently by Texas Instruments and aligned with the IB Mathematics curriculum, but is not endorsed by IB™. IB is a registered trademark owned by the International Baccalaureate Organization.*