**Students may also follow along with this activity on the handheld by downloading the file *Which\_Garage\_is\_Better.tns.***

Move to **page 1.2.**

**Problem 1 – A Parking Garage**

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| The cost schedules for two different parking garages are below. The maximum stay is 24 hours.   |  |  | | --- | --- | | **Blue Street Garage** | | | **Length of time in the garage** | **Cost** | | 1 hour or less | A flat fee of $10. | | More than 1 hour | $10 for the first hour plus an additional fee of $5 for every hour after your first hour in the garage. | |  | | | **Red Street Garage** | | | **Length of time in the garage** | **Cost** | | 5 hours or less | $7 per hour | | More than 5 hours | A flat fee of $35 | |

**1.** Complete the table.

|  |  |  |
| --- | --- | --- |
| **Length of time in the garage (hours)** | **Blue Street Garage total cost (dollars)** | **Red Street Garage total cost (dollars)** |
| 0 |  |  |
| 1 |  |  |
| 2 |  |  |
| 3 |  |  |
| 4 |  |  |
| 5 |  |  |
| 6 |  |  |
| 7 |  |  |
| 8 |  |  |
| 9 |  |  |

**2.** Joe parked in the Blue Street Garage and Flo parked in the Red Street Garage for the  
 same length of time. After they checked out and paid, they asked each other which  
 garage was cheaper, only to discover they paid the same amount for their stay.

Using the table above, answer the following questions:

(a) Find the length of time each might have parked in the garage. Find all possible   
 answers.

(b) Find what their fee would have been. Find all possible answers.

|  |  |  |
| --- | --- | --- |
|  | | |
| **3.** Write the equations of piecewise functions that model the cost of staying in each of the garages.  Blue Street Garage: *B*(*x*) =  Red Street Garage: *R*(*x*) = | | |
| **4.** Move to **page 1.4**. To graph a piecewise function on your TI-Nspire CX II, from a graph page (make sure the graph is clear and the entry line is showing), press the **math template button**, then the **two piece piecewise function template** (one to the right of the log template). Enter your equations and inequalities into the four empty boxes. You will repeat this for the Red Street Garage as well. Your graph should look like the one to the right using the viewing window shown. | |  |
| **5.** Find when the costs for using each garage will be equal to each other. Write down the equations you would set equal to each other to find when the costs are equal. Solve these equations below. Verify your answer by examining the intersection on the handheld. Press **menu**, **6 Analyze Graph**, **4 Intersection**.  Equation 1: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_  Equation 2: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ | | |
| **6.** Move to **page 1.5**. Use the table, formula, or graph to answer the following. Press **ctrl t** for the **table**.  a. Find which garage costs less for a short stay. For example, you enter the garage, park, realize you forgot your wallet, and end up having to leave only 15 minutes later.  b. Move to **page 1.6**. Suppose after a 2.5-hour movie you decide to go out to a restaurant and stay an additional 2 hours. Find which garage will cost less. State how much less.  c. Move to **page 1.7**. Suppose you needed to park your car for 12 hours in the garage. State which garage will cost less. State how much less. | | |
| **7.** Move to **page 1.8**. Use the graph to solve when . Interpret the solution in real-world practical terms. |  | |
| **8.** Move to **page 1.9**. Over the length of a day, find what duration the Blue Street Garage is better. Find what duration the Red Street Garage is better. | | |
| **Problem 2 – Music Sales** | | |
| Move to **page 2.1**. In recent years, the numbers of CDs sold in the United States has   declined while digital music has become the new method for purchasing music.  The table below, and on **page 2.2**, shows data of the sales, in millions, of CDs, digital albums (**DA**), and individual songs (**IS**) for the first three months of the year.   |  |  |  |  | | --- | --- | --- | --- | | **Year** | **CD** | **DA** | **IS** | | 2006 | 112 | 119 | 24.2 | | 2007 | 89 | 99 | 28.8 | | 2007 – 2006 | -23 | -20 | 4.6 | | | |
| **9.** Move to **page 2.3**. Describe what the value of -23 (under CD) represents.  **10.**  Move to **page 2.4**. Discuss with a classmate and write why you think it is negative.  **11.**  Discuss with a classmate how the result in the final column (IS) is different from the  other two (CD and DA) and explain why. | | |
| **12.** Move to **page 2.5**. Use the data in the table above to find the equation for each of the   three lines in either slope‑intercept form or point-slope form and write them in the   spaces provided.   * CDs \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ * Digital Albums \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ * Individual Songs \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_   Move to **page 2.6**. Use the lines to find and record the coordinates of the three intersection  points.  CDs and Digital Albums (\_\_\_\_\_\_\_\_\_\_\_\_ , \_\_\_\_\_\_\_\_\_\_\_\_\_\_)  CDs and Individual Songs (\_\_\_\_\_\_\_\_\_\_\_\_ , \_\_\_\_\_\_\_\_\_\_\_\_\_\_)  Digital Albums and Individual Songs (\_\_\_\_\_\_\_\_\_\_\_\_ , \_\_\_\_\_\_\_\_\_\_\_\_\_\_) | | |
| **13.**  Move to **page 2.7**. Find when the sales of digital albums overtakes the CDs.  **14.**  Move to **page 2.8**. Find when the graph projects that the sales of individual songs   overtakes CDs.  **15.**  Move to **page 2.9**. Find when the graph projects that the sales of individual songs  overtakes digital albums.  **16.**  Move to **page 2.10**. As time goes on according to the graph, it indicates the CD sales  becoming zero. Discuss with a classmate if you think this is possible. Explain why or  why not. | | |

**IB Further Extension**

To further instruction, finding where two functions are equal should not be limited to linear functions. In this extension, you will be exploring where two exponential functions are equal.

Luca purchases a new bike for himself at a cost of $355. He also purchases a professional racing bike for his sister Christine for $1815. Luca’s bike will depreciate in value 5% per year, while Christine’s will depreciated at a rate of 12% per year. Luca and Christine’s bikes will have the same value *p* years after they were purchased.

(a) Estimate the value of Luca’s bike after 6 years.

(b) Using your handheld, find *p*.

(c) Explain why or why not the answer to part (b) is valid.