|  |  |  |
| --- | --- | --- |
| **Math Objectives**   * Students will analyze and discuss 3D objects and the 2D shapes that make up those objects. * Students will unfold 3D objects to aid in finding both the Surface Area and Volume of the objects. * Students will apply this knowledge to finding the Surface Area and Volume of real world objects. * Students will try to make a connection with how to understand these topics in IB Mathematics courses and on their final assessments.   **Vocabulary**   * Circle • Circumference • Sector * Cylinder • Surface Area • Volume   **About the Lesson**   * This lesson is aligning with the curriculum of IB Mathematics Applications and Interpretations SL/HL and IB Mathematics Approaches and Analysis SL/HL * This falls under the IB Mathematics Core Content Topic 3 Geometry and Trigonometry:   **3.1b** Volume and surface area of three-dimensional solids including right pyramid, right cone, cylinder, sphere, hemisphere, and combinations of these solids.   * As a result, students will: * Apply this information to real world situations   **Teacher Preparation and Notes**   * This activity is done with the use of the TI-84 family as an aid to the problems.   **Activity Materials**   * Compatible TI Technologies:   TI-84 Plus\*, TI-84 Plus Silver Edition\*, TI-84 Plus C Silver Edition, TI-84 Plus CE  *\* with the latest operating system (2.55MP) featuring MathPrintTM  functionality.* | **Tech Tips:**   * This activity includes screen captures taken from the TI-84 Plus CE. It is also appropriate for use with the rest of the TI-84 Plus family. Slight variations to these directions may be required if using other calculator models. * Watch for additional Tech Tips throughout the activity for the specific technology you are using. * Access free tutorials at <http://education.ti.com/calculators/pd/US/Online-Learning/Tutorials>   **Lesson Files:**  *Student Activity*  3D\_Surface\_Area\_and\_Volume\_Student-84.pdf  3D\_Surface\_Area\_and\_Volume\_Student-84.doc | |
| |  |  |  |  | | --- | --- | --- | --- | | |  | | --- | | **Review**  In this activity, you will be finding both the Surface Area and Volume of several 3D objects. The following formulas will be useful:  Right Cylinder Rectangular Prism Right Cone Sphere  Surface Area:    Volume:    **Problem 1**  Before we start finding the Surface Area and Volume, let us practice unfolding 3D objects. First, the right cylinder. Discuss with a classmate what three 2D shapes you can unfold this cylinder into. Also, mention how the dimensions of the 2D shapes are found.    **Possible discussion points:**  The cylinder can be unfolded into two circles (the top and bottom) and a rectangle.  The length of the rectangle is the circumference of the  circular top or bottom and the width of the rectangle is  the height of the cylinder.  Second, the rectangular prism. Discuss with a classmate what six possible 2D shapes you can unfold  this rectangular prism into. Also, mention how the dimensions of the 2D shapes are found.  **Possible discussion points:**  The rectangular prism can be unfolded into 6 total rectangles.  The length of the prism is the length of one rectangle,  the height of the prism is the width of one rectangle,  and the width of the prism is the length of one of the  end rectangles.  And finally, a right cone. Discuss with a classmate what two 2D shapes you can unfold this right cone  into. Also, mention how the dimensions of the 2D shapes are found.    **Possible discussion points:**  The right cone can be unfolded into a sector (of a circle) and a circle.    The radius of the sector is the slant height of the cone found  by creating a right triangle with the height as a leg, the radius  as the other leg and the hypotenuse is the slant height.  **Problem 2**  Find the Surface Area and Volume of each of the following 3D objects:  (a) A right cylinder with a height of 8 in. and with a base that has a diameter of 4 in.  4 in.  8 in.  **Solution:**          (b) A rectangular prism with a length of 3 ft., a width of 2 ft., and a height of 30 in.  30 in.  2 ft.  3 ft.  **Solution:**  **\*\***First convert the height from 30 in. to 2.5 ft        (c) A right cone with a height of 18 cm and its base has a radius of 5 cm.    18 cm  5 cm  **Solution:**        **Problem 3**  Given the ice cream cone below is made up of a hemisphere scoop of vanilla ice cream and a right sugar cone, find the total surface area and volume of the entire cone and ice cream.  r = 1.5 in.  Ice Cream Cones: The True Story - America Comes Alive    h = 4.625 in.  **Solution:**        **Problem 4**  The water below has a half of a sphere dome as the top. Find the total surface area of the entire water bottle, and if only the bottom cylindrical portion of the bottle can hold liquid, find how much it can hold.  r = 1 cm  Baseline® Plus 750 ml dome lid sport bottle | Leoprinting 1.3 cm  h = 17 cm  r = 4.5 cm |   **Solution:**  There are actually **two** cylinders in the water bottle where you only find the surface area of one of its bases.         |  | | --- | | **Teacher Tip:** After doing each of the real-world Surface Area and Volume problems, it would be a good place to have a discussion about accuracy due to the 3D objects, when combined, are not a perfect fit or that there might be some irregularities in the making of the objects. If time permits, you can do a class experiment and bring in ice cream cones and ice cream and have the students collect their own measurements and check for accuracy. |   **Extension**  **Problem 5**  The entire rectangular toy chest below with a half cylindrical top needs to be stained. If the stain costs $25.95 to cover 2 square feet of surface, find the surface area of the entire chest and the cost of the stain you will need to cover it.  DIY Glowing Night Light Treasure Chest - TheDIYPlan  10 in.    8 in. 20 in.  **Solution:**  You will use the Surface Area formula for a rectangular prism, but that needs to be adjusted due to the top being half a cylinder.    **Method 1:**  Since the stain cost is in , you can convert each measurement from inches to feet and plug into the formula:      **Method 2:**  You also have the option to leave your dimensions in inches, but then at the end, since there are 12 inches in a foot, and you are looking for , you would divide your answer by .        **Total cost of the stain:**     |  | | --- | | **Teacher Tip:** Please know that in this activity there is a lot of time dedicated to students talking with one another and sharing their thoughts with the class. The goal here is to not only review Surface Area and Volume of 3D objects, but also to generate discussion. | | | |

*\*\*Note: This activity has been developed independently by Texas Instruments and aligned with the IB Mathematics curriculum, but is not endorsed by IB™. IB is a registered trademark owned by the International Baccalaureate Organization.*