Radio Station KTNS Student Activity

Open the TI-Nspire document Radio Station KTNS.tns.

In this activity, you will explore a real-world example of the Law of Sines and the Law of Cosines.

Radio Station KTNS is located at point P in the figure. The range of its signal is r miles, meaning that people within r miles of P would be able to hear the station. You are driving along road OM at an angle of 30° with OP. For how many miles, d, could you hear station KTNS?

hear radio station KTNS if the range of the radio station is r miles?" in two ways empirically and theoretically. 1.1 1.2 1.3 ▶ Radio_St...re

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r =6.4 **d=4.**39 12 1

In ΔPAB , the Law of Cosines tells us that $d^2 = 2r^2 - 2r^2 \cdot \cos(\angle APB)$, so it is reasonable to assume

that d^2 could be a linear function of r^2 . To solve this problem, you will determine d^2 in terms of r^2 in two ways:

- Find an experimental model by gathering data and fitting an appropriate regression function to the data.
- Find a theoretical model using the Law of Sines, the Law of Cosines, and algebra.

Move to page 1.2.

Press ctrl > and ctrl < to

navigate through the lesson.

The figure is a scale drawing with 1 unit = 10 miles so that OP = 12 units or 120 miles.

1. In miles, the reasonable values of r satisfy $k < r \le 120$. What is the value of k? Why?

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Using the slider, the following data has been gathered in the spreadsheet in the four $dis(d) \quad r2 = r^2 \quad d2 = d^2$ columns: *rad(r)*

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A scatterplot of the data has been drawn on this page.

You will solve the problem: "As you drive

along road OM, for how many miles can you

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2. Fit a linear regression function to the data with $x = r^2$ and $y = d^2$ in units. Select **MENU** >

Statistics > Stat Calculations > Linear Regression (mx+b). with r^2 for X List, d^2 for Y List, and Save RegEqn to: f^1 .

Record your answer here: $d^2 = \underline{\qquad} r^2 - \underline{\qquad}$.

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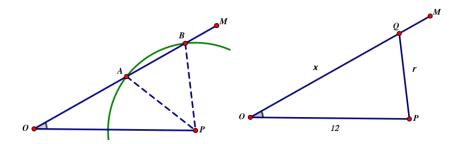
3. Plot the regression equation on the scatterplot, and note how well it fits. Open the entry line, move back up to f(x), and press enter.

According to this linear model, for how many miles, d, could you hear the station if r = 90 miles? Hint: Remember r = 9 units corresponds to r = 90 miles.

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Theoretical Model

Find the theoretical function expressing d^2 in terms of r^2 by completing the argument below.



4. The figure for this problem shows an example of an ambiguous case of the Law of Sines since there are two triangles with two sides OP = 12, r, and the non-included angle of 30°. Consequently, if we apply the Law of Cosines to a triangle with sides OP = 12, r, x and angle 30°, we obtain the equation:

_____= 0.

On the scale drawing, then, the two solutions for *x* are *OA* and *OB*, and the distance, *d*, is d = OB - OA.

5. a. Find the two solutions for *x* of this equation._____ Hint: You can use "solve" command. Both solutions will be functions of r^2



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b. Find the difference of the two solutions and express d^2 in terms of r^2 in units:

*d*² = _____

- 6. How does your theoretical equation compare to the regression equation?
- 7. According to this theoretical model, for how many miles, d, could you hear the station if r = 90 miles?

Hint: Remember r = 9 units corresponds to r = 90 miles.

8. Suppose the angle between the two roads *OP* and *OM* is changed to θ° . Express d^2 in terms of r^2 and θ :

*d*² = _____