## Running Circles Around Quads

ID: 12144

Time Required

15 minutes

## Activity Overview

In this activity, students will explore various properties of cyclic quadrilaterals.

## Topic: Quadrilaterals \& General Polygons

- Cyclic Quadrilaterals


## Teacher Preparation and Notes

- To complete this activity, students will need to know how to change between pages, grab and move points.
- The multiple-choice items are self-check and students can check them by pressing (tri) $+\boldsymbol{\Delta}$.
- To download the student TI-Nspire document (.tns file) and student worksheet, go to education.ti.com/exchange and enter "12144" in the quick search box.


## Associated Materials

- CirclesAroundQuads_Student.doc
- CirclesAroundQuads.tns


## Suggested Related Activities

To download any activity listed, go to education.ti.com/exchange and enter the number in the quick search box.

- Opposite Angles in Cyclic Quadrilaterals (TI-84 Plus family) - 6800
- Cyclic Quadrilaterals (TI-Nspire technology) - 9691
- Cyclic Quadrilaterals (TI-89 Titanium) - 4598


## Problem 1 - Properties of Cyclic Quadrilaterals

Students will begin this activity by looking at properties of cyclic quadrilaterals. They will discover that opposite angles are supplementary.

Students will be asked to collect data when $Q$ is on the circle and then be asked to collect data when they redefine $Q$ to be a point not on the circle. Students will need to use the Redefine tool (MENU > Actions > Redefine). To redefine the point, students will need to move to point $Q$ and press enter, then move to a point outside of the circle and press enter again.

Finally, students will be asked several always-sometimes-never questions. Students should use the properties of opposite angles to select the correct choice.

## Problem 2 - Extension

In Problem 2, students can discover properties of angles created by the diagonals of a cyclic quadrilateral.

On page 2.2, students are given the measure of angles $Q, U, A, D, D Q A$, and $D U A$. They should move point $Q$ to four different points and collect data in the table on the accompanying worksheet.


## Student Solutions

1. Sample answers:

| Position | $\angle \boldsymbol{Q}$ | $\angle \boldsymbol{U}$ | $\angle \boldsymbol{A}$ | $\angle \boldsymbol{D}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 91 | 89 | 89 | 91 |
| $\mathbf{2}$ | 91 | 107 | 89 | 73 |
| $\mathbf{3}$ | 91 | 119 | 89 | 61 |
| $\mathbf{4}$ | 91 | 54 | 89 | 126 |

2. Opposite angles are supplementary.
3. Sample answers:

| Position | $\angle \boldsymbol{Q}$ | $\angle \boldsymbol{U}$ | $\angle \boldsymbol{A}$ | $\angle \boldsymbol{D}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 73 | 107 | 89 | 91 |
| $\mathbf{2}$ | 76 | 95 | 89 | 100 |
| $\mathbf{3}$ | 81 | 78 | 89 | 112 |
| $\mathbf{4}$ | 117 | 65 | 89 | 88 |

4. No relationship exists.
5. sometimes
6. sometimes
7. always
8. sometimes
9. always
10. always
11. sometimes
12. Sample answers:

| Position | $\angle \boldsymbol{Q}$ | $\angle \boldsymbol{U}$ | $\angle \boldsymbol{A}$ | $\angle \boldsymbol{D}$ | $\angle D Q A$ | $\angle D U A$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 102 | 95 | 78 | 85 | 51 | 51 |
| $\mathbf{2}$ | 94 | 95 | 106 | 105 | 43 | 43 |
| $\mathbf{3}$ | 72 | 95 | 108 | 105 | 21 | 21 |
| $\mathbf{4}$ | 130 | 95 | 50 | 85 | 79 | 79 |

13. They are congruent.
