## Hit the brakes, Charles!

Student Activity
$\begin{array}{llllll}7 & 8 & 9 & 10 & \mathbf{1 1} & \mathbf{1 2}\end{array}$


TI-Nspire


Investigation


Student


60 min

## Introduction

## Hit the brakes, Charles! - bivariate data including $\mathrm{x}^{2}$ data transformation

As soon as Charles got his P's he did some real data collection for his mathematics project. He decided to check whether the Auto Club figures for stopping distances and speed were true.

The table below shows the speed in $\mathrm{km} / \mathrm{h}$ when Charles hit the brakes with the distance in $m$ it took him to come to a complete stop.

| Speed km/h | 40 | 60 | 70 | 80 | 90 | 110 | 120 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Stopping <br> distance m | 29 | 55 | 67 | 96 | 112 | 168 | 223 |

## Problem 1A

Construct a data table in the Lists \& Spreadsheet page using the variables speed and distance.


What variable (speed or distance) will you use for the explanatory (independent) variable? On what axis will this be placed?


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Student: Type response here.

## Problem 1B

Construct a scatter plot showing the relationship between the speed and braking distance.

Insert a Data \& Statistics page.
Add the variables to the axes by clicking on the Click to add variable boxes or press tab to go to the variables list.

Describe the relationship between the two variables.

Perform a Quadratic regression on the data using menu >Analyze>Regression>Show Quadratic

Use the regression equation in a Calculator page to predict the stopping distance (to the nearest metre) of a car travelling at $50 \mathrm{~km} / \mathrm{h}$.

Hint: the regression equation can be recalled by pressing var and scrolling to stat.regeqn and adding (x).

Answer: m.

Note: If you are asked to do a data transformation to linearise (e.g. VCE Further Mathematics) then this answer is not acceptable. Instructions on this procedure follows; for courses not requiring linearization, you may be given the transformed data to continue as a linear relationship.

## Problem 2A

Apply an $x^{2}$ transformation.
Use ctrl + to return to the Lists \& Spreadsheet. Label the new list as spdsq. Enter the formula in the formula cell shown opposite i.e. $=$ speed $^{2}$

Hint: use the var key to paste in list variables to avoid any typing errors.

|  | 1.11 .2 | Brake - student $\nabla$ |  | DEG $\left.{ }^{1}\right]$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\checkmark$ | A speed | $B$ distance | ${ }^{C}$ distsq | D | 슷 |
| $=$ |  |  |  |  |  |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 |  |  |  |  |  |
| 4 |  |  |  |  |  |
| 5 |  |  |  |  | $\checkmark$ |
|  | distsq |  |  | 4 | - |

[^0]Construct a scatter plot on a new Data \& Statistics page showing the relationship between $y$ (distance) and $x^{2}$ (speed squared). You will need to mouse click on the axes label to use the tab key to insert the variables.


To go to other existing pages in your document at any time press atrid to see thumbnail pages. Use your cursor to highlight the page you want and press enter. If you want the previous page you can also use ctrl +4 , similarly ctrr $+\square$ will give the next page.

## Problem 2B

Determine the least squares regression for this transformation.

On the linearised scatter plot page press
menu >Analyze>Regression>Show Linear (a+bx).
Note: your teacher will let you know if they prefer you to use Show Linear(mx+b)
Hint: to show the $r^{2}$ value when doing linear regressions press menu >Settings and tick the Diagnostic field, then select Make Default.

The regression equation, correct to 3 decimal places, is:
$y($ distance $)=$ $\qquad$ $+$ $\qquad$ x (speed squared)

A full statistical display can be shown in a Calculator page using menu >Statistics>Stat Calculations>Linear Regression (a+bx). Complete the table depending on the Linear model you have used.

| Using Linear $\mathbf{a + b x}$ | Using Linear $\mathbf{m x} \mathbf{+ b}$ |
| :--- | :--- |
| $\mathrm{a}=$ | $\mathrm{m}=$ |
| $\mathrm{b}=$ | $\mathrm{b}=$ |
| $\mathrm{r}=$ | $\mathrm{r}=$ |
| $\mathrm{r}^{2}=$ | $\mathrm{r}^{2}=$ |

Note: if you have performed a linear regression in the Data \& Statistics page you can access the statistics in the Calculator page by pressing var >Stat Results.

What is the meaning of the $r^{2}$ value in this practical example?

What is the value of $r^{2}$ and what does this mean in this example?

Student: Type response here.

By pressing menu >Analyze>Residuals>Show Residual Squares you can display the residual squares on the plot. These appear as boxes based on the vertical distances the points are from the regression line and also the numerical value is shown. This figure is the smallest sum of squares possible and the regression line is often referred to as the Least Squares Regression Line.

Use menu >Analyze>Residuals>Hide Residual Squares to remove this line before doing the next section.

## Problem 2C

Show a residual plot (residual vs speed squared) linearised data.
On Data \&Statistics page showing the transformed data plot with regression line press menu $>$ Analyze>Residuals>Show Residual Plot. You will see the original plot and the residual plot on the same screen.

Does the residual plot show any obvious pattern?

For a data transformation to be considered appropriate it must satisfy two things.
1.
2.

Was the $x^{2}$ transformation appropriate in this example?

Use the regression equation to predict the stopping distance (to the nearest metre) of a car travelling at 50 km/h

In the Calculator page recall the regression equation by pressing var and select stat.regeqn to paste to work area. You need to add ( x ) after pasting as shown. When substituting in the speed value remember that the $x$ now represents speed squared so enter as $50^{2}$.

How does this value compare to the one obtained earlier calculated from the quadratic regression?


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