# Exploring Inverse Functions—Teacher Notes

#### Activity Overview

Students will investigate the fundamental concept of an inverse, generate the inverse graphs of relations applying this concept, and algebraically determine the inverse.

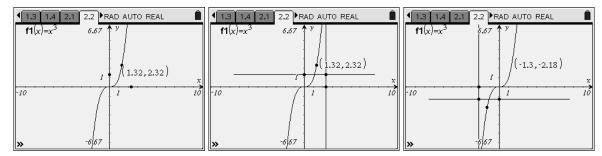
#### Materials

- Technology: TI-Nspire handheld, TI-Nspire CAS handheld, or TI-Nspire CAS computer software
- Documents: Inverse\_Functions.tns, Inverse\_Functions\_Student.doc

### **Student Solutions**

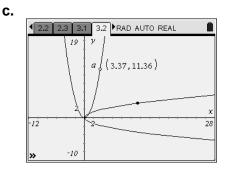
### **Inverses Point-by-Point**

- **1.** {(5, 2), (5, -4), (-2, -9), (-3, 0)}
- **2.** Point moves like the original function, only flipped about y = x.



### Inverses as a Graphical Relation

- 3. a. Moves like the original parabola turned on its side
  - b. Yes



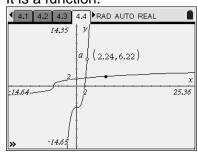
**d.** Two halves of  $y = \sqrt{x}$  and  $y = -\sqrt{x}$  or simply  $y^2 = x$ 

### Inverses as Functions

**4. a.** If there exists a horizontal line that intersects the graph at more than one point, then the inverse relation is not a function.



**b.** It is a function.



## **Finding Inverses Algebraically**

5.

5.1 5.2 5.3 5.4 RAD AUTO REAL	
ine $e(x)=x$	Done
$\operatorname{ine} f(x) = \sqrt{x^2 + 1}$	Done
x))	$\sqrt{x^2+1}$
κ))	$\sqrt{x^2+1}$
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6. a. Yes, it matches the locus.



**b.** The composition gives a result of *x*. This is important because the composition of a function with its inverse should give the identity function (maps x directly back to x).