Name $\qquad$
$\qquad$

## Problem 1 - A general trigonometric function

Using the Transformation Graphing app, press $Y$ and enter the general sine function in $\mathbf{Y}_{1}$,
$Y_{1}=A * \sin (B * X+C)+D$.
Complete the table.

| A | B | C | D | zero1 | zero2 | $\min$ | $\max$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 0 | 0 |  |  |  |  |
| 4 | $1 / 2$ | 3 | 1 |  |  |  |  |

## Problem 2 - The effect of the coefficients $A, B, C$, and $D$

## Examining A

- Set $B=1$ and $C=D=0$ and change the value of $A$. Try 4 different values of $A$.

| A | B | C | D | zero1 | zero2 | $\min$ | $\max$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 0 | 0 |  |  |  |  |
|  | 1 | 0 | 0 |  |  |  |  |
|  | 1 | 0 | 0 |  |  |  |  |
|  | 1 | 0 | 0 |  |  |  |  |

- How did the appearance of the graph change?
- Which graph features changed? Which did not change?
- Write equations to describe the relationship between $A$ and the features that did change.
- When $B=1$ and $C=D=0$, $\qquad$ .

The value of $A$ is the amplitude. It is equal to half of the difference between its maximum and minimum values.

- Calculate the amplitude from the minimum and maximum values in the table above.
- Compare the results to the values of $A$. What do you notice?


## Examining B

| $\boldsymbol{A}$ | $\boldsymbol{B}$ | $\boldsymbol{C}$ | $\boldsymbol{D}$ | zero1 | zero2 | $\min$ | $\max$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  | 0 | 0 |  |  |  |  |
| 1 |  | 0 | 0 |  |  |  |  |
| 1 |  | 0 | 0 |  |  |  |  |
| 1 |  | 0 | 0 |  |  |  |  |

- Try 4 different values of $B$. How did the appearance of the graph change?
- Which graph features changed? Which did not change?
- Describe the relationship between $B$ and the features that did change.


## Examining $C$

| $\boldsymbol{A}$ | $\boldsymbol{B}$ | $\boldsymbol{C}$ | $\boldsymbol{D}$ | zero1 | zero2 | $\min$ | $\max$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 |  | 0 |  |  |  |  |
| 1 | 1 |  | 0 |  |  |  |  |
| 1 | 1 |  | 0 |  |  |  |  |
| 1 | 1 |  | 0 |  |  |  |  |

- Try 4 different values of $C$. How did the appearance of the graph change?
- Which graph features changed? Which did not change?
- What is the effect of an increasing sequence of values for $C$ on the graph?
- What is the effect of a decreasing sequence of values for $C$ on the graph?


## Examining D

| $\boldsymbol{A}$ | $\boldsymbol{B}$ | $\boldsymbol{C}$ | $\boldsymbol{D}$ | zero1 | zero2 | $\min$ | $\max$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 0 |  |  |  |  |  |
| 1 | 1 | 0 |  |  |  |  |  |
| 1 | 1 | 0 |  |  |  |  |  |
| 1 | 1 | 0 |  |  |  |  |  |

- Try 4 different values of $D$. How did the appearance of the graph change?
- Try an increasing sequence of values for $D$ such as $0,1,2,3,4 \ldots$

What is the effect on the graph?

- Try a decreasing sequence of values for $D$ such as $0,-1,-2,-3,-4 \ldots$

What is the effect on the graph?

- Describe the effect of the value of $D$ on the graph. How does changing $D$ change the graph features?


## Problem 3 - A closer look at amplitude, period, and frequency

In $Y_{1}$, enter the general cosine function, $A^{*} \cos \left(B^{*} \boldsymbol{X}+\boldsymbol{C}\right)+\boldsymbol{D}$.
amplitude: half of the vertical distance from minimum value to maximum value period: horizontal distance from one peak (maximum point) to the next frequency: number of cycles per $2 \pi$ interval

- Write a formula to find the frequency $f$ given the period $p$.
- Use the formula to complete the table on the next page.

| $\boldsymbol{A}$ | $\boldsymbol{B}$ | $\boldsymbol{C}$ | $\boldsymbol{D}$ | max <br> point | min <br> point | next <br> max <br> point | amplitude | period | frequency |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: | :---: | :---: |
| 1 | 1 | 0 | 0 | $(0,1)$ | (3.14,-1) | $(6.28,1)$ | $1 / 2^{*}(1-(-1))$ <br> 2 | $6.28-0$ <br> 6.28 <br> $2 \pi$ |  |
|  | 1 | 0 | 0 |  |  |  |  |  |  |
| 1 | 1 | 0 | 0 |  |  |  |  |  |  |
| 1 |  | 0 | 0 |  |  |  |  |  |  |
| 1 | 1 |  | 0 |  |  |  |  |  |  |
| 1 | 1 |  | 0 |  |  |  |  |  |  |
| 1 | 1 | 0 |  |  |  |  |  |  |  |
| 1 | 1 | 0 |  |  |  |  |  |  |  |
| 1 | 1 | 0 |  |  |  |  |  |  |  |

- Based on the results in the table, determine and record each relationship:
- A and the amplitude
o $\quad B$ and the frequency
o $B$ and the period

