

**Law of Sines:  
The Ambiguous Case**

**Name:** \_\_\_\_\_  
**Date:** \_\_\_\_\_ **Period:** \_\_\_\_\_

*So far in your studies of the Law of Sines you have solved triangles given the measure of two angles and a side. In this exploration you will examine the use of the Law of Sines when given the measures of two sides and a non-included angle (sides  $a$  and  $b$  and angle  $A$ ). Open the TI-Nspire Document **Ambiguous LOS** and complete the following.*

1. Move point  $C$  on the figure so that when you rotate point  $B$  only one oblique triangle is formed with the marked angle  $A$ . Write an inequality relating  $a$  and  $b$ .
  
2. Move point  $C$  so that when you rotate point  $B$  two triangles can be formed with the marked angle  $A$ . Write an inequality relating  $a$ ,  $b$ , and  $h$ .
  
3. Move point  $C$  so that when you rotate point  $B$  a right triangle is formed. How does  $a$  compare to  $h$ ?
  
4. Move point  $C$  so that when you rotate point  $B$  no triangle is formed. How does  $a$  compare to  $h$ ?
  
5. Make conjectures about how the measures of  $a$ ,  $b$ , and  $h$  can be used to determine the number of triangles possible when given the measures of two sides and a non-included angle.
  - a. One oblique triangle
  
  - b. Two triangles
  
  - c. One right triangle
  
  - d. No triangles