

Teacher Notes



Activity 14

Discovering the Derivative of the Sine and Cosine Functions

Problem

The slope of the tangent to a curve at a point is defined to be the derivative. By calculating the derivative of a curve at many points a new function can be obtained. By finding the equation that will fit the points, the derivative of $f(x) = \sin(x)$ and $g(x) = \cos(x)$ can be discovered.


Exploration

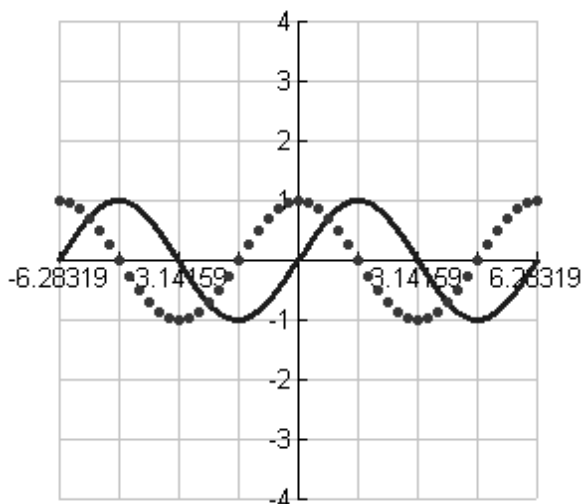
Steps 1 through 10 are details for the students to set up the problem. When students have completed step 10, their graph should look appear as shown.

Objective

- ◆ Students will discover the derivative of $\sin(x)$ and $\cos(x)$ by analyzing a scatterplot of x -values and the function's numerical derivatives at these x -values.

Applicable TI InterActive! Functions

- ◆ Define `variable:= value`
- ◆ Store `{list} → list_name`
- ◆ NDeriv `nDeriv(function, variable)`
- ◆ Graph 



Analysis

1. $y_2(x) = \cos(x)$
2. Yes, y_2 matches y_3 .
4. $f'(x) = \cos(x)$
5. Students answers may vary.
6. The graph of $f(x)$ and the scatterplot of numerical derivatives have changed. Since $y_2 = \cos(x)$, the graph of $f(x)$ is the same as the graph of y_2 .
7. $y_2(x) = -\sin(x)$
8. $f'(x) = -\sin(x)$

Additional Exercises

2. $y_2(x) = 2 \cos(2x)$
3. When $g(x) = \sin(2x)$, $g'(x) = 2 \cos(2x)$.
5. $y_2(x) = 3 \cos(3x)$
6. When $g(x) = \sin(3x)$, $g'(x) = 3\cos(3x)$.
8. $y_2(x) = 5 \cos(5x)$
9. When $g(x) = \sin(5x)$, $g'(x) = 5 \cos(5x)$.
11. $y_2(x) = -2 \sin(2x)$
12. When $g(x) = \cos(2x)$, $g'(x) = -2 \sin(2x)$.
14. $y_2(x) = -3 \sin(3x)$
15. When $g(x) = \cos(3x)$, $g'(x) = -3 \sin(3x)$.
17. $y_2(x) = -5 \sin(5x)$
18. When $g(x) = \cos(5x)$, $g'(x) = -5 \sin(x)$.
19. If $f(x) = \sin(n * x)$, $f'(x) = n \cos(nx)$.
20. If $f(x) = \cos(n * x)$, $f'(x) = -n \sin(nx)$.