Solving Differential Equations Using Euler's Method

by

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Textbook Correlation: Key Topic

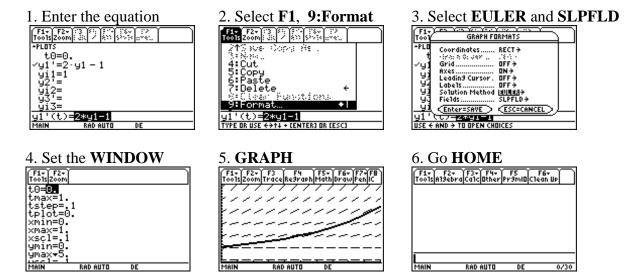
• Differential Equations

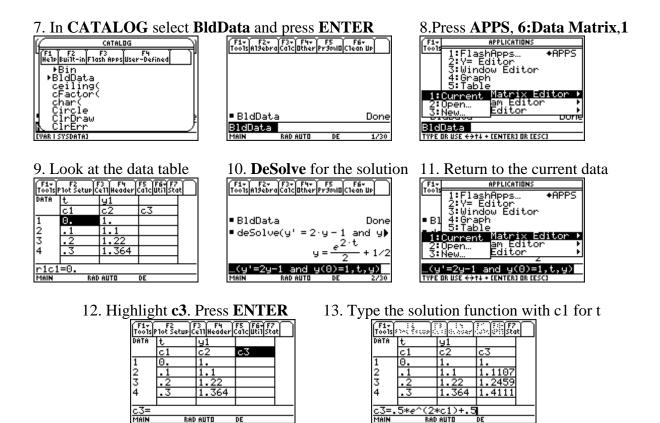
NCTM Principles and Standards:

- Process Standard
 - Representation
 - Connections

Exercises:

Given the initial value problem, $\frac{dy}{dt} = 2y - 1$, y(0) = 1, use Euler's Method to approximate the solution over the interval [0,1] with step size = 0.1.





14. Compare the approximate results using Euler's Method in c2 with the analytical solution function values in c3.

F17 T0015	F1+ F2 ToolsPlot Setup CellHeader CalcutilStat				
DATA	t	y1			
	c1	c2	c3		
5	.4	1.5368	1.6128		
5 6 7	.5	1.7442	1.8591		
7	.6		2.1601		
8	.7	2.2916	2.5276		
8r8c	8 r8c3=2.5275999834224				
MAIN	RAD	AUTO	DE		

RAD AUTO

DE

	Plot Setup C	'3 F4 e11Header(FS F6+F7 CalcutilSta	, T
DATA	t	y1		
	c1	c2	c3	
8	.7	2.2916	2.5276	
9	.8	2.6499	2.9765	
10	.9		3.5248	
11	1.	3.5959	4.1945	
∄r11c3=4.1945280494654				
MAIN	RAD	AUTO	DE	

5*e

RAD AUTO

15. Define scatter plots for c1 vs c2 and c1 vs c3.

/ 	V V	<u> </u>	
	sysdata		<u> </u>
C F1 Define	F2 F3 F4 CopyClear 4)	
1 記録	≤Xx:c1 9:c2 ≤ <u>0x:c1 9:c3</u>		
4 Plot 4:			
1 P1ot 6:			
1 Plots			لر
D F 1100-	4.1240200	7474034	
MAIN	RAD AUTO	DE	

16. Select them in the Y = editor.

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t0=0.			
ÿi1=1 92' =			
<u>yi</u> 2= y2'(t)=			
MAIN	RAD AUTO	DE	

17. GRAPH.

18. Compute the differences.

DATA	y1			
	c2	сЗ	c4	
1	1.	1.	0.	
2 3 4	1.1	1.1107	.0107	
3	1.22	1.2459	.02591	
4	1.364	1.4111	.04706	
c4=c3-c2				
MAIN	RAD	AUTO	DE	