

**Problem 1 – An isosceles triangle**

Triangle  $ABC$  is shown on page 1.3.

- Make a conjecture about the angle measures and the lengths of the opposite sides of an isosceles triangle.
- In an isosceles triangle, when is the measure of the vertex angle *greater than* the measure of either base angle? When is it *less than* the measure of either base angle?

**Problem 2 – Exterior and remote interior angles**

Triangle  $DEF$  is shown on page 2.2.

- How are the largest angle and longest side related?
- How are the smallest angle and smallest side related?

Complete each statement.

- In a triangle, the measure of an exterior angle is *equal to* \_\_\_\_\_.
- $m\angle GEF >$  \_\_\_\_\_
- $m\angle GEF >$  \_\_\_\_\_
- In a triangle, the measure of an exterior angle is *greater than* \_\_\_\_\_.

**Problem 3 – The perpendicular distance**

On page 3.2,  $\overline{PM} \perp \overline{XY}$ .

- Make a conjecture about the lengths of  $\overline{PM}$  and  $\overline{PQ}$ .

# Triangle Inequalities

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Prove the following statement:

*The perpendicular segment from a point to a line is the shortest segment from the point to the line.*

Given:  $\overline{PM} \perp \overline{XY}$

Prove:  $\overline{PQ} > \overline{PM}$

Statements	Reasons

**Challenge:** Prove the same statement using a different approach.

Given:  $\overline{PM} \perp \overline{XY}$

Prove:  $\overline{PQ} > \overline{PM}$

Statements	Reasons