## Growing Interest




TI-Nspire CAS


Investigation


Student

To compare the different growth patterns for a sum of money invested under a simple interest plan and a compound interest plan.

## Equipment

For this activity you will need:

- TI-Nspire CAS (or TI-Nspire)


## Problem Description

Daisy is a hard-working maths student who was the lucky winner of a scholarship lump sum payment of \$2000. She was absolutely delighted but she did not need to use the money straight away. She decided to put it into an investment account so that she could withdraw it at a later time to help her with her studies. When she went to her bank, Daisy saw that there were two different investment options available:
a) Simple interest paid at $5 \%$ p.a.
b) Compound interest at 4\% p.a.

## INVESTMENT ACCOUNT

$5 \%$ per annum
(simple interest paid annually)

INVESTMENT ACCOUNT
4\% per annum
(compound interest paid annually)

Which investment option should Daisy choose?
An accurate answer to this question is not necessary. The idea is to encourage students to consider the options. An intuitive response is satisfactory at this stage.

Are there any other factors that could affect her decision?
Students may offer a variety of factors that are not necessarily mathematical. These could include accessibility to the bank, fees that may apply to early withdrawal from the investment plan, etc. You may use this question to stimulate discussion that explores what students might already know about banks and investment opportunities.

## Essential Understanding

It is essential for this investigation to understand that simple interest and compound interest are two different ways that interest can be calculated and paid into an investment account. This investigation will help you understand that compound interest is repeated applications of simple interest.

Simple Interest is when an interest amount is calculated on the principal and then that fixed amount is paid into the investment account at the end of each investment period.

Compound Interest is when the first interest payment is made into an account and the new account balance is then used to calculate the interest that is due for the next investment period and so on. Because the account balance grows after each interest payment, each subsequent interest payment also increases.

## Technology

Calculating the interest amount for the first year

Open a new Calculator page. Determine how much interest would be paid for the first year by each of the two investment plans. Remember that 'percent' means 'per hundred'. A good way to do this is to input 2000 and then use the fraction template to multiply it by the percentage over 100.


## Simple Interest

First, we need build a spreadsheet that shows how the investment account balance grows under the simple interest plan.

Step 1. Open a new Lists \& Spreadsheet page.

Step 2. Input column headings of year, startbalsimp, intsimp, and endbalsimp.

Step 3. In the year column input the data: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10.

Step 4. In the intsimp column enter the value $\mathbf{1 0 0}$ into each of the first ten cells of that column.(Note: the 100 is the amount of simple interest that will be paid into the account each year, as determined on the calculator page in the previous section.

Step 5. In cell B1 input 2000.

Step 6. In cell D1 input =b1+c1.


Step 7. Press enter and the formula will convert to 2100, which is the balance at the end of the first year.


Step 8. Move to cell B2 and input =d1.
(Note that the spreadsheet will insert the value $\mathbf{2 1 0 0}$ into cells D1 and B2.)


Step 9. We now want to do a relative copy of the formulas in cells D1 and B2 to the other cells of those columns. There are several ways in which this can be done. If you are unsure how to do this, then you may wish to perform the following steps:
a. Use the arrow keys to highlight cell B2.
b. Press and hold the mouse key until a broken dashed line indicates that the cell has been selected.

c. Use the down arrow key to 'stretch' the selected area downwards until you get to row 10.

d. Press enter. (Note: No values will be displayed yet as the startbal for each year needs the figures of the endbal from the previous year, which are yet to be calculated).

e. Move the cursor to cell D1.


Step 10. Perform the following steps to set up the endbal formula in column $\mathbf{D}$ :
a. Use the arrow keys to highlight cell D1.
b. Press and hold the mouse until a dashed line indicates that the cell has been selected.
c. Use the down arrow to 'stretch' the selected area downwards until you get to row 10.
d. Press enter. (Note that all the values for both columns $\mathbf{B}$ and $\mathbf{D}$ will now be displayed.

| 1.1 | 1.2 |  | saved $\nabla$ | ¢1] |
| :---: | :---: | :---: | :---: | :---: |
| year |  | ${ }^{\text {B }}$ startba... ${ }^{\text {C }}$ intsimp |  | $\square_{\text {Dendbal... }}{ }^{\boldsymbol{\Lambda}}$ |
| - |  |  |  |  |
|  |  | 2400 | 100 | 200 |
| 6 | 6 | 2500 | 100 | 2600 |
| 7 | 7 | 2600 | 100 | 2700 |
| 8 | 8 | 2700 | 100 | 2800 |
| 9 | 9 | 2800 | 100 | 2900 |
| 10 | 10 | 2900 | 100 | 3000 |
| D1 | $=b 1+c 1$ |  |  | 4 |

Question: By referring to the spreadsheet, what amount will Daisy's $\$ 2000$ investment have grown to after 10 years?

Daisy's investment will have grown to $\$ 3000$ in 10 years.

Step 11. Open a Data \& Statistics page. Set year as the independent variable (horizontal axis) and endbalsimp as the dependent variable (vertical axis).

Question: How would you describe the shape of the scatterplot?
The shape of the scatterplot is linear.


## Compound Interest

Now let's build a spreadsheet that shows how the investment account balance will grow under the compound interest plan.

Step 1. Open a new Lists \& Spreadsheet page.

Step 2. Set the column headings as year, startbalcomp, intcomp, and endbalcomp.

Step 3. In the year column, the previous data 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 will be displayed. If not, input these values again.

Step 4. In cell B1 input 2000.

Step 5. In cell C1 input $=\mathbf{b} \mathbf{1} \times \mathbf{0} \mathbf{0 4}$.

Step 6. In cell D1 enter =b1+c1.


Step 7. In cell B2 input =d1.

Step 8. In cell $\mathbf{C} 2$ input $=\mathbf{b} \mathbf{2} \times \mathbf{0} \mathbf{0 4}$.

Step 9. In cell D2 input =b2+c2.


Step 10. Perform the following steps to relatively copy the row two formulas:
a. Use the arrow keys to move to cell B2. Press and hold the mouse key and then press the right arrow to move across to column D.
b. Press and hold the mouse key until a broken dashed line indicates that the three cells have been selected.

c. Use the down arrow to 'stretch' the selected area downwards until you get to row 10.
d. Press enter. (Note that all the values for columns B, C and $\mathbf{D}$ will now be displayed.


Question: By referring to the spreadsheet, what amount will Daisy's \$2000 investment have grown to after 10 years?

Daisy's investment will have grown to $\$ 2960.49$ in 10 years.
Question: Over a ten year period, which investment option has been better?
Option 1 using simple interest is the best investment over a ten year period.
Step 11. Open a Data \& Statistics page. Set year as the independent variable (horizontal axis) and endbalcomp as the dependent variable (vertical axis).

Question: How would you describe the shape of the scatterplot?
The shape of the scatterplot is almost linear but it has a slight upward curve.


## Examining the investment over the longer term

Will your answer to the question in the last section always be the case? Let us now consider what happens over a longer time period.

Step 1. Open a Graphs page.

Step 2. Press menu > Window/Zoom $>$ Window Settings.
Set a domain of $\mathbf{- 2 \leq x \leq 1 5}$ and a range of $1400 \leq y \leq 4000$.

Step 3. Input $\mathbf{f 1}(\mathbf{x})=\mathbf{2 0 0 0} \mathbf{+ 1 0 0 x}$ to show the growth of the account balance under the simple interest plan.

Step 4. Input $\mathbf{f} \mathbf{2}(\mathbf{x})=\mathbf{2 0 0 0}(\mathbf{1 . 0 4})^{\mathbf{x}}$ to show the growth of the account balance under the compound interest plan.

Step 5. Notice that both the $\mathbf{f 1}(\mathbf{x})$ and $\mathbf{f} \mathbf{2}(\mathbf{x})$ investment graphs start at the same point on the $y$-axis ( $\$ 2000$ ). Initially, the simple interest line grows at a faster rate but eventually the compound interest curve crosses the line and grows at a faster rate.

Step 6. Press menu > Analyse Graph > Intersection and click on either side of the point to determine the coordinates of the point of intersection.

Question: What do the $x$ and $y$-values of these coordinates mean?

The $x$-value represents the number of years. The $y$-value represents the amount that the investment has grown to.


## Conclusion

Look again at the original questions posed in the Problem Description.
Question Which investment option should Daisy choose?
If Daisy is going to invest her money for less than 11.9 years, she should choose the first option using simple interest.

If Daisy is going to invest her money for more than 11.9 years, she should choose the second option using compound interest.

Question Are there any other factors that could affect her decision?
Interest rates vary over the years. If interest rates are high, Daisy should try for a fixed term rate. If interest rates are low, she should not select a fixed term rate in case interest rates rise.

To further extend this investigation, you may wish to:
a. Fill down your spreadsheet formulas to compute values for a longer time period.
b. Experiment by amending the formulas to show different interest rates.

## The Finance Solver

Another feature of TI-Nspire CAS that is useful for quickly seeing the effect of changing different compound interest variables (such as the interest rate) is the Finance Solver. To access it, open a Calculator page and press menu $>$ Finance $>$ Finance Solver.


Finance Solver info stored into tvm.n. tvm.i, tvm.pv, tvm.pmt.

