The Movie Contract

Student Worksheet

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Introduction

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Stella Rosengren is one of the hottest movie stars of the century. One major studio, 21st Century Dingo, was so anxious to get her to sign a film contract with them that they offered her a choice of three salary options. This exploration examines the effects of the different payment options on her final payment for the film.

Part 1: Payment schemes

Stella is offered three payment schemes for working on this movie.

- Scheme A: A flat rate of \$100 000 per day for as many days as the movie is being shot. That is, \$100 000 for a one-day contract, \$200 000 for a two-day contract, and so on.
- *Scheme B*: \$20 for the first day of work, but overall earnings double for each additional day of full work. That is, \$20 for a one-day contract, \$40 for a two-day contract, and so on.
- *Scheme C*: Two cents for the first day of work, but overall earnings triple for each additional day of work. That is, \$0.02 for a one-day contract, \$0.06 for a two-day contract, and so on.

Stella, although a brilliant actor and mathematician in her own right, prefers to leave financial matters to you, her agent. Your job is to give her advice about which offer to accept. First you will need to know how Stella's earnings under each of the schemes depend on number of days (*x*) Stella works.

Begin by examining the value of scheme A.

Question 1.

Copy and complete the following information to devise a rule for Stella's overall earnings under Scheme A [EA(x)] within the first week of work (7 days).

 $EA(1) = 100\ 000 \times 1 = \$\ 100\ 000$ $EA(2) = 100\ 000 \times __= ___$ $EA(3) = 100\ 000 \times __= ___$ $EA(4) = 100\ 000 \times __= __$ $EA(5) = 100\ 000 \times __= __$ $EA(6) = 100\ 000 \times __= __$ $EA(7) = 100\ 000 \times __= __$

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Question 2.

How much would Stella earn if she worked for 10 days using scheme A?

Question 3.

Explain why the rule for Stella's overall earnings using Scheme A after x days is EA(x) = 100000x.

Question 4.

Scheme A is an example of a linear relationship. What does this mean?

Now look at scheme B, in which the amount earned by Stella doubles each day.

Question 5.

Copy and complete the following information to devise a rule for Stella's overall earnings under scheme B [EB(x)] within the first week of work (7 days)

Question 6.

How much would Stella earn if she worked for 10 days using scheme B?

Question 7.

Use the above information to find a rule for calculating Stella's overall earnings *EB(x)* using scheme B after *x* days.



Using a similar method, we will devise a rule for Stella's overall earnings under scheme C [EC(x)], in which the amount earnt triples each day.

Question 8.

Copy and complete the following information to devise a rule for Stella's overall earnings under scheme C [EC(x)] within the first week of work (7 days).

Question 9.

How much would Stella earn if she worked for 10 days using scheme C?

Question 10.

Use the above information to find a rule for calculating Stella's overall earnings *EC(x)* using scheme C after *x* days.

Question 11.

Schemes B and C are examples of exponential relationships. What does this mean?



Part 2: Comparing the schemes numerically

The producer at 21st Century Dingo estimates that shooting the movie will take between 14 and 18 days. The TI-Nspire CAS can be used to help compare the value of each of the schemes in 2 weeks of shooting.

On the TI-Nspire CAS

- Press **HOME-1** to create a new document, and then press **1** to add a **Calculator** page
- Press MENU-1 and then press 1 to select Define and then type the following to complete the rule: Define ea(x) = 100000x
- To use the rule to calculate the amount earned under scheme A after two days, type **ea(2)**
- To use the rule to calculate the amount earned under scheme A after each day in the first week, type ea({1,2,3,4,5,6,7})

Question 12.

Use your TI-Nspire CAS and the procedure outlined above to define a rule for the earnings under scheme B and scheme C. (Define rules for **eb(x)** and **ec(x)**.)

eb(x) = _____ ec(x) = _____

Question 13.

Check your answers by using your rules to calculate the amount earned under scheme A, B and C for each day in the first week of shooting. (i.e. check the calculator amounts with those found previously in your answers to question 5 and 8).

Question 14.

Complete the following calculations to find which scheme would earn Stella the most money if shooting lasted 14 days.

- a) *EA*(14) =
- b) *EB*(14) =
- c) *EC*(14) =

Question 15.

If the shooting lasts 14 days, Stella can earn most money by choosing which scheme?

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Define $ea(x) =$	100000 <i>·x</i>	Done					
ea(2)		200000					
ea({1,2,3,4,5,6,7}) {100000,200000,300000,400000,500000,60*							
		\sim					

To explore and compare the value of each scheme over the days of shooting, you can use the table feature. To do this on the TI-Nspire CAS

- Press HOME and add a Lists and Spreadsheet page.
- Press MENU-5 to select Table, and then press 1 to select Switch to Table.
- Click at the top of the first column and select **ea** to make a table of the values of *ea*(*x*) for various *x* values.
- Click at the top of the next column, and select **eb** to make a table of the values of *eb(x)* for various *x* values.
- Tab right to move to the next column, and select **ec** to make a table of the values of *ec(x)* for various *x* values.

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Х	ea(x):= ▼	eb(x):= ▼	ec(x):= ▼	
	100000*x	20*2^(x	0.02*3^(x.	
1.	100000.	20.	0.02	
2.	200000.	40.	0.06	
3.	300000.	80.	0.18	
4.	400000.	160.	0.54	
5.	500000.	320.	1.62	
0.	02			•

Question 16.

Scroll down through the table to 10 days. The table shows that under scheme A, Stella would earn '1.E6' dollars. What does this mean?

Question 17.

Use your table to answer the following questions for 14 to 18 days of shooting.

- a) For which number of days is scheme A the most lucrative?
- b) For which number of days is scheme B the most lucrative?
- c) For which number of days is scheme C the most lucrative?

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Part 3: Comparing the schemes graphically

Now we will compare the earnings using graphs.

To do this using the TI-Nspire CAS

- Press **HOME** and add a **Graphs** page.
- Enter the rule for each scheme as follows (note that CTRL-G toggles between showing and hiding the rules) f1(x) = ea(x)
 - f2(x) = eb(x)
 - f3(x) = ec(x)
- The graph screen should appear as at right, using the standard window [-10,10] by [-6.67,6.67].

Question 18.

Is this a suitable window in which to view the graphs? Explain why/why not.



Question 19.

Using the information found earlier, identify suitable minimum and maximum values (rounded) for the number of days (x) and the earnings (y) for between 14 and 18 days.

- a) XMin =
- b) XMax =
- c) YMin =
- d) YMax =

Question 20.

Use your answer to the previous question to change the viewing window. [To modify the window settings, press **MENU-4** to select **Window/Zoom** and then **1** to select **Window Settings**].

Question 21.

Once you have located the graphs in a suitable viewing window to view earnings between 14 and 18 days, draw a sketch of the three graphs. Label each graph clearly, and the window boundaries.



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Question 22.

Compare the graphs for the earnings under each scheme. How does each graph explain how the earnings for each scheme change over the course of the 18 days?

- a) Graph of scheme A
- b) Graph of scheme B
- c) Graph of scheme C

Things go terribly wrong! As a result of a freak storm, shooting of the movie is delayed and Stella ends up working for a total of 23 days. In a moment of weakness (and clearly without checking!), the producer agrees to pay Stella under the terms of the original contract. This proves to be quite lucrative for Stella.

Question 23.

Explain why this turn of events favours Stella if she chose scheme C. How much money will she earn in this case?

Question 24.

Explain what you have learnt from this task about the behaviour of exponential functions.

