## Extending the Trigonometric Ratios

## Concepts

- Trigonometric ratio


## Materials

- TI-Nspire
- TI-Nspire document


## Objectives

- Students will use a rotating ray in a coordinate plane to define angles measuring greater than $90^{\circ}$ and less than $360^{\circ}$.
- Students will define sine, cosine, and tangent for angles of any size.

1. Download the TI-Nspire document called ExtendingTrigRatios to your handheld. Use TI-Nspire computer link. (Fig 1)
2. Open the document in your handheld. Press Home, 7:MyDocuments, select the document ExtendingTrigRatios using the NavPad (arrows), hit enter.(Figs 2-4)


Fig 1


Fig2


| 1.1 | 1.2 | 1.3 | 1.4 | DEG AUTO REAL |
| :--- | :--- | :--- | :--- | :--- |

Extending
The Trigonometric Ratios
| by
Miriam Santana

Measuring angles greater than $90^{\circ}$

1. Go to page 1.2 Press ctrl and > (right arrow key). You will see the objectives of this lesson.
2. Skip page 1.3 Go to page 1.4 by pressing ctrl and right arrow key.
3. In page 1.4 there are 3 windows. You can move between windows by pressing ctrl tab. Fig 6
4. Explore how to measure angles greater than $90^{\circ}$. Measure $\angle A B C$. Drag point $C$ and measure the angle in the different quadrants.

- Drag point C. Use the NavPad to put the cursor on top of point C. To hold the point press ctrl click. Now move the point
- Observe how the measurement of the angle changes.
- Is the angle always positive?
- How do you think an angle of rotation could have a negative measure? Answer in your handheld. (Fig 7)


Fig 5


## Question

How do you think an angle of rotation could have a negative measure?

## Extending Sine and Cosine

1. Go to problem 2. Page 2.3 Press ctrl right arrow key (NavPad).
Now we will drag point $P$ and measure the sine and cosine for the angles between O and 360 degrees.

- Make sure that in your spreadsheet screen you can see columns E, F and G.
- Grab point P and each time you want to capture a set of data press Ctrl + .( Figs 8 and9)

2. Go to pages 2.4 and 2.5 and observe how these points are plotted.
In page 2.4 you will see sine in function of the angle.
In page 2.5 you will see cosine in function of the angle
Go back to page 2.3 to capture more points that will allow you to have a better graph.
3. Now, observe your graphs and answer the questions.

- What is the maximum value?
- What is the minimum value?
- Where is the graph zero? (fig 10)


For each set of data you wish to capture
press Ctrl +.
Fig 8


For each set of data you wish to capture press Ctrl + .

Fig9

Fig 10
4. To get a better look of your graph.

- Go to your graphing window. Press ctrl tab.
- Press menu, 2:View,6:Show Entry Line, write sin(x) Fig 11
- Press Menu, 5:Trace,1:Graph trace and find the max, min and zero of your graph.

5. Repeat steps 8 and 9 for Cosine graph.
6. Go to page 2.6 and complete the table. (Fig 12)


Fig 12

## Graphing Tangent from a Right Triangle

1. Go to page 3.2 and drag point $A$ towards point C. Each time that you want to capture angle $\alpha$ and $\operatorname{Tan} \alpha$ press ctrl + . (Figures 13-14)

2. All the values of $\alpha$ and $\operatorname{Tan} \alpha$ are capture in the spreadsheet of page 3.3 Fig 15

|  | 3.13 .2 | 3.3 3.4 | DEG AUTO REAL |  |  | ${ }^{\text {Ps }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A ang... | B tan... | C | D | E | F |
| - | = capture | =capture |  |  |  |  |
| 8 | 8.842 | . 156 |  |  |  |  |
| 9 | 11.310 | . 200 |  |  |  |  |
| 10 | 13.134 | . 233 |  |  |  |  |
| 11 | 15.642 | . 280 |  |  |  |  |
| 12 | 19.290 | . 350 |  |  |  | $\checkmark$ |

A8 | $=8.8418145602$
Fig 15
3. Go to page 3.4 and observe the graph of Tan $\alpha$ (Fig 16)
4. Answer the questions:

- What is the domain of the function? Why?
- Does the function have a maximum value? Why?

5. To get a better look of your graph.

- Go to your graphing window. Press ctrl tab.
- Press menu, 2:View,6:Show Entry Line, write $\tan (x)$
- Press Menu, 5:Trace,1:Graph trace and find the max, min and zero of your graph. (Fig 17)

6. Discuss your answers and findings with the rest of the class.

