## Fencing the Dog Yard

TI-Nspire Investigation from MathBits.com
Name


Directions: Grab your TI-Nspire and read carefully!

1. Get the dogyard.tns file loaded onto your TI-Nspire.

Open the document dogyard.tns
created by: Donna Roberts
MathBits.com
2. On page 1.3 you will see a rectangle with a fixed perimeter of 20 cm , which will simulate your paper clip fencing.

Grab and drag the lower right vertex (the point) of the rectangle and observe the changes in the length, width, area and perimeter.

Pay particular attention to the changes in the area and the shape of the rectangle.


Obsrevation: What appears to be happening to the area of the rectangle as the vertex is moved?
3. You are now ready to start collecting data from the moveable rectangle to further investigate this situation. From your rectangle, on page 1.3, you will now collect data that will be placed in the spreadsheet on page 1.5.

By moving the lower right vertex, place the rectangle in a variety of shapes, and press "CTRL, period" after each shape to collect the data. Have a minimum of 10 data collections.

The length, width and area of each of your chosen rectangles will appear in their respective columns in the spreadsheet.

4. On page 1.7, you will create a scatter plot to graph your data.

For a scatter plot, choose Menu, \#3 Graph Type and \#4 Scatter Plot.

| Scatter Plo. |  |  |
| :---: | :---: | :---: |
| 5. Hit Var: Choose the $x$-axis to be len. | 41.6 1.7 1.8 , *dog | rd $\geqslant$ 國 |
| Hit Var: Choose the $y$-axis to be area1. Hit Menu - 4-9 for Zoom Data. | 6.67 <br> 1 | $x$ |
|  |  | $-\hat{10}$ |

Observation: Does the graph support your thoughts about what was happening with the area? Do you think there will be a maximum area for this problem? Explain.
6. It is time to look at the statistics for this data and obtain a representative model equation (a regression equation). Is this the "name" you chose for your paper clip graph?

Return to page 1.5.
Click a cell in Column E.
Choose Menu \#4 Statistics, \#1 Stat Calculations, \#6
Quadratic Regression
Choose X List = len
Y List = area1
Save to..... f1
7. Return to the graph, page 1.7.

## Choose Menu \#3 Graph Type, \#1 Function

Arrow up to $f 1(x)$ if it is not visible.
Hit ENTER. You will see the graph on top of the scatter plots. You may need to adjust the window.

8. Now, let's find that maximum area.

Choose Menu \#6 Analyze Graph - \#3 Maximum. Move the hand until the Maximum appears.

You answer will not, necessarily, be the same as the one shown at the right.


Observation: To the nearest tenth, that is the maximum possible area of your dog yard?

What are the dimensions that create this dog yard? State both length and width.

Conclusion: Would the dog yard of maximum area be the BEST shape for the dog yard? Explain your answer, listing factors that would affect your decision.

Comparison: When you built the dog yard with the paper clips, you used only integer values for the lengths of the sides of the pen. At the bottom of your table (chart) for that activity, you represented the length, width and area in terms of $x$. Plot the area you listed in that table onto page 1.7 along with your other graph.

How does that initial equation compare with the quadratic regression equation?

Explain why you did not get the "exact" (best fit) equation using the paper clips.


