

## Ballooning inside the box



## Activity Overview:

Using the USA TODAY Infograph, "Ballooning inside the box," you will explore the geometric relationships using similar triangles. You will use triangles with two pairs of congruent angles to explore similarity properties of the triangles. You will explore what happens to the ratios of corresponding sides of a variety of similar triangles. Finally, the relationships found will be applied to determine the height of a hot-air balloon indirectly.


## Focus Questions:

Q. Maggie places a mirror on the ground 40.5 feet from the base of the basket. She walks backwards until she can see the top of the balloon in the middle of the mirror. At that point, Maggie's eyes are 5 feet off the ground and she is 2 feet from the mirror. What is the height of the balloon that Maggie is watching?
Q. A balloon is anchored to the ground at the beginning of a race with a cable. The cable forms a perpendicular line from the basket to the ground. Maggie places a mirror on the ground 150 feet from the perpendicular line and walks backward until she can see the bottom of the basket in the mirror. Her eyes are 5 feet off the ground and she is 8 feet from the mirror. What is the altitude of the bottom of the basket?
Q. Maggie is watching a balloon coming down. The balloon drops a 50 foot rope that forms a perpendicular with the ground. She is 6 feet from her mirror and looking at the bottom of the balloon in the mirror. She is kneeling and her eye level is 3 feet from the ground. How far is the mirror from the perpendicular line formed between the rope and ground?


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## Procedure:

Activity 1: You will explore geometric relationships with similar triangles. Complete Activity 1 before answering the Focus Questions.

Step 1. Press and select Cabri Jr. and press $\subseteq$.

Step 2. Press $\perp(\mathrm{Y}=$ button), select Open... , and press $\subseteq$. Highlight SIMILAR and press $\subseteq$. Look at the two triangles ABC and DEF, what conclusion can you make about them? $\qquad$

Step 3. Press $\beta$, choose Calculate, and press $\subseteq$. Determine the three ratios in the lower right corner of the screen. Move the pointer to the measure of AC and press $\subseteq$. Move the pointer to the measure of DF, press $\infty$ and $\subseteq$ to calculate the ratio for AC:DF. Move this value to AC:DF on the screen and press $\subseteq$. Repeat this procedure for the other ratios and press when finished. What can you conclude about these ratios? $\qquad$
$\qquad$

Step 4. Move the pointer to $C$ and press. Grab and move $C$ to change the measures for angles A and B. Press $\subseteq$. Repeat the same procedure for $F$. Remember to keep the corresponding angle measures the same.

Step 5. After you have made a number of these changes, what can you conclude about the ratios? $\qquad$

Step 6. Complete the following:

- If two angles of one triangle are congruent to two angles of another triangle, then the triangles are $\qquad$ .
- In similar figures, ratios of corresponding sides are $\qquad$ .


## Data Source:

FireFly Balloons; howstuffworks.com; Albuquerque International Balloon Fiesta

## Materials:

- TI-83 Plus family or TI-84 Plus family
- Cabri ${ }^{\text {Tw }}$ Jr. Application


## Additional Information:



## Ballooning inside the box

## Procedure:

Activity 2: Use the information from Activity 1 and the USA TODAY Infograph "Ballooning inside the box" to answer the Focus Questions.

Step 1. Maggie places a mirror on the ground 40.5 feet from the base of the basket. She walks backwards until she can see the top of the balloon in the middle of the mirror. At that point, Maggie's eyes are 5 feet off the ground and she is 2 feet from the mirror. What is the height of the balloon that Maggie is watching?

Step 2. A balloon is anchored to the ground at the beginning of a race with a cable. The cable forms a perpendicular line from the basket to the ground. Maggie places a mirror on the ground 150 feet from the perpendicular line and walks backward until she can see the bottom of the basket in the mirror. Her eyes are 5 feet off the ground and she is 8 feet from the mirror. What is the altitude of the bottom of the basket? $\qquad$

Step 3. Maggie is watching a balloon coming down. The balloon drops a 50 foot rope that forms a perpendicular with the ground. She is 6 feet from her mirror and looking at the bottom of the balloon in the mirror. She is kneeling and her eye level is 3 feet from the ground. How far is the mirror from the perpendicular line formed between the rope and ground? $\qquad$

