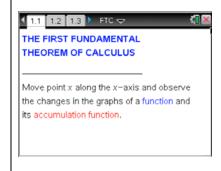


The First Fundamental Theorem of Calculus Student Activity

Name _____

Open the TI-Nspire document FTC.tns.

The accumulation function, A(x), measures the definite integral of a function f from a fixed point a to a variable point x. In this activity, you will explore the relationship between a function, its accumulation function, and the derivative of the accumulation function. These observations will help you better understand the first Fundamental Theorem of Calculus.



Move to page 1.2.

Press ctrl ▶ and ctrl ◀ to navigate through the lesson.

1. The graph shown is of the function y = f(x). The **accumulation function** of f(t) from a to x is given by $A(x) = \int_a^x f(x) dx$. The accumulation function measures the definite integral of f from a to x. For example, if you set a to -3, $A(2) = \int_{-3}^2 f(x) dx$, you get the value of the definite integral of f from -3 to 2.

Drag the point *x* along the *x*-axis to determine the values of the accumulation functions below:

a.
$$A(3) = \int_{-3}^{3} f(x) dx =$$

b.
$$A(0) = \int_{-3}^{0} f(x) dx =$$

Move to page 1.3.

- 2. The top graph shows the original function, y = f(x), and the shaded region between the graph of the function and the *x*-axis as the point *x* is dragged along the *x*-axis. The bottom graph shows the value of the definite integral for each upper limit *x*, with lower limit a = -3. Drag point *x* along the *x*-axis in the top graph to observe the relationship between the two graphs.
 - a. At what value(s) of x does the accumulation function, A(x), have a local maximum? A local minimum? Explain how you know.
 - b. Drag point x to the x-value at which A(x) has a local maximum. What do you notice about the value of the original function, f(x), at that point?



The First Fundamental Theorem of Calculus Student Activity

- c. Drag point x to the x-value at which A(x) has a local minimum. What do you notice about the value of the original function, f(x), at that point?
- d. At what value of x does the accumulation function, A(x), have an inflection point? Explain how you know.
- e. Drag point x to the inflection point of A(x). What do you observe about the original function, f(x), at that point?
- 3. a. Over what interval(s) is A(x) increasing? Decreasing?
 - b. What do you observe about f(x) over the interval(s) where A(x) is increasing? Over the interval(s) where A(x) is decreasing?
- 4. Based on your observations in questions 2 and 3, what do you believe the relationship between the functions f(x) and A(x) to be? Explain your reasoning.

Move to page 1.4.

- 5. The top graph on page 1.4 is the graph of the accumulation function, A(x), for the function f(x) from previous pages.
 - a. Drag point *x* and observe the changes in both graphs. What is the graph on the bottom of the page measuring? How do you know?
 - b. What is the relationship between the bottom graph on page 1.4 and the original function, f(x)?
 - c. Based on your observations, what is the relationship between the functions f(x) and A(x)? How do you know? How does this compare to your answer to question 4?
- 6. Complete the following: $\frac{d}{dx}A(x) = \frac{d}{dx}\int_a^x f(t)dt =$ _____. Explain your reasoning.