

MATHEMATICAL METHODS CAS
UNIT ONE

POLYNOMIALS

Earlier we saw that you could build up complex polynomials from a series of simpler polynomials.

A real polynomial is of the form:

$$P(x) = a_0 + a_1x + a_2x^2 + \dots + a_nx^n,$$

where each power is a positive integer ($n \in J^+$) and the degree of the polynomial is the highest power of the polynomial.

The first degree polynomial is called a linear function.

The second degree polynomial is called a quadratic function.

The third degree polynomial is called a cubic function.

The fourth degree polynomial is called a quartic function.

Exercise One:

Let $f(x) = 3x^2 - 4x - 5$ and $g(x) = x^3 - 6x^2 + 8x + 2$. Find the rules for the following polynomials.

(i) $-f(x)$ and $-g(x)$

(ii) $2f(x)$

(iii) $-3g(x)$

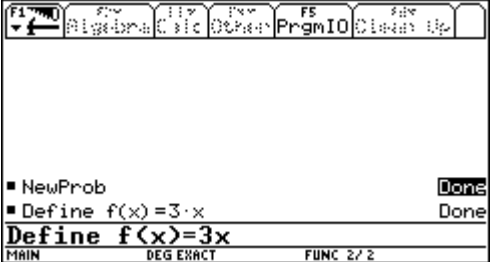
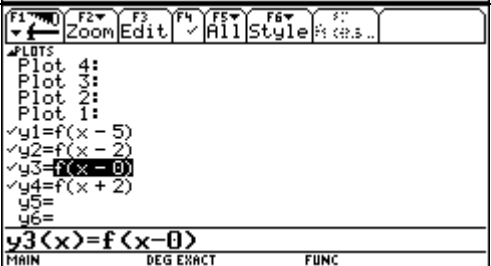
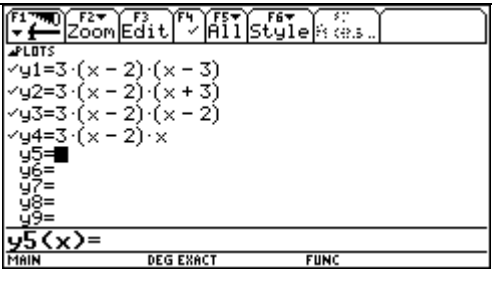
(iv) $f(x) + 2g(x)$

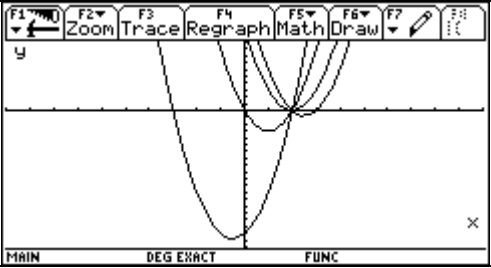
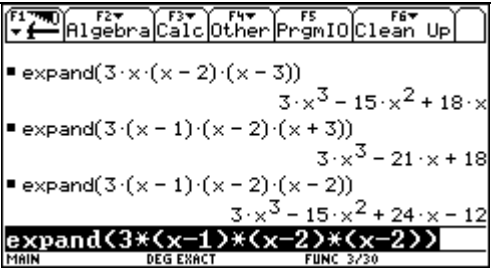
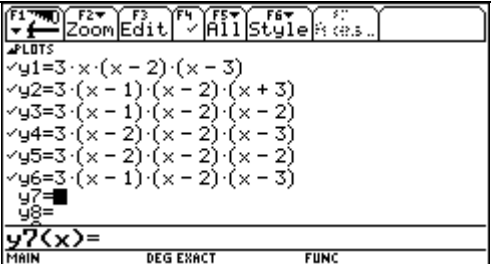
GRAPHS OF POLYNOMIALS

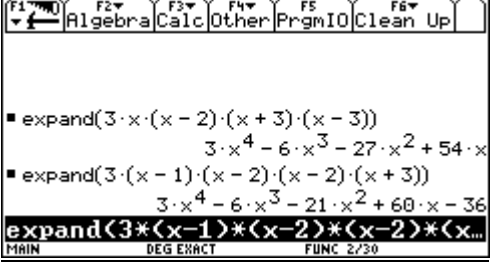
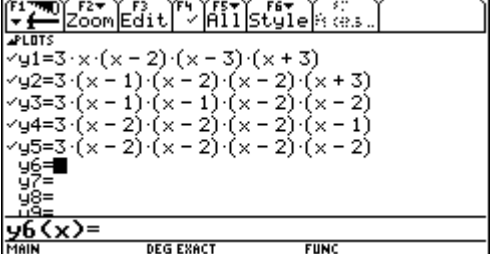
When using the CAS calculator, it is important to include all the key features on the graph. These include:

- (i) the axes labelled.
- (ii) x and y intercepts.
- (iii) turning points or points of inflexion.
- (iv) points of intersection.
- (v) if the graph cuts the x axis once then a second reference point is necessary.
- (vi) asymptotes. (not necessary for polynomials)

Investigating polynomial graphs

<p>On Home screen, NewProb F6 2 Define $f(x) = 3x$</p>	
<p>Sketch the following functions. $f(x-5)$, $f(x-2)$, $f(x-0)$, $f(x+2)$</p>	
<p>What are the zeros of these graphs???</p> <p>What is the relationship between the zeros and the graphs of the function?</p>	
<p>Consider the following quadratic polynomial. What is the degree of these polynomials?</p> <p>Graph the equations as shown in the screen dump on the right.</p>	

<p>You will need to change the window to see all the important feature so the graph.</p>	
<p>What are the zeros of these graphs???</p> <p>What is the relationship between the zeros and the graphs of the function?</p>	<p><i>In your binder book you are to sketch the graphs of each polynomial on a separate set of axes. Label the intercepts with the axes ONLY.</i></p>
<p>Consider the following cubic functions.</p> <p>Using the Expand key to expand the following.</p> <p>$Y = 3x(x - 1)(x - 3)$ $Y = 3(x - 1)(x - 2)(x + 3)$ $Y = 3(x - 1)(x - 2)(x - 2)$ $Y = 3(x - 2)(x - 2)(x - 3)$ $Y = 3(x - 2)(x - 2)(x - 2)$ $Y = 3(x - 1)(x - 2)(x - 3)$</p>	
<p>What is the degree of these polynomials?</p> <p>Graph the equations as shown in the screen dump on the right.</p>	
<p>Graph each equation one at a time.</p> <p>You will need to investigate the number of times the graph cuts the x axes.</p> <p>Consider the zeros and the graphs of the functions. What is the relationship between the two?</p>	<p><u>NOTE YOUR FINDINGS</u></p> <p><i>In your binder book you are to sketch the graphs of each polynomial on a separate set of axes. Label the intercepts with the axes ONLY.</i></p>

<p>Consider the following quartic functions.</p> <p>Using the Expand key to expand the following.</p> <p>$Y = 3x(x - 2)(x - 3)(x + 3)$ $Y = 3(x - 1)(x - 2)(x - 2)(x + 3)$ $Y = 3(x - 1)(x - 1)(x - 2)(x - 2)$ $Y = 3(x - 2)(x - 2)(x - 2)(x - 1)$ $Y = 3(x - 2)(x - 2)(x - 2)(x - 2)$</p> <p>What is the degree of these polynomials?</p>	
<p>Graph the equations as shown in the screen dump on the right.</p>	
<p>Graph each equation one at a time.</p> <p>You will need to investigate the number of times the graph cuts the x axes.</p> <p>Consider the zeros and the graphs of the functions. What is the relationship between the two?</p>	<p><u>NOTE YOUR FINDINGS</u></p> <p><i>In your binder book you are to sketch the graphs of each polynomial on a separate set of axes. Label the intercepts with the axes ONLY.</i></p> <p><u>What have you found out???</u></p>