## The Binomial Distribution Using the TI-89

By

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# **Textbook Correlation: Key Topic**

- Binomial Distribution
- Probability Distribution
- Histogram

## **NCTM Principles and Standards:**

- Process Standard
  - Representation
  - Connections
  - Problem Solving

## Description

The purpose of this activity is to apply the binomial probability distribution function, the binomial cumulative density function, and a histogram to analyze the probability of an outcome.

A True – False test has ten items. Count the number X of correct answers. There are n = 10 observations. Successive outcomes are independent. Each answer falls into one of only two categories, success or failure. The probability of a success (a correct answer) is p = 0.5 for each question.

## a) What is the probability of answering correctly exactly 4 questions?

## Solution:

Method I.

Place the cursor in the entry line on the **HOME** screen. Select the binomial probability distribution function, "**binomPdf**" from **CATALOG**, **F3** Flash Apps. Press enter to paste the command on the entry line of the **HOME** screen. Complete the command by entering **10**, **.5**, **4**) for n, p and X respectively and the right parenthesis key.



The answer is .205078 or approximately 20.5%.

Method II.

If we want to **obtain the list for all eleven outcomes**, we can type the command in the list editor as illustrated below. Enter all the possible outcomes in **list1**. Highlight **list2**, paste the **binomPdf** command from **CATALOG**, **F3 Flash Apps**, and type **10**, **.5**, **list1** to complete the command.

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list1	list2	list3	list4		list1	list2	list3	list4		list1	list2	list3	list4
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list1=seq(x,x,0,10) MAIN RADAUTO FUNC 1/6					list2=binomPdf(10,.5,lis] MAIN RADAUTO FUNC 2/6				list2[5]=.20507812500001 MAIN RADIAUTO FUNC 2/6				

#### b) Draw a histogram of the binomial distribution.

The following screens illustrate the procedures to draw the histogram. In the list editor press F2 for Plots. Select 1: Plot Setup. Highlight Plot 1 and press F1 for Define. Select 4:Histogram for Plot Type. Type list1 for x, 1 for Hist. Bucket Width, select Yes for Use Freq and Categories?, and type list2 for Freq (frequency).

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Press the **green diamond key** and **F1** to enter the equation editor. Make sure Plot 1 is selected. The check mark indicates that it is selected. F4 is a toggle for selecting and deselecting functions. Press the **green diamond key** and **F2** to enter the window editor. Assign the window settings displayed in the middle screen below. Press the **green diamond key** and **F3** to graph the histogram. Press **F3** and the right (left) arrow key to trace.



c) What is the probability of answering correctly at most 4 questions?

#### Solution:

The following screens portray how to use the binomial cumulative density function, "**binomCdf**" command in either of the two methods described in part a.



The answer is .376953 or approximately 37.7%.

## References

Connors, M.A. and Connors, E.A. (in press). "Statistics With The TI-89 Statistics Flash Application And List Editor," *Proceedings of the Fourteenth International Conference on Technology in Collegiate Mathematics, Baltimore, MD*, November 1-4, 2001. Reading, MA: Addison Wesley.