## By

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## Textbook Correlation: Key Topic

- Binomial Distribution
- Probability Distribution
- Histogram

NCTM Principles and Standards:

- Process Standard
- Representation
- Connections
- Problem Solving


## Description

The purpose of this activity is to apply the binomial probability distribution function, the binomial cumulative density function, and a histogram to analyze the probability of an outcome.

A True -False test has ten items. Count the number X of correct answers. There are $\mathbf{n}=\mathbf{1 0}$ observations. Successive outcomes are independent. Each answer falls into one of only two categories, success or failure. The probability of a success (a correct answer) is $p=0.5$ for each question.
a) What is the probability of answering correctly exactly 4 questions?

## Solution:

Method I.
Place the cursor in the entry line on the HOME screen. Select the binomial probability distribution function, "binomPdf" from CATALOG, F3 Flash Apps. Press enter to paste the command on the entry line of the HOME screen. Complete the command by entering $\mathbf{1 0}, \mathbf{5}, \mathbf{4}$ ) for $\mathrm{n}, \mathrm{p}$ and X respectively and the right parenthesis key.


The answer is . $\mathbf{2 0 5 0 7 8}$ or approximately $\mathbf{2 0 . 5 \%}$.

Method II.
If we want to obtain the list for all eleven outcomes, we can type the command in the list editor as illustrated below. Enter all the possible outcomes in list1. Highlight list2, paste the binomPdf command from CATALOG, F3 Flash Apps, and type 10, .5, list1 to complete the command.


## b) Draw a histogram of the binomial distribution.

The following screens illustrate the procedures to draw the histogram. In the list editor press $\mathbf{F} 2$ for Plots. Select 1: Plot Setup. Highlight Plot 1 and press F1 for Define. Select 4:Histogram for Plot Type. Type list 1 for $\mathbf{x}, \mathbf{1}$ for Hist. Bucket Width, select Yes for Use Freq and Categories?, and type list2 for Freq (frequency).


Press the green diamond key and F1 to enter the equation editor. Make sure Plot 1 is selected. The check mark indicates that it is selected. F4 is a toggle for selecting and deselecting functions. Press the green diamond key and $\mathbf{F} 2$ to enter the window editor. Assign the window settings displayed in the middle screen below. Press the green diamond key and F3 to graph the histogram. Press F3 and the right (left) arrow key to trace.


## c) What is the probability of answering correctly at most 4 questions?

## Solution:

The following screens portray how to use the binomial cumulative density function, "binomCdf" command in either of the two methods described in part a.


The answer is $\mathbf{.} \mathbf{3 7 6 9 5 3}$ or approximately $\mathbf{3 7 . 7 \%}$.

## References

Connors, M.A. and Connors, E.A. (in press). "Statistics With The TI-89 Statistics Flash Application And List Editor," Proceedings of the Fourteenth International Conference on Technology in Collegiate Mathematics, Baltimore, MD, November 1-4, 2001. Reading, MA: Addison Wesley.

