## Exploration 8-1 a: Introduction to Linear Regression

Objective: Find the sum of the squares of the residuals for a function found by linear regression.

Turkey Problem: Tom raises turkeys. He records the weight, $y$, measured in pounds, of one of his turkeys over several months, $x$.

| $\boldsymbol{x}$ | $\boldsymbol{y}$ |
| :---: | ---: |
| 2 | 7 |
| 5 | 9 |
| 8 | 18 |
| 11 | 17 |
| 14 | 24 |



1. The graph is a scatter plot of the data, along with the linear regression line. Run linear regression on the data to find the particular equation of this line. Use $\hat{y}$ (pronounced " $y$ hat") to distinguish the $y$-values for the regression equation from the $y$-values in the data. Store this equation as $y_{1}$ in your grapher.
$\hat{y}=$
2. Calculate the value of $\hat{y}$ for each value of $x$ in the table. Record the results in a new, third column in the table.
3. The dotted lines on the graph show by how much each data point deviates from the regression line. This is called the residual deviation, or simply the residual. Calculate the residual, $y-\hat{y}$, for each $x$-value, and record the results in a fourth column.
4. Show that the sum of the residuals is zero.
5. Square each residual and record the results in a fifth column. Then find the sum of the squares of the residuals. This number is abbreviated $S S_{\text {res }}$. It is a measure of how well the equation fits the data. The smaller the $S S_{\text {res }}$, the better the fit.

$$
S S_{\mathrm{res}}=
$$

$\qquad$
6. In Problem 1, you found $\hat{y}=1.4 x+3.8$. The value of $S S_{\text {res }}$ for this equation is the lowest possible. Demonstrate that this is correct by using the function $y_{2}=1.4 x+3.9$, which increases the $y$-intercept by 0.1 , to calculate $S S_{\text {res }}$ again. Show that the answer is greater than in Problem 5. What does this fact tell you about the new function?

| $\boldsymbol{x}$ | $\boldsymbol{y}$ |
| :---: | :---: |
| 2 | 7 |
| 5 | 9 |
| 8 | 18 |
| 11 | 17 |
| 14 | 24 |

$S S_{\text {res }}=\square$
7. Use the function $y_{3}=1.5 x+3.8$, which increases the slope of the regression equation by 0.1 , to calculate $S S_{\text {res }}$ a third time. What do the results indicate about how well $\hat{y}, y_{2}$, and $y_{3}$ fit the given data?

| $\boldsymbol{x}$ | $\boldsymbol{y}$ |
| :---: | :---: |
| 2 | 7 |
| 5 | 9 |
| 8 | 18 |
| 11 | 17 |
| 14 | 24 |

$S S_{\text {res }}=$ $\qquad$
8. What reason can you think of to explain why the turkey's weight decreased between the 8th and the 11th month?
9. What did you learn as a result of doing this Exploration that you did not know before?

