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| **Math Objectives**   * Students will discover and discuss the graphical and algebraic relationships a function has with its inverse and the line . * Students will apply inverse functions to real world situations including temperature and money conversions. * Students will try to make a connection with how to understand these topics in IB Mathematics courses and on their final assessments.   **Vocabulary**   * Inverse • Reflection • Domain * Range   **About the Lesson**   * This lesson is aligning with the curriculum of IB Mathematics Applications and Interpretations SL/HL and IB Mathematics Approaches and Analysis SL/HL * This falls under the IB Mathematics Content Topic 4 Functions:   **2.2e** Inverse function as a reflection in the line and the notation .  **2.5c** (AA only) Finding the inverse function .  **2.14b** (AA HL only) Finding the inverse function , including domain restrictions.   * As a result, students will: * Apply this information to real world situations   **HH_SW_iconsTI-Nspire™ Navigator™**   * Transfer a File. * Use Class Capture to examine patterns that emerge. * Use Live Presenter to demonstrate. * Use Teacher Edition computer software to review student documents. * Use Quick Poll to assess students’ understanding   .  **Activity Materials**   * Compatible TI Technologies: **Trail Blaszer:Users:ronblasz:Documents:WIP:CL947_Platform icons:Handheld_icon.png** TI-Nspire™ CX Handhelds,  Trail Blaszer:Users:ronblasz:Documents:WIP:CL947_Platform icons:Tablet_icon.png TI-Nspire™ Apps for iPad®, Trail Blaszer:Users:ronblasz:Documents:WIP:CL947_Platform icons:Software_icon.png TI-Nspire™ Software | **Tech Tips:**   * This activity includes screen captures taken from the TI-Nspire CX II handheld. It is also appropriate for use with the TI-Nspire family of products including TI-Nspire software and TI-Nspire App. Slight variations to these directions may be required if using other technologies besides the handheld. * Watch for additional Tech Tips throughout the activity for the specific technology you are using. * Access free tutorials at <http://education.ti.com/calculators/pd/US/Online-Learning/Tutorials>   **Lesson Files:**  *Student Activity*  Inverse\_Functions\_Student-Nspire.pdf  Inverse\_Functions\_Student-Nspire.doc  *TI-Nspire document*  Inverse\_Functions.tns | |
| **Move to page 1.2.** | |
| The prior knowledge needed for this activity is the relationship between a function and its inverse. The first few pages will revisit these relationships before asking you to apply this knowledge to real world scenarios.  First, we will review the graphical relationship. On page 1.4, you are given the graph of the function and the line .   |  | | --- | | **Teacher Tip:** Although the topic of inverse functions and their algebraic and graphical relationships is learned early on in Algebra 1, Algebra 2, and Precalculus, many students forget about these relationships and how to apply them to different problems. Make sure you are circling the classroom as they discuss each of these problems to ensure they are making the connections. |   **Move to page 1.3.**  Before looking at the graph on page 1.4, take a moment to discuss with a partner the significance of the  line with respect to the function and its inverse. Share your thoughts with the class.  **Possible discussion points:** A function’s inverse is a reflection in the line . To reflect over the  line , you would transform a coordinate onto .  **Move to page 1.4.**  Select the point that is hovering next to the y-axis in quadrant I. Grab the point that is on the function and move it left and right along the curve. Discuss with a partner what is happening and share your thoughts with the class.  **Possible discussion points:** As the student grabs and slides the point along the curve, each  of those points are being reflected in the line , and those points are being  geometrically traced to show the inverse of the given function. | | |
| **Move to page 1.5.** | | |
| Now let us discuss an algebraic relationship a function has with its inverse, finding a function's inverse. We use a two-step process. With the given function, you will first switch the x and y, and second, you will solve for y:  *Given Function:*    *Switch x and y:*    *Solve for y:*        \*\*Further practice:  *Find the inverse of each function.*  (a)  **Solution:**  (b)  **Solution:**  (c)  **Solution:**  **Move to page 1.6.**  Graph this new function from page **1.5** in . Discuss with a partner what you notice after graphing  the new function. Share your thoughts with the class.  **Possible discussion points:** The inverse function graphed was a complete parabola whereas the original function was a square root function and only half a parabola. This could lead to a discussion of restricted domains and how the domain and range are affected by the reflection in the line . | | |
| **Move to page 1.7.** | | |
| Extension Question:  What is the relationship between the domain and the range of a function and its inverse?  Use the graphical and algebraic relationships on the previous pages to discuss this with a partner. Share your results with the class.  **Possible discussion points:** A reflection in the line requires one to switch x and y, which is the first step in finding a function’s inverse. This also leads to a function’s domain equating to its inverse’s range and a function’s range equating to its inverse’s domain.   |  | | --- | | **Teacher Extension:** If time permits, this is a great place to have students compare values in the table. They can easily see how the x and y values are just switched with the side by side comparison. |      |  | | --- | | **TI-Nspire Navigator Opportunity: *Quick Poll (Open Response)***  **Given that , find .** |  |  | | --- | | **Teacher Tip:** Please know that in this activity there is a lot of time dedicated to students talking with one another and sharing their thoughts with the class. The goal here is to not only review inverse functions, but also to generate discussion. |   **Extension**  **Move to page 1.8.**  **Real World Inverse Function Applications Example 1:**  *Temperature Conversions*  (°F → °C and °C → °F)  The formula to convert temperatures from degrees Celsius to Fahrenheit is  (a) Write the inverse function, which converts temperatures from Fahrenheit to Celsius.  **Solution:**    (b) Find the Celsius temperature that is equal to 89 degrees Fahrenheit.  **Solution:** 31.7  (c) Explain how you could have found the answer to part (b) without finding the inverse function.  **Possible discussion points:** Using the idea that a function’s domain is equal to the inverse’s range and using the table feature on the Nspire to find the corresponding temperature to approximately 89 .  **Move to page 1.9.**  **Real World Inverse Function Applications Example 2:**  *Money Conversions*  A Canadian traveler who is heading to the United States exchanges some Canadian dollars for U.S. dollars. At the time of his travel, $1 Can = $0.79 U.S.  At the same time an American business woman who is in Canada is exchanging some U.S. dollars for Canadian dollars at the same exchange rate.  (a) Write an equation that gives the amount of money in U.S. dollars, d, as a function of the Canadian dollar amount, c, being exchanged.  **Solution:**  (b) Find the amount of money in U.S dollars that the Canadian traveler would get if he exchanged $500.  **Solution:**  (c) Find the amount of money in Canadian dollars that the American Business woman would get if she exchanged $1000 U.S.  **Solution:**  (d) Explain why it might be helpful to write the inverse of the function you wrote in part (b) to answer part (c). Then, write an equation that defines the inverse function.  **Possible solution:** Since you are reversing the exchange process, it will be helpful to undo the operation of the initial money exchange. You will change from multiplying by 0.79 to convert to US dollars to dividing by 0.79 to convert to Can dollars. The equation would be .  **Further IB Style Question:**  The price of a liter of soda at Carl’s Convenient Store is $1.20. Carl’s is having a sale on soda. If you purchase a minimum of 8 liters, a $4 discount is applied to your total. This can be modeled by the function, S, which gives the total cost when buying a minimum of 8 liters of soda.  (a) Find the total cost of buying 10 liters of soda at Carl’s. [2 marks]  **Solution:**  (b) Find . [2 marks]  **Solution:** Knowing that the range of function is equal to the domain of the inverse, then | | |

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