

Approximating Pi

by – Sandra Hocutt

Activity overview

Archimedes was a Greek mathematician who lived during the third century B.C. Among his contributions to mathematics was an early method for approximating pi – the ratio of the circumference to the diameter of a circle. In his method, Archimedes used regular polygons constructed inside and outside of circles. The perimeter of the polygon approximates the circumference of the circle. Thus pi is approximately the polygon perimeter divided by the diameter of the circle. Using Graphs and Geometry, the students will construct regular polygons and circumscribed circles. They will then take measurements and store them into a Lists and Spreadsheets application and make calculations to see how closely they approach pi.

Concepts

Regular polygons, circles, perimeter and circumference.

Teacher preparation

Students should know regular polygons, circles, and how to use the TI-nspire. Cabri Jr. knowledge transfers to TI-nspire graphs and geometry.

Classroom management tips

Students will be given assigned polygons. They will compare their results when finished.

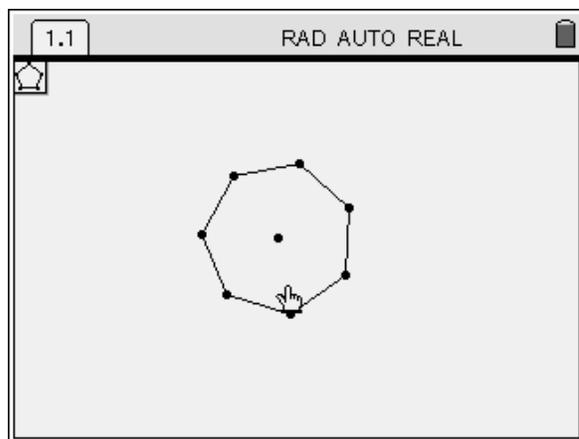
TI-Nspire Applications

TI-Nspire and/or TI-Nspire CAS Graphs and Geometry and Lists and Spreadsheet applications will be used during this activity

Step-by-step directions

Step 1.

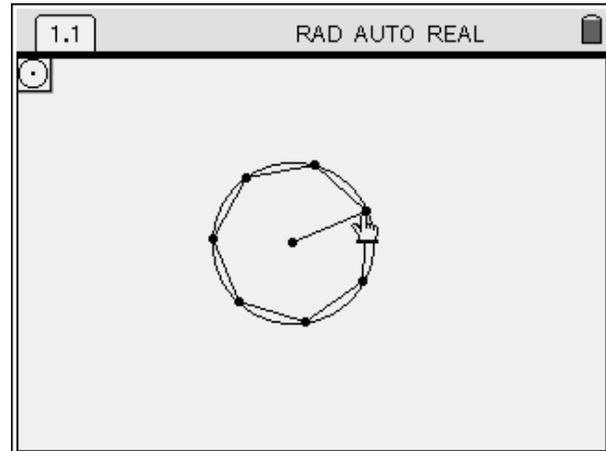
Open a new document. Remove the function line by pressing (ctrl) (G). Remove the axes by pressing (menu), 2:View, 4:Hide axes. Press (menu), 8:Shapes, 5:Regular Polygon, (enter). Move the cursor to the center of the screen and press (enter) to mark the center of the polygon. Move the cursor out to mark the outside of the polygon and press (enter). To decrease the number of sides on the polygon, press the left arrow on the Nav-Pad. To increase the number of sides, press the right arrow.



Step 2.

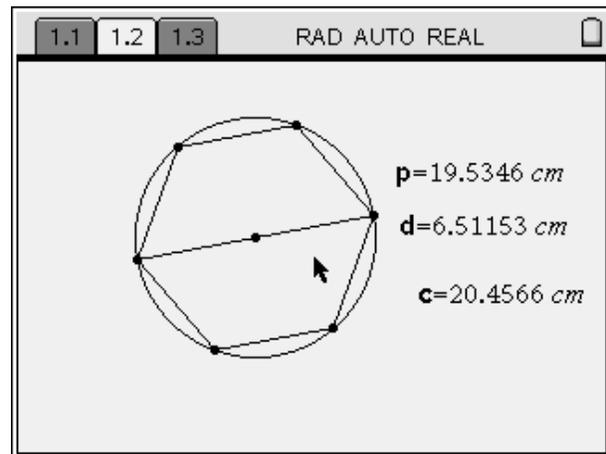
Press (menu), 6: Points and Lines, 5:Segment.
 Move the cursor to one of the vertices on the polygon to anchor the first endpoint, then to the opposite side for the other endpoint. (If the assigned polygon has an odd number of sides, the second endpoint will be the center.)
 Press (menu) 8:Shapes, 1:Circle. Use the center of the polygon as the center of the circle and one of the vertices as the outside of the circle.

If the polygon you were assigned has an odd number of sides, you will need to construct a diameter. First, (menu), 6: Points and Lines, 4:line. Use the vertex with the segment as one endpoint and the center as the other point. Press (menu), 6: Points and Lines, 3: Point of Intersection, to anchor the diameter on the circle.

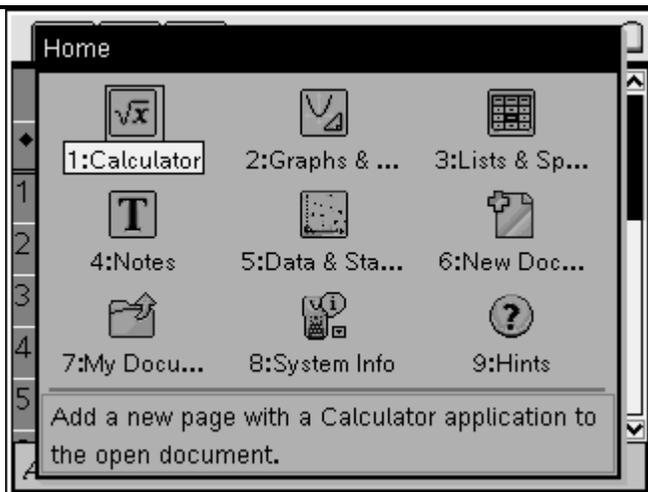


Step 3:

You will now measure the diameter, the perimeter and the circumference. Once these are measured, you will store each as a variable. Label the circumference as c , the diameter as d and the perimeter as p .



Step 4.
 Create a new page. Do this by pressing 3:
 Lists and Spreadsheets.



Step 5.
 Label the columns cir, dia, per, cir/d, and per/d.

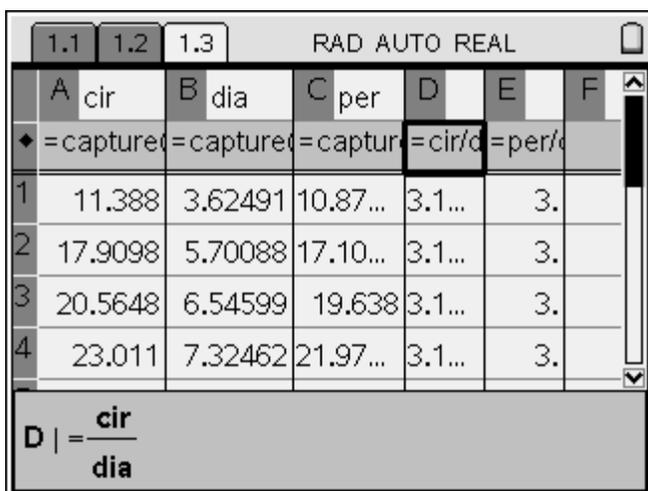
In the cell beneath the label for column a, press Ⓜ , Actions, Data Capture, 2: Manual Capture. Link to cir.

Repeat for columns b and c, linking to dia and per.

For column d, in the space beneath the label, type, \ominus cir/dia. For column e, type \ominus per/dia.

To populate the columns, go back to the graphs and geometry page, press Ⓜ ⏏

Grab one of the vertices and move it to another location. Notice that this changes the measurements. Press Ⓜ ⏏ . Repeat this process several times.



	1.1	1.2	1.3	RAD AUTO REAL		
	A cir	B dia	C per	D	E	F
	= captured	= captured	= captured	= cir/d	= per/d	
1	11.388	3.62491	10.87...	3.1...	3.	
2	17.9098	5.70088	17.10...	3.1...	3.	
3	20.5648	6.54599	19.638	3.1...	3.	
4	23.011	7.32462	21.97...	3.1...	3.	

$D = \frac{\text{cir}}{\text{dia}}$

Assessment and evaluation

Have students compare their columns D and E. Whose polygon has the closest approximation to pi?

Student TI-Nspire Document

None. Students will create the above document.