## Topic 5: Calculus

Timekeepers Inc. produces and sells watches. The Company's profit, $P$, in thousands of dollars, changes based on the number of watches, $w$, they produce per month.

The rate of change of their profit from producing $w$ watches is modelled by

$$
\frac{d P}{d w}=-1.2 w+30, \quad w \geq 0
$$

The company makes a profit of 70 (thousand dollars) when they produce 20 watches.
(a) Find an expression for $P$ in terms of $w$.
(b) The company regularly increases the number of watches it produces. watches per month and up to 35 watches per month. Justify your answer.

Mark scheme:

$$
\begin{array}{ll}
\text { (a) Evidence of integration } & \text { M1 } \\
\begin{array}{ll}
P(w)=-0.6 w^{2}+30 w(+c) & \text { A1 A1 } \\
70=-0.6(20)^{2}+30(20)+c & \text { M1 }
\end{array}
\end{array}
$$

Note: Award $\boldsymbol{M} \mathbf{1}$ for correct substitution of $w=20$ and $P=10$. A constant of integration must be seen (can be implied by a correct answer).

$$
\begin{aligned}
& c=-290 \\
& P(w)=-0.6 w^{2}+30 w-290
\end{aligned}
$$

(b) Profit will decrease (with each new watch produced)

Either
Because the profit function is decreasing/ the gradient is negative/ the rate of change of $P$ is
negative
Or
$\int_{25}^{35}-1.2 w+30(d x)=-60$
Or
Evidence of finding $P(25)=85$ and $P(35)=25$
Note: Award at most R1A0 if $P(25)$ or $P(35)$ or both have incorrect
A1
 values.

