

## More Power to Ya!

ID: 11303

Time Required  
10–15 minutes


## Activity Overview

In this activity, students will use the Calculator application to explore the Power Rule. For each of the four examples, they will first examine “true” statements about various derivatives of  $x^n$  where  $n$  is an integer. They will observe patterns, and use these patterns to create a rule for finding the derivative of  $x^n$  with respect to  $x$ . They will then use their rule to create examples of their own.

## Topic: Power Rule

- Derivative of  $x^n$  with respect to  $x$
- Definition of a derivative

## Teacher Preparation and Notes

- This activity uses the  $\frac{d}{dx}f(x)$  notation to denote the derivative. Some students may attempt to type the letter  $d$  in the numerator of a fraction and ‘ $dx$ ’ in the denominator. This will not work. In the Calculator application, this notation can be found in the Calculus menu (**MENU > Calculus > Derivative**). Alternatively, you may find the derivative template in the templates menu in the catalog, .
- **To download the student TI-Nspire document (.tns file) and student worksheet, go to [education.ti.com/exchange](http://education.ti.com/exchange) and enter “11303” in the quick search box.**

## Associated Materials

- *MorePowerToYa\_Student.doc*
- *MorePowerToYa.tns*

## Suggested Related Activities

To download any activity listed, go to [education.ti.com/exchange](http://education.ti.com/exchange) and enter the number in the quick search box.

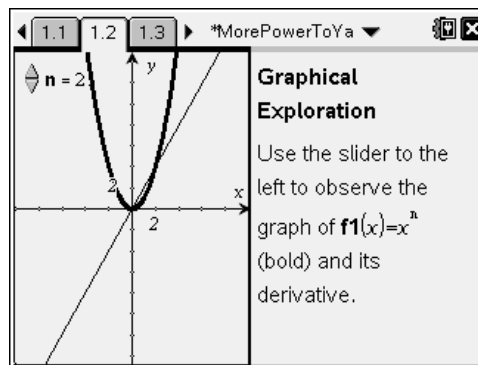
- *The Derivative of a Polynomial (TI-Nspire technology)* — 9858

**Problem 1 – Graphical Exploration**

Students are to use the slider to observe the graph of  $f(x) = x^n$  and its derivative. Students should begin to predict the relationship between  $x^n$  and its derivative.

**Student Solutions**

- The degree of the derivative is one less than that of the original function.

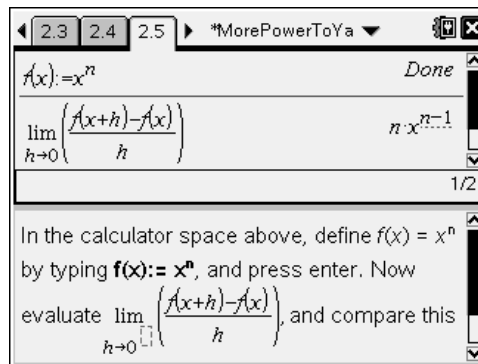
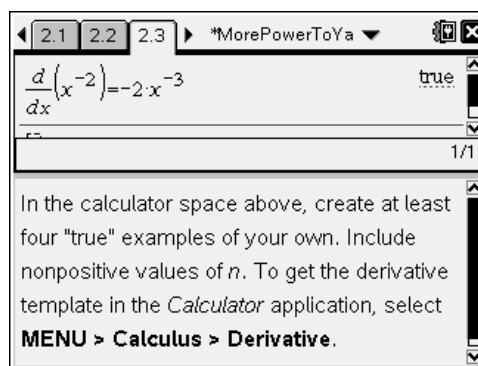


**Problem 2 – Defining the Derivative of  $x^n$**

On page 2.2, students are to examine four true statements of the derivative of  $x^n$  with respect to  $x$  where  $n$  is an integer. They are then asked to observe any patterns. After coming up with a pattern, students will test several examples of their own on page 2.3.

Students should create a rule for taking the derivative of  $x^n$  that fits the given examples and the examples that they created.

Students are asked to use the calculator space at the top of the page to find the derivative of  $x^n$  with respect to  $x$ , using the definition of a derivative. They are to compare this result with the result found on page 2.4. Students should be aware that this result is called the Power Rule.



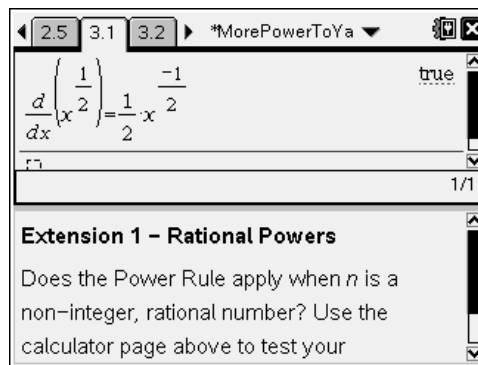
*Note:* If the variable  $n$  is already defined, the results will not be correct. The value for the variable can be deleted using the command **delvar**  $n$  in the Calculator screen.

**Student Solutions**

- The exponent becomes the coefficient of  $x$  and the degree is one less. Sample answers:  $\frac{d}{dx} x^6 = 6 \cdot x^5$ ,  $\frac{d}{dx} x^7 = 7 \cdot x^6$ ,  $\frac{d}{dx} x^{-2} = -2 \cdot x^{-3}$ ,  $\frac{d}{dx} x^{-3} = -3 \cdot x^{-4}$
- Sample answer:  $\frac{d}{dx} x^n = n \cdot x^{n-1}$
- Sample answer: The result is the same as the rule I found.

**Extension**

Students are asked if the Power Rule applies when  $n$  is a non-integer, rational number. They should use the calculator space on page 3.1 to test their conjecture.



**Student Solution**

- Yes, the Power Rule also applies when  $n$  is a non-integer, rational number.

For example,  $\frac{d}{dx} x^{\frac{1}{2}} = \frac{1}{2} x^{-\frac{1}{2}}$

Students are asked to, expand the binomial  $(x + h)^n$  on a separate piece of paper. They will use this to evaluate the limit they entered on page 2.5 by hand to prove the Power Rule.

**Student Solution**

- $$\begin{aligned} & \lim_{h \rightarrow 0} \frac{(x+h)^n - x^n}{h} \\ &= \lim_{h \rightarrow 0} \frac{\left( {}_n C_0 x^n + {}_n C_1 x^{n-1} h + {}_n C_2 x^{n-2} h^2 + \dots + {}_n C_{n-1} x h^{n-1} + {}_n C_n h^n \right) - x^n}{h} \\ &= \lim_{h \rightarrow 0} \frac{\left( {}_n C_1 x^{n-1} h + {}_n C_2 x^{n-2} h^2 + \dots + {}_n C_{n-1} x h^{n-1} + {}_n C_n h^n \right)}{h} \\ &= \lim_{h \rightarrow 0} \frac{h \left( {}_n C_1 x^{n-1} + {}_n C_2 x^{n-2} h + \dots + {}_n C_{n-1} x h^{n-2} + {}_n C_n h^{n-1} \right)}{h} \\ &= \lim_{h \rightarrow 0} \left( {}_n C_1 x^{n-1} + {}_n C_2 x^{n-2} h + \dots + {}_n C_{n-1} x h^{n-2} + {}_n C_n h^{n-1} \right) \\ &= {}_n C_1 x^{n-1} \\ &= n \times x^{n-1} \end{aligned}$$

where  ${}_n C_r = \frac{n!}{(n-r)! \cdot r!}$