## Geometry

## Polygons and Angles：Looking for Patterns．

Name：

## Getting Started：

Step 1：On your TI－nSpire calculator go to the home screen（ヘ⿴囗十 Documents．＂Find＂Polygons and Angles－BLP＂and hit enter 气inier ．You will be asked to save the previous document．Just choose＂No．＂

Step 2：The first screen（1．1）is just the title of the activity．Hit control／and right cursor on the donut to go to the next page．

## Interior and Exterior Angles

Step 3：Interior and Exterior angles（1．2）．Record the original values of $m \angle A C B$ and $m \angle A C E$ ．Grab A by moving the cursor over the letter until the hand appears $\mathbb{A}$ and then hold down the center button（＊＊）until the hand closes S．Use the arrow keys until the values change．Record the new values．Repeat three more times．Fill in the chart as you go．When you are finished go to the next page by hitting control ctri）and right cursor on the donut．

| $\mathrm{m} \angle \mathrm{ACB}$ | $\mathrm{m} \angle \mathrm{ACE}$ | $\mathrm{m} \angle \mathrm{ACB}+\mathrm{m} \angle \mathrm{ACE}$ |
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Step 4：Interior and Exterior angles（1．3）．Record the original values of $m \angle$ UAD and $m \angle U A S$ ．Grab $U$ by moving the cursor over the letter until the hand appears \＆ and then hold down the center button＊＊＊until the hand closes S．Use the arrow keys until the values change． Record the new values．Repeat three more times．Fill in the chart as you go．When you are finished go to the next page by hitting control atrl right cursor on the donut．

| $\mathrm{m} \angle \mathrm{UAD}$ | $\mathrm{m} \angle \mathrm{UAS}$ | $\mathrm{m} \angle \mathrm{UAD}+\mathrm{m} \angle \mathrm{UAS}$ |
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Observation 1：Write a conjecture about the relationship of an interior angle and its corresponding exterior angle．

## Angles of a Triangle

Step 5: Sum of the interior angles. Go to the next page (2.1) by hitting control ctrt and right cursor on the donut. To collect the data just hit control ctri) decimal point $\zeta$. You will see the $1^{\text {st }}$ line of the chart automatically fill in. Move any point of the triangle to change the measures of the angles. Stop and collect the data after each move. Collect at least five sets of data; record in the table below. In order to see the last column hit control atri) tab (tab) to switch to the right hand side of the screen cursor to the right to see the fourth column.

| $\mathrm{m} \angle \mathrm{A}$ | $\mathrm{m} \angle \mathrm{B}$ | $\mathrm{m} \angle C$ | $\mathrm{~m} \angle A+\mathrm{m} \angle \mathrm{B}+\mathrm{m} \angle C$ |
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Observation 2: Write a conjecture about the relationship of the interior angles of a triangle.

Step 6: Sum of the exterior angles. Go to the next page (3.1) by hitting control ctrl and right cursor on the donut. To collect the data just hit control ${ }^{\text {ctrrr }}$, decimal point $\zeta$. Although you can't see the table on 3.2 it will still fill in as you collect data. Move any point of the triangle to change the measures of the angles. Stop and collect the data after each move. Collect at least five sets of data; record in the table below. In order to see the table hit control cotrl right cursor to proceed to page 3.2.

| $\mathrm{m} \angle \mathrm{DTI}$ | $\mathrm{m} \angle G I R$ | $\mathrm{~m} \angle \mathrm{TRF}$ | $\mathrm{m} \angle \mathrm{DTI}+\mathrm{m} \angle G I R+\mathrm{m} \angle$ TRF |
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Observation 3: Write a conjecture about the relationship of the exterior angles of a triangle.

Step 7: A regular triangle (3.3). A regular triangle has been constructed on this page. Measure all six angles by hitting menu menu choose 7: Measurement, on the sub menu choose 4: Angle. You should see an angle icon in the upper left hand corner of the screen. In order to measure an angle you must choose the 3 points that make up the angle with the vertex in the center. When you see the measure of the angle you must hit enter to make it stick. Move the measure to the appropriate angle. Fill in your information below. Grab one of the points and move it. Note the angle measures.

| Interior Angles | Exterior Angles |
| :--- | :--- |
| $\mathrm{m} \angle 1=$ | $\mathrm{m} \angle 6=$ |
| $\mathrm{m} \angle 2=$ | $\mathrm{m} \angle 7=$ |
| $\mathrm{m} \angle 3=$ | $\mathrm{m} \angle 8=$ |

Observation 4: Write a conjecture about the interior and exterior angles of a regular triangle.

## Angles of a Quadrilateral

Step 8: Go to the next page (4.2) by hitting control ant and right cursor on the donut. To collect the data just hit control ctrl , decimal point $\zeta$. Although you can't see the table on 4.3 it will still fill in as you collect data. Move any point of the quadrilateral to change the measures of the angles. Stop and collect the data after each move. Collect at least five sets of data; record in the table below. In order to see the table hit control cotrl right cursor to proceed to page 4.3.

| $\mathrm{m} \angle \mathrm{A}$ | $\mathrm{m} \angle \mathrm{B}$ | $\mathrm{m} \angle C$ | $\mathrm{~m} \angle \mathrm{D}$ | $\mathrm{m} \angle A+\mathrm{m} \angle B+\mathrm{m} \angle C+m \angle \mathrm{D}$ |
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Observation 5: Write a conjecture about the relationship of the interior angles of a quadrilateral.

Step 9: Sum of the exterior angles. Go to the next page (5.1) by hitting control ctrl and right cursor on the donut. To collect the data just hit control ctrl, decimal point $\because$. Although you can't see the table on 5.2 it will still fill in as you collect data. Move any point of the quadrilateral to change the measures of the angles. Stop and collect the data after each move. Collect at least five sets of data; record in the table below. In order to see the table hit control ctrr right cursor to proceed to page 5.2.

| $\mathrm{m} \angle \mathrm{XFR}$ | $\mathrm{m} \angle \mathrm{YRO}$ | $\mathrm{m} \angle \mathrm{GOZ}$ | $\mathrm{m} \angle \mathrm{FGW}$ | $\mathrm{m} \angle \mathrm{XFR}+\mathrm{m} \angle \mathrm{YRO}+\mathrm{m} \angle G O Z+\mathrm{m} \angle \mathrm{FGW}$ |
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Observation 6: Write a conjecture about the relationship of the exterior angles of a quadrilateral.

Step 10: A regular quadrilateral (5.3). A regular quadrilateral has been constructed on this page. Measure both angles by hitting menu menu) choose 7: Measurement, on the sub menu choose 4: Angle. You should see an angle icon in the upper left hand corner of the screen. In order to measure an angle you must choose the 3 points that make up the angle with the vertex in the center. When you see the measure of the angle you must hit enter to make it stick. Move the measure to the appropriate angle. Fill in your information below. Grab one of the points and move it. Note the angle measures.

| Interior Angles | Exterior Angles |
| :---: | :---: |
| $\mathrm{m} \angle \mathbf{7}=$ | $\mathrm{m} \angle 8=$ |

Observation 7: Write a conjecture about the interior and exterior angles of a regular triangle.

## Angles of a Pentagon

Step 11: Go to page 6.1.

Conjecture about the interior angles of a pentagon:

Step 12: Collect data on page 6.2 and observe the answer on 6.3. Was you conjecture correct? If not, revise your conjecture.

Revised Conjecture:

Step 13: Finally, make a conjecture about the sum of the exterior angles of a pentagon, the measure of one interior angle of a pentagon, and the measure of one exterior angle of a pentagon.

Sum of the exterior angles:

One interior angle:

One exterior angle:

