# NUMB3RS Activity: Clearing All Obstacles Episode: "Hot Shot" 

Topic: Parabolic Equations
Grade Level: 10-12
Objective: Students will use the TI-Navigator ${ }^{\text {TM }}$ system to explore changes of projectile motion due to initial angle of flight.
Time: 30 minutes
Materials: TI-83/84 Plus graphing calculators, TI-Navigator ${ }^{\text {TM }}$ system, piece of paper made into a paper ball, plastic spoon, CBL $2^{\text {TM }}$, Vernier Photogate sensor, DATAGATE Program, PhotogateSetup.doc, ProjectileA.act, ProjectileB.act
To download these files, go to http:Ileducation.ti.com/exchange and search for " 6955 ."

## Introduction

In "Hot Shot," Larry is in his office catapulting grapes with a spoon to practice for the Physics Department food fight. This catapulting action is similar to work that was done in the Middle Ages when Galileo Galilei found that the path of a projectile is parabolic in nature.

As a fun exercise, you are going to us a paper ball projectile to simulate a food fight. This activity allows students to review algebraic solutions of equations as well as practice curve fitting to determine a parabolic path of a projectile. Students will first use the CBL 2 and Vernier Photogate sensor to determine the initial velocity of a paper projectile being launch from a spoon.

## Part I: Data Collection

1. a. Students should work in groups during this part of the activity.
b. Students will use the CBL 2 and Vernier Photogate to determine the velocity $v$ with which a paper projectile leaves a plastic spoon.
c. Students should follow the instructions on the Photogate Setup Guide to determine the velocity $v$.
d. Have students repeat the trial three times and find an average velocity for their group.
2. a. Assign each group an angle at which their paper projectile has left the spoon.

| Group 1: | $15^{\circ}$ angle |
| :--- | :--- |
| Group 2: | $25^{\circ}$ angle |
| Group 3: | $35^{\circ}$ angle |
| Group 4: | $45^{\circ}$ angle |
| Group 5: | $55^{\circ}$ angle |
| Group 6: | $65^{\circ}$ angle |
| Group 7: | $75^{\circ}$ angle |

b. Using this angle, students should find the vertical velocity $V_{V}$ and horizontal velocity $V_{H}$ of the projectile using the following equations:

$$
\begin{array}{ll}
\text { Horizontal Velocity: } & V_{H}=v(\cos (\theta)) \\
\text { Vertical Velocity: } & V_{v}=v(\sin (\theta))
\end{array}
$$

Example with a velocity of $10 \mathrm{~m} / \mathrm{s}$ and an angle of launch of $70^{\circ}$ :

| Horizontal Velocity: | $V_{H}=10\left(\cos \left(70^{\circ}\right)\right)$ <br>  <br>  <br> Vertical Velocity: |
| :--- | :--- |
|  | $V_{H}=3.42 \mathrm{~m} / \mathrm{s}$ |
|  | $V_{v}=10\left(\sin \left(70^{\circ}\right)\right)$ |
|  | $V_{v}=9.40 \mathrm{~m} / \mathrm{s}$ |

Note: Make sure your calculator is in degree mode.
c. Once students determine the vertical and horizontal velocities, they must determine the vertical and horizontal displacement over time. Have students use the following formulas to calculate the vertical and horizontal displacement for the given time values in the table:

$$
\begin{array}{ll}
\text { Horizontal Displacement: } & x=V_{H}(t) \\
\text { Vertical Displacement: } & y=-4.9\left(t^{2}\right)+V_{v}(t)+\underset{\left(H_{0}=\text { Initial height of object }\right)}{H_{0}}
\end{array}
$$

| Time <br> $(t)$ | Horizontal <br> Velocity <br> $\left(V_{H}\right)$ | Horizontal <br> Displacement <br> $\left(\mathrm{L}_{1}\right)$ | Vertical <br> Velocity <br> $\left(\boldsymbol{V}_{\mathbf{v}}\right)$ | Vertical <br> Displacement <br> $\left(\mathrm{L}_{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: |
| 0.0 |  |  |  |  |
| 0.1 |  |  |  |  |
| 0.2 |  |  |  |  |
| 0.3 |  |  |  |  |
| 0.4 |  |  |  |  |
| 0.5 |  |  |  |  |
| 0.6 |  |  |  |  |
| 0.7 |  |  |  |  |
| 0.8 |  |  |  |  |
| 0.9 |  |  |  |  |
| 1.0 |  |  |  |  |
| 1.1 |  |  |  |  |
| 1.2 |  |  |  |  |
| 1.3 |  |  |  |  |
| 1.4 |  |  |  |  |
| 1.5 |  |  |  |  |
| 1.6 |  |  |  |  |
| 1.7 |  |  |  |  |
| 1.8 |  |  |  |  |
| 1.9 |  |  |  |  |
| 2.0 |  |  |  |  |

d. Have students enter their horizontal displacement in list $L_{1}$ on their calculators and the vertical displacement in list $L_{2}$ on their calculators.
3. a. Launch TI-Navigator on the computer and click Begin Class to start the session.
b. Have students log into NavNet on their calculators.
c. Open the Activity Center in TI-Navigator.
d. Load the ProjectileA.act activity setting file into Activity Center. This activity setting is configured to grab the lists from the students' calculators once the activity has been started.
e. Click Start Activity. Instruct students to enter the Activity Center. Once the lists appear on their calculator screens, have students press Send.
f. Click Stop Activity.
4. a. Discuss the results of the resultant parabolic paths. Include a discussion about how the angle at which the paper projectile left the spoon affects the vertical and horizontal displacement. Also, remember to discuss how the amount of time the projectile is in flight changes with the angle.
b. Have students algebraically determine an equation that will match their plots. Remember that $x$ is horizontal displacement and $y$ is vertical displacement. This can be done by solving the horizontal displacement equation for $t$. Then substitute that solution for $t$ in the vertical displacement equation.

$$
\begin{aligned}
& x=V_{H}(t) \rightarrow t=\frac{x}{V_{H}} \\
& y=-4.9\left(\frac{x}{V_{H}}\right)^{2}+V_{V}\left(\frac{x}{V_{H}}\right)+H_{0} \quad \quad\left(H_{0}=\text { Initial Height of object }\right)
\end{aligned}
$$

Example with a velocity of $10 \mathrm{~m} / \mathrm{s}$ and an angle of launch of $70^{\circ}$ (using values found in example from $2 b$ ):

$$
\begin{aligned}
& y=-4.9\left(\frac{x}{V_{H}}\right)^{2}+V_{v}\left(\frac{x}{V_{H}}\right)+H_{0} \\
& y=-4.9\left(\frac{x}{3.42}\right)^{2}+9.40\left(\frac{x}{3.42}\right)+H_{0}
\end{aligned}
$$

5. a. Students should still be in the Activity Center. Go to the Contribute drop-down list, select Equations, and then click Configure. Reconfigure activity center so that students can submit one equation, students are allowed to resubmit equations, and send the current graph contents as background.
b. Click Start Activity and have the students input their new equation for $y$ into $Y_{1}$ and press Send.
c. Discuss the differences and similarities found in students' equations.
d. Click Stop Activity.

The goal of this activity is to give your students a short and simple snapshot into a very extensive math topic. TI and NCTM encourage you and your students to learn more about this topic using the extensions provided below and through your own independent research.

## Extension: Clearing an Object

Josh (left, white shirt) is practicing for a food fight (not recommended for actual practice). He is trying to shot a piece of food over the obstacle (the girls) to hit Barry (right, brown shirt). At what angle must Josh launch the food in order to clear the girls and hit Barry?


ProjectileB.act screen shot

1. a. In this part of the activity, students will work in groups to determine the angle at which an object must leave the spoon in order to hit a desired target.
b. Load the ProjectileB.act activity setting file into Activity Center. Go to Edit > Clear Activity Data and click Yes. This activity setting is configured to allow groups to submit an equation that will allow them to hit the desired target. Click $\downarrow$ Start Activity.
c. Have one student in each group log into NavNet and enter the Activity Center. This calculator will be used by the group to enter their equation(s) into activity center. All other calculators in the group should be used for the needed calculations to obtain the group's equation.
2. a. Using the results from Part I, find the class' average velocity.
b. Have students choose an angle to begin. Repeat Part I Steps 2b and 4b from the activity using this angle and the average velocity. Determine an equation that will allow the projectile in the picture to hit the desired target. (Hint: Students may need to change the initial height.)
c. Have the groups enter their equations into $\mathrm{Y}_{1}$ (on the calculator in the Activity Center) and press Send. Do their equations hit the target? (That is, did they choose the correct angle?)
d. If a group's equation is not correct, have them choose another angle and repeat Extension Steps 2 b and 2 c until they hit the desired target.
e. Once all equations have been submitted, click Stop Activity and discuss the results. Is there more than one angle that you could launch a projectile to hit the desired target?
