

Na	me:
	e number 72 can be factored to 9 \times 8 or 12 \times 6 or? Find some other ways to factorise 72 into the product of two whole numbers. How will you know if you have all the possible pairs? $9 \times 8 \ 12 \times 6$
b)	Find a way to factorise 72 into the product of 3 different factors. Are there any other ways to do this? Find as many as you can with a partner. You can use the calculator if needed.
c)	What about 4 different factors or 5 different factors? Investigate.



You can write 72 as the product of only its **PRIME** factors which means that only prime numbers can be used so the prime factorisation of:

72 is $2 \times 2 \times 2 \times 3 \times 3$ (called expanded form) which is usually written in shorthand form as:

72 is $2^3 \times 3^2$ (called the index or exponent form)

(The small 3 indicates that there are 3 twos multiplied together and the small 2 indicates that there are 2 threes multiplied together.)

To do this, divide the original number by 2 as many times as you can, then by 3 and so on with prime numbers only, recording as you go.

d) Write each of the numbers from the table in worksheet 1 as the product of ONLY its Prime factors in the table below. You may need to use a prime factor more than once!

- as you can see with 72.

Number	As the product of only PRIME Factors	How many factors does this number have altogether? Refer back to Worksheet 1
24		
17		
36		
25		
50		
64		
72	$2 \times 2 \times 2 \times 3 \times 3 = 2^3 \times 3^2$	12



- 2. Use the calculator to find the number represented by:
 - a) 2^4 (Press either 2 x 2 x 2 x 2 or 2 ^ 4. This is called the **EXPANDED** form.)
 - b) $2^2 \times 3^2$
 - c) $2 \times 3^3 \times 5$
 - d) $2^3 \times 3 \times 5^2 \times 7$
- 3. To write 24 as the product of its prime factors follow these steps on the calculator:

First: Set up the TI-15 as indicated below

- a) Press Frac button to enter the Fraction Menu. The selection U n/d is displayed. This lets you choose to display fractions results as mixed numbers (U n/d) or improper fractions (n/d).
- b) Press the left ← and right → arrow keys to move the underline to choose the display you want.
- c) In this case, move the underline to <u>n/d</u>.
- d) Press the down arrow -, and move the underline to MAN. This lets you choose to simplify fractions manually (using the Simp key).
- e) Select Enter.



Enter the fraction $\frac{24}{24}$

- 1. Press 24124 d Enter
- 2. Press Simple . The fraction $\frac{12}{12}$ is displayed and at the top of the screen is $\frac{n}{d} \div \frac{N}{D} \to \frac{n}{d}$ is visible.

 This means that the fraction $\frac{12}{12}$ can be simplified further.
- 3. Press Fac and a 2 is shown, meaning that the fraction has been simplified by dividing numerator and denominator by 2.
- 4. This is the first prime factor of 24. Press [and the fraction reappears.
- 5. Press Simple The fraction $\frac{6}{6}$ is displayed and at the top of the screen is $\frac{n}{d} \div \frac{N}{D} \to \frac{n}{d}$ is still visible.

Press $\overline{\text{Fac}}$ and a 2 is again shown. This means we have another factor of 2. Record the factors as you find them.

- 6. Repeat these steps until $\frac{1}{1}$ appears and the symbols at the top are now $\frac{n}{d}$ ÷ which indicates that no further simplification is possible.
- 7. Now we have the prime factors of 24 as $2 \times 2 \times 2 \times 3 = 2^3 \times 3$
- 4. Use this method to check the prime factors of 72 found above in Q 4.
- 5. Try these:
 - a) $\frac{30}{30}$
 - b) $\frac{48}{48}$
 - c) <u>67</u> 67

Each time you think you have the factors of the given number check using the calculator to multiply the factors together.



5.	Find a number with exactly 6 different factors. How many others are there with exactly 6 different factors.			
	(Hint: $8 = 2 \times 2 \times 2 = 2^3$ which has 4 factors: 1, 2, 4 and 8)			
7.	Find a number with exactly 6 different PRIME factors. How many others are there?			
8.	Find the SMALLEST number with exactly 6 factors, which need not be prime factors.			
9.	Challenge: Find the smallest number with exactly 20 factors.			