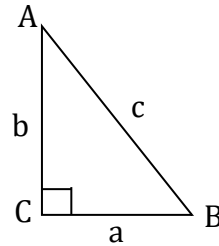


### Nspire Activity: It's the Law!!

*In this activity you will look at triangles where two sides and an included angle (SAS triangles) are given. You will derive a formula to determine missing sides & angles for this type of triangles.*

1. State the Pythagorean Theorem relating the sides in a right triangle.

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2. Based on the Pythagorean Theorem, determine the value of  $a^2 + b^2 - c^2$  for the right triangle. \_\_\_\_\_
3. Suppose sides 'a' and 'b' stay constant and angle C becomes an acute angle. Predict whether the value of ' $a^2 + b^2 - c^2$ ' will be positive, negative, or zero. Explain.

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4. Suppose sides 'a' and 'b' stay constant and angle C becomes an obtuse angle. Predict whether the value of ' $a^2 + b^2 - c^2$ ' will be positive, negative, or zero. Explain.

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5. Open the document 'lawofcos' and move to page 1.2. You will see  $\triangle ABC$  with side lengths calculated. The measurements for segment 'a' (= 3) and segment 'b' (=5) have been locked so they will not change. The value for  $a^2 + b^2 - c^2$  has also been calculated. Verify your predictions from #3 and #4 by dragging on vertices of  $\triangle ABC$  to make angle 'C' acute and obtuse.

6. Continue dragging on a vertex of  $\triangle ABC$  and observe the range of values that  $a^2 + b^2 - c^2$  takes on for all possible measures of angle C. Write the set of values observed in interval notation below.

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7. Move to page 2.1. You will see the same triangle and measurements from the previous page. There is also a graph below. You will observe the scatterplot that is formed when 'x' is represented by the measure of angle C and 'y' is represented by the value  $a^2 + b^2 - c^2$ . (You should see a point currently plotted at  $(90^\circ, 0)$  to represent 'x' and 'y' when angle C is equal to  $90^\circ$ ).

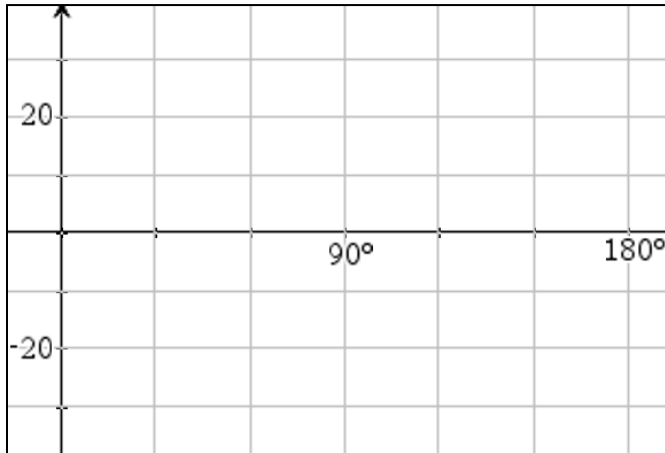
8. Grab point A and slowly drag the point so that angle C takes on a range of measurements in the interval  $(0^\circ, 180^\circ)$ . Observe the graph formed at the bottom of the page.

*What type of function would best fit this data? Explain your choice and state properties of the graph that support your choice.*

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9. Make a sketch of the graph you see at the bottom of page 2.1 below. Then, write an appropriate trig function that best fits this data.

Sketch:



Function:

\_\_\_\_\_

10. Using your function written above, set up an equation by substituting expressions for 'x' and 'y' based on what 'x' and 'y' represent. The variable definitions are re-written below.

$$'x' = \text{measure of angle } C$$

$$'y' = a^2 + b^2 - c^2$$

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11. At this point you should have one numeric coefficient remaining in your equation. Recall that 'a' = 3 and 'b' = 5. How does the remaining coefficient in your equation relate to the values for these two fixed sides?

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12. Re-write the coefficient in your equation in terms of 'a' and 'b' and re-write the equation below.

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13. Now, solve your equation in step #12 for  $c^2$ . This is the Law of Cosines!!

**Law of Cosines:** \_\_\_\_\_

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