



Problem 1 – Properties of Parallelograms

A cyclic quadrilateral is a quadrilateral inscribed in a circle. Page 1.3 shows cyclic quadrilateral *QUAD* and the measures of angles *Q*, *U*, *A*, and *D*.

1. Drag point *Q* to four different positions and collect data in the table below

Position	$\angle Q$	$\angle U$	$\angle A$	$\angle D$
1				
2				
3				
4				

2. What do you notice about the opposite angles of a cyclic quadrilateral?
3. Redefine (**MENU > Actions > Redefine**) point *Q* (on page 1.3) to be a point not on the circle. Drag point *Q* to two points inside and two points outside the circle and collect data in the table below.

Position	$\angle Q$	$\angle U$	$\angle A$	$\angle D$
1				
2				
3				
4				

4. What do you notice about the opposite angles of a quadrilateral that is not necessarily cyclic?

Answer the following questions with *always*, *sometimes*, or *never*. Use what you know about the opposite angles of special quadrilaterals (parallelogram, rectangle, kite, trapezoid, etc.) and what you know about the opposite angles of cyclic quadrilaterals.

5. A kite is _____ a cyclic quadrilateral.



Running Circles Around Quads

6. A trapezoid is _____ a cyclic quadrilateral.
7. An isosceles trapezoid is _____ a cyclic quadrilateral.
8. A parallelogram is _____ a cyclic quadrilateral.
9. A rectangle is _____ a cyclic quadrilateral.
10. A square is _____ a cyclic quadrilateral.
11. A rhombus is _____ a cyclic quadrilateral.

Problem 2 – Extension

For this problem, we will look at the angle properties created by the diagonals of cyclic quadrilaterals.

12. Page 2.2 shows the measures of angles Q , U , A , D , DQA , and DUA . Move point D between Q and A to four different points and collect data in the table below.

Position	$\angle Q$	$\angle U$	$\angle A$	$\angle D$	$\angle DQA$	$\angle DUA$
1						
2						
3						
4						

13. What do you notice about the measure of angles DQA and DUA ?