## Objective

- Students will develop an understanding of solving a system of equation using the method of substitution.


## Applicable TI InterActive! Functions

```
- Solve solve(equation, variable)
- Define function_name:= function
```


# Solving Systems of Equations: The Method of Substitution 

## Problem

There are several methods that can be used to solve a system of equations.
Students will employ the method of substitution to solve systems of equations.

## Pre-Activity

Solve the system $\begin{aligned} & 3 x+y=5 \\ & 4 x-y=2\end{aligned}$ by using the substitution method and verify graphically.

1. Let eq1 be $3 x+y=5$ and eq2 be $4 x-y=2$.
2. Using paper and pencil, have the students solve eq1 for $y$ in terms of $x$. Then have them substitute this expression in eq2 for $y$ and solve for $x$. And finally, have students substitute the $x$-value into eq1 and solve for $y$.
3. Students should open a new TI InterActive! document, select Math box⿶ and define eq1: $=3 x+y=5$. In the next math box, define eq2: $=4 x-y=2$. In the next math box, select Math $>$ Algebra $\downarrow$ Solve and type eq1,y) to solve eq1 for $y$. Have students compare this answer to their written work. Students should define $y$ to be the expression for $y$.
4. Students should use the solve command again to solve eq2 for $x$. Have them compare this answer to their written answer. In the next math box, students should define $x$ to be the result that they obtained when they solved for $x$.
5. Using the next math box, students should type $y$ to have the value of $y$ for the solution to this system of equations. Have the students compare this answer to their written answer.
6. This solution should be the $(x, y)$ point of intersection in the graph of two lines. Students should type $3 x+y$ and $4 x-y$ in math boxes to verify their solutions.

This activity has students solve systems of equations that can't be verified graphically in the $x y$ plane. Solutions to the systems of equations in the student activity can be verified using matrices. To solve the system in the pre-activity using matrices:

1. On the Math Palette, select Matrix [:::] and choose a 2 x 2 matrix.
2. Enter the coefficients as shown below.
3. Select Inverse $X^{-1}$ from the Math Palette and multiply the inverse of the coefficient matrix by a $2 x 1$ matrix of the constants.
$\left[\begin{array}{cc}3 & 1 \\ 4 & -1\end{array}\right]^{-1} *\left[\begin{array}{l}5 \\ 2\end{array}\right]$

## Exploration

3. $\mathrm{z}:=-3 \mathrm{x}+2 \mathrm{y}+6$
4. $\mathrm{y}:=\frac{11 \mathrm{x}-23}{5}$
5. $\mathrm{x}:=3$
6. $\mathrm{y}:=2$
7. $\mathrm{z}:=1$
8. 6
9. 5
10. 9
11. The solution to this system is $\{3,2,1\}$. The answers to questions $8-10$ verify the solution to this system since the left side of each equation has the same value as the corresponding right sides when $x=3, y=2$, and $z=1$.

## Additional Exercises

1. The process may vary with each student. One process could be:

## Process

## Solution

$z:=2 x+5 y+8$
$\mathrm{x}:=4$
$\mathrm{y}:=\frac{-(7 \mathrm{x}+44)}{24}$
$\mathrm{y}:=-3$
$\mathrm{x}:=4$

$$
\mathrm{z}:=1
$$

2. The process may vary with each student. One process could be:

## Process

$\mathrm{x}:=2 \mathrm{y}+3 \mathrm{z}-1$
$\mathrm{x}:=-2$
$\mathrm{y}:=\frac{-(11 \mathrm{z}+5)}{7}$
$\mathrm{z}:=-3$
$y:=4$
$\mathrm{z}:=-3$
3. The process may vary with each student. One process could be:

## Process

$y:=-3 x-5 z-2$

## Solution

$\mathrm{x}:=-1$
$\mathrm{z}:=\frac{-(\mathrm{x}+1)}{9}$
$\mathrm{x}:=-1$
$\mathrm{z}:=0$
4. The process may vary with each student. One process could be:

## Process

$y:=6 z-5$
$\mathrm{x}:=\frac{3(14 \mathrm{z}-15)}{4}$
$\mathrm{z}:=\frac{1}{2}$

## Solution

$\mathrm{x}:=6$
$\mathrm{y}:=-2$
$\mathrm{z}:=\frac{1}{2}$
5. The process may vary with each student. One process could be:

## Process

$\mathrm{z}=\frac{\mathrm{x}+2(2 \mathrm{y}-5)}{2}$
$y=\frac{5 x-26}{10}$
$x=\frac{334}{25}$

## Solution

$$
\mathrm{x}:=\frac{334}{25}
$$

$$
\mathrm{y}:=\frac{102}{25}
$$

$$
\mathrm{z}:=\frac{246}{25}
$$

6. The process may vary with each student. One process could be:

## Process

$$
\begin{aligned}
& \mathrm{z}=-\mathrm{x}+\mathrm{y}+12 \\
& \mathrm{y}=\frac{-2(2 \mathrm{x}+21)}{3} \\
& \mathrm{x}=0
\end{aligned}
$$

## Solution

$$
\mathrm{x}:=0
$$

$$
\mathrm{y}:=-14
$$

$$
\mathrm{z}:=-2
$$

