Chords, Secants, and Tangents

Exploration

- a. Using a geometry utility, draw a circle whose diameter is approximately two-thirds the width of the screen.
- **1.** A **chord** is a line segment joining any two points on a circle. Draw two chords of your circle.
 - **2.** Predict where the perpendicular bisectors of the two chords will intersect. Draw a point at that location.
 - **3.** Construct the perpendicular bisectors of the chords. Mark the intersection point (if different from the location predicted in Step 2).
 - **4.** Drag the endpoints of the chords to change their sizes and locations. Record your observations.
 - **5.** Change the size of the circle. Record your observations.
- **c.** 1. Draw a new circle and construct a diameter.
 - 2. Identify the intersection points of the diameter and the circle.
 - 3. Construct a line through one of the points of intersection.
 - **4.** Measure an angle at the intersection of the diameter and the line constructed in Step 3.
 - 5. Adjust the angle constructed in Step 3 until its measure is 90°.
 - **6.** Record your observations.

Mathematics Note

A **secant** of a circle is a line that intersects a circle in two points.

A **tangent** of a circle is a line, segment, or ray in the plane of the circle that intersects the circle in exactly one point and is perpendicular to a radius at that point. This intersection is the **point of tangency**.

For example, Figure 14 shows circle O with secant \overline{AB} , tangent \overline{BC} , and B, a point of tangency.

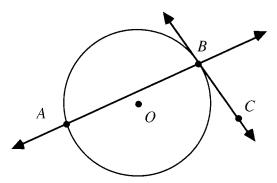


Figure 14: Circle with secant and tangent lines

Discussion 2

- a. 1. What is the measure of the angle between a diameter of a circle and a tangent to that circle whose point of tangency is the endpoint of the diameter?
 - 2. Suppose that a secant does not contain the center of a circle. If a tangent to the circle is then drawn as in Figure 14, what can be said about the measure of an angle formed by this secant and tangent?
- **b.** Describe how to use paper folding to find a line tangent to a circle.
- **c.** What is true about two tangents whose points of tangency are opposite endpoints of a diameter? Explain your response.
- d. Figure 15 shows a fragment of American Indian pottery. Before beginning reconstruction of the circular plate, a museum curator might first make a sketch of the original artifact, including its center. Using your observations from the exploration, describe how to find the center of this circular plate.

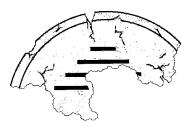


Figure 15: Pottery fragment

- **e.** Describe how to use paper folding to find the center of a circle.
- f. The perpendicular bisector of a chord is the set of points in the plane equidistant from the ends of the chord. This means that for any point C in Figure 16 below, AC = BC.

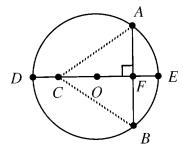


Figure 16: Chord AB and its perpendicular bisector

How does this verify that the intersection of the perpendicular bisectors of two chords is the center of the circle?

g. In Figure 16, $\triangle ABC$ is isosceles and \overline{CF} is an altitude. What is the relationship between the altitude of an isosceles triangle and its base?