

## Data Collection and Analysis

Name: Sample Answers

Date: \_\_\_\_\_

### Activity: Cooking the Thanksgiving Day Turkey

#### Collecting the data

Record your data in the table below.

Time (hours)	Temperature of Turkey (Fahrenheit)	Temperature difference between Turkey and Oven (Fahrenheit) <i>325 is the temp of the oven</i>
0	40	285
1	105	220
2	128	197
3	155	170
4	170	155

#### Analyze the data

Use the equation you find in number 1 to answer questions 2 through 4.

1. Find an equation for the data in **L1** and **L2** using Newton's Law of Heating

y = \_\_\_\_\_

L1	L2	L3a
0	40	285
1	105	220
2	128	197
3	155	170
4	170	155

$$T(t) = T_{\alpha} + (T_0 - T_{\alpha}) \cdot e^{kt}$$

$$T(t) = 325 + (40 - 325) \cdot e^{kt}$$

$$\text{Solve}(105 = 325 + (40 - 325) \cdot e^{(k \cdot 1)}, k) = k = -.258862$$

$$T(t) = 325 + (40 - 325) \cdot e^{(-.258862t)}$$

Enter your equation in Y1 in the TI-83 Plus.

The first equation was not a good fit. Try using another point.

$$T(t) = 325 + (40 - 325) \cdot e^{kt}$$

$$\text{Solve}(128 = 325 + (40 - 325) \cdot e^{(k \cdot 2)}, k) = k = -.184643$$

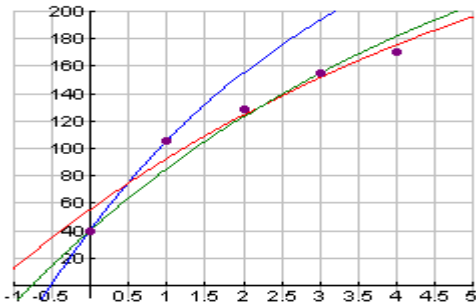
$$T(t) = 325 + (40 - 325) \cdot e^{(-.184643t)}$$

The second equation I came up with was a bit better, but I'll try one more point of data.

$$T(t) = 325 + (40 - 325) \cdot e^{kt}$$

$$\text{Solve}(155 = 325 + (40 - 325) \cdot e^{(k \cdot 3)}, k) = k = -.17223$$

$$T(t) = 325 + (40 - 325) \cdot e^{(-.17223 \cdot t)}$$



From looking at my results from all 3 I feel that my second equation was the best one to work with.

$$T(t) = 325 + (40 - 325) \cdot e^{(-.184643 \cdot t)}$$

2. What is the temperature of the turkey after one and a half hours? \_\_\_\_\_

$$325 + (40 - 325) \cdot e^{(-.184643 \cdot 1.5)} = 108.947 \text{ degrees Fahrenheit}$$

3. How long has the turkey been in the oven when the temperature of the turkey is 100°F?

\_\_\_\_\_

$$\text{Solve}(100 = 325 + (40 - 325) \cdot e^{(-.184643 \cdot t)}, t) = t = 1.28025$$

One hour and approximately 17 minutes

4. A turkey should be cooked until it reaches a temperature of 180°F. At what time should the turkey be taken out of the oven? \_\_\_\_\_

$$\text{Solve}(180 = 325 + (40 - 325) \cdot e^{(-.184643 \cdot t)}, t) = t = 3.65979$$

Three hours and approximately 40 minutes

5. Find an equation for the data in **L1** and **L3**

$y =$  \_\_\_\_\_

$$y = a \cdot b^x$$

$$285 = a \cdot b^0$$

$$a = 285$$

$$y = 285 \cdot b^x$$

$$\text{Solve}(170 = 285 \cdot b^3, b) = b = .841785$$

$$y = 285 \cdot .841785^x$$

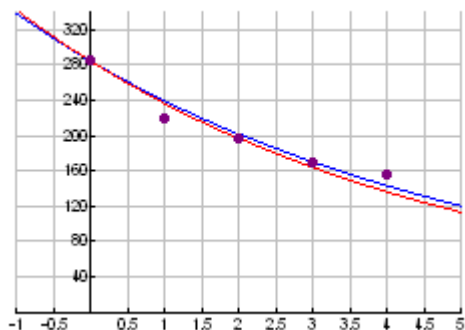
I used  $t=3$  and  $325 - \text{temp} = 170$  data point, but I think it would work better with the data point at  $t=2$ .

$$y = 285 \cdot b^x$$

$$\text{Solve}(197 = 285 \cdot b^2, b) = b = .831401 \text{ or } b = -.831401$$

$$y = 285 \cdot .831401^x$$

However, when I graphed the second set of data it did not give as close of an equation. So I am going to work with the first equation that I came up with.



6. Enter the equation from your calculator for the exponential regression

$y =$  \_\_\_\_\_ .  $y = 269.589 \cdot 0.86278^x$

Exponential Equation of Oven - Turkey temps vs. time

Exponential Regression

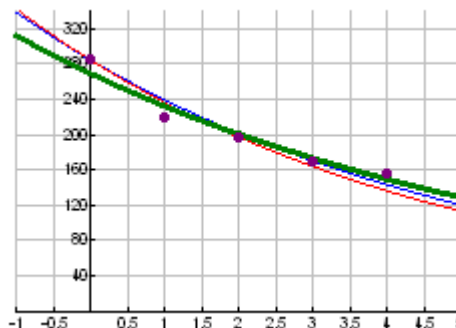
$$\text{regEQ}(x) = 269.589 \cdot .86278^x$$

$$a = 269.589$$

$$b = .86278$$

$$r = -.981629$$

$$r^2 = .963596$$



7. Is this equation close to the equation you came up with? yes

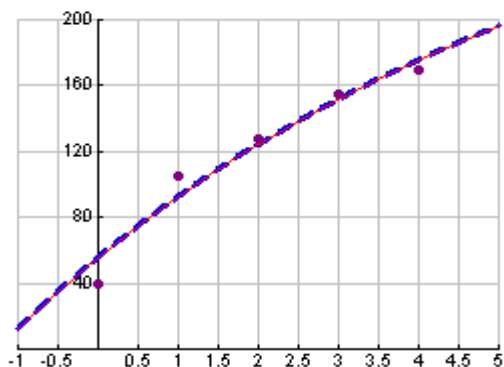
What could you have done to come up with a more accurate equation? instead of using the data points at t=0 and at t = 3, I could have used the data points at t = 2 and t = 3 to come up with the exponential equation

8. Knowing how we changed the data and equation to an exponential equation from Newton's Law of Heating, use your exponential equation from problem 6 to write an equation for the data of time vs. temperature of the turkey (**L1** vs. **L2**).

y = \_\_\_\_\_

$$T(t) = 325 - 269.589 \cdot 0.86278^t$$

9. How does this equation compare to your equation in problem 1? They look the same. WOW! :O)



10. Explain any discrepancies between your data points (**L1** vs. **L2**) and your equation in problem 9.

The discrepancies would be from opening and closing the oven and misreading the temperature and/or being off slightly on the times that I read the turkey's temperature.

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