

Chapter 6

1. $LS(100) = .306069952038$, $RS(100) = .314484661886$, $TRAP(100) = .310277306962$,
 $MID(100) = .310263799029$, $SIMP(100) = .310268301673$.
2. (a) I is exactly $-\frac{1}{8\ln 2} + \frac{1}{2\ln 2}$.
(b) $\mathbf{fnInt}(2^{-x}, x, 1, 3)$ gives .541010640333.
(c) $RS(50) = .533545297248$.
(d) $(1/25)\mathbf{sum seq}(2^{-(1+K/25)}, K, 1, 50, 1)$ also gives .533545297248.
3. The two areas are equal since $\int_0^{\pi/2} 2\sin 2x \, dx = \int_0^{\pi} \sin \theta \, d\theta$ using the substitution $\theta = 2x$.
4. (a) $\mathbf{seq}(\mathbf{fnInt}(1/x^2, x, 1, K), K, 100, 1000, 100)$ with $\mathbf{tol} = 1 \times 10^{-5}$ will generate the list
{.9900000000037, .9950000000056, .9966666666751, .9975000000067, .9980000000058, .998333333424,
.998571428652, .998750000072, .998888888955, .999000000062}.
(b) 1.48687910268E-6.
5. Take $y1 = \mathbf{fnInt}(x^{\sin x} - 0.8, x, 0, x) + 0.2$. Set $\mathbf{tol} = .01$ to speed up the graphing and then graph
 $y1$ on the window $[0, 1, .5] \times [-1, 2, 1]$.
6. Computing $\mathbf{nDer}(\mathbf{sin}(\mathbf{fnInt}(\sqrt{t^3 + 1}), t, 0, x)), x, 1.7)$ gives a negative result, so the graph is
decreasing at $x = 1.7$.