



# Polar Coordinates

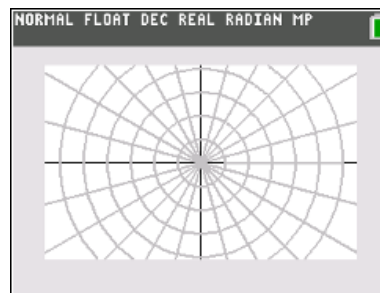
## Student Activity

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Class \_\_\_\_\_

Open the document *POLARGRD.8xp*.

In this activity, you will be introduced to the polar coordinate system. You will plot points given in polar form, convert polar coordinates to the rectangular coordinate system, and sketch the graphs of polar equations.



The polar coordinate system is a two-dimensional coordinate system defined by a point, called the pole, and a ray from the pole, called the polar axis. In a rectangular coordinate system, the **pole** is usually placed at the origin, and the **polar axis** is represented by the positive x-axis. A point in the polar coordinate system is represented by the ordered pair  $(r, \theta)$  where  $r$  is the distance from the pole and  $\theta$  is the angle (in radians) measured counterclockwise from the polar axis.

### Problem 1 – Identifying The Quadrants in a Polar System

- Press graph.** On this screen, you will see a polar grid. Use this grid to aid in completing the table below. Starting at the polar axis and rotating counterclockwise, each slant line increases by a unit of  $\frac{\pi}{12}$  (or  $15^\circ$ ) and each ring increases by one unit.
  - Complete the following tables by finding the quadrant in which the point  $(r, \theta)$  lies.

$r$	1.7	1.3	-0.6	-4.2	-3.2	3.1	-1.5	-2.5
$\theta$	$\frac{5\pi}{6}$	$-\frac{3\pi}{4}$	$-\frac{7\pi}{6}$	$\frac{3\pi}{4}$	$-\frac{4\pi}{3}$	$-\frac{13\pi}{4}$	$\frac{13\pi}{12}$	$-\frac{7\pi}{4}$
<b>Quadrant</b>								

$r$	0.8	2.1	2	-2.7	4	3.5	-1.4	-3
$\theta$	$\frac{19\pi}{6}$	$\frac{\pi}{4}$	$-\frac{17\pi}{12}$	$\frac{11\pi}{4}$	$\frac{7\pi}{6}$	$-\frac{\pi}{3}$	$\frac{11\pi}{3}$	$\frac{\pi}{3}$
<b>Quadrant</b>								

$r$	-4	2.7	1	3.9	-5	-2	-1	1.5
$\theta$	$-\frac{\pi}{6}$	$-\frac{11\pi}{3}$	$\frac{23\pi}{12}$	$-\frac{11\pi}{6}$	$-\frac{9\pi}{4}$	$\frac{11\pi}{6}$	$-\frac{7\pi}{6}$	$\frac{9\pi}{4}$
<b>Quadrant</b>								



b. Describe the location of the point with the following polar coordinates:

(i)  $r > 0$  and  $\theta = 0$

(ii)  $r < 0$  and  $\theta = \frac{3\pi}{2}$

(iii)  $r < 0$  and  $\theta = \frac{\pi}{2}$

(iv)  $r > 0$  and  $\theta = -3\pi$

**Problem 2 – Matching Polar Coordinates with Rectangular Coordinates**

If a point has polar coordinates  $(r, \theta)$ , then the rectangular coordinates are given by  $x = r \cos \theta$  and  $y = r \sin \theta$ . Similarly, if a point has rectangular coordinates  $(x, y)$ , then the polar coordinates are

$(r, \theta)$  such that  $r^2 = x^2 + y^2$  and  $\tan \theta = \frac{y}{x}$ ,  $x \neq 0$ .

2. Complete each of the following tables. Remember that there are an infinite number of polar coordinates that can be plotted in a single location. For example,  $(1, \frac{\pi}{6})$  is equivalent to  $(-1, \frac{7\pi}{6})$ .

a. For each given polar coordinate, find two different polar coordinates that represent the given point.

$(r_1, \theta_1)$	$(2, \frac{\pi}{4})$	$(3, \frac{7\pi}{4})$	$(6, \frac{2\pi}{3})$	$(1, \frac{7\pi}{6})$	$(-2, \frac{5\pi}{4})$	$(\frac{3}{4}, \frac{17\pi}{6})$
$(r_2, \theta_2)$						
$(r_3, \theta_3)$						



**Polar Coordinates**  
**Student Activity**

Name \_\_\_\_\_

Class \_\_\_\_\_

- b. For each point given in polar coordinates below, determine the rectangular coordinates.

$(r, \theta)$	$\left(3, \frac{7\pi}{3}\right)$	$\left(1, \frac{\pi}{6}\right)$	$\left(-2, -\frac{4\pi}{3}\right)$	$\left(\sqrt{5}, -\frac{3\pi}{2}\right)$	$\left(-8, \frac{3\pi}{4}\right)$	$\left(\frac{13}{4}, -\frac{\pi}{3}\right)$
$x$						
$y$						

- c. For each point given in rectangular coordinates below, determine two representations in polar coordinates.

$(x, y)$	$(3, 4)$	$(-\sqrt{2}, 2)$	$(4, -7)$	$(-\sqrt{3}, -1)$	$(-5, 5)$	$(7, 24)$
$r_1$						
$\theta_1$						
$r_2$						
$\theta_2$						

**Problem 2 – Graphing Polar Functions**

3. Over the next two worksheet pages, carefully sketch a complete graph of each given polar equation. Create a table of values, search for patterns, and sketch the graph on the axes provided. Check your results on the handheld.

Note: Make sure the Graph Mode is set to Polar. Press mode and use the down/right arrows to move and change from function to polar form.



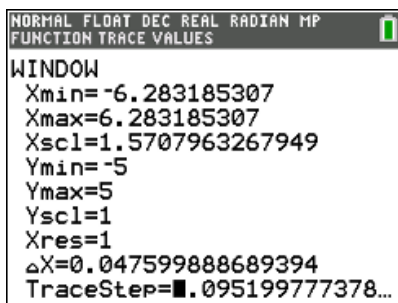




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### Problem 4 – Comparing Trigonometric Functions in the Polar and Rectangular Systems

In this problem, you will compare the four polar graphs from **Problem 3** with their rectangular system counterparts. Graph each of the following on the handheld (remember to change the graph mode back to function, clear the POLARGRD program, and set your window to the screen shot below) and answer each corresponding question.



4.  $f(x) = 4 \cos(x)$

- (a) What shape was created on the polar graph from question 3 (a)?
- (b) What connection can be made between the parts of the trigonometric function in the rectangular system as compared to the polar system? Pay close attention to the amplitude and period in the explanation.

5.  $f(x) = 2 + 2 \sin(x)$

- (a) What shape was created on the polar graph from question 3(b)?
- (b) What connection can be made between the parts of the trigonometric function in the rectangular system as compared to the polar system? Pay close attention to the amplitude, period, and vertical shift in the explanation.

6.  $f(x) = 4 \cos(3x)$

- (a) What shape was created on the polar graph from question 3(c)?
- (b) What connection can be made between the parts of the trigonometric function in the rectangular system as compared to the polar system? Pay close attention to the amplitude and period in the explanation.



**Polar Coordinates**  
**Student Activity**

Name \_\_\_\_\_

Class \_\_\_\_\_

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7.  $f(x) = 1 + 2 \cos(x)$

- (a) What Shape was created on the polar graph from question 3(d)?
  
- (b) What connection can be made between the parts of the trigonometric function in the rectangular system as compared to the polar system? Pay close attention to the amplitude and period in the explanation.