

## Math Concepts

- Number sense
- Data analysis


## Hello Dolly

## Materials <br> - TI-73 calculator <br> - TI-GRAPH LINK ${ }^{\text {TM }}$ (optional)

## In this activity, you will:

- Draw a model of a Punnett Square on the TI-73
- Discover all the possible combinations of genotypes
- Explore experimental and theoretical probability
- Generate data using experimental probability and the laws of heredity


## Introduction

You may have noticed that offspring often resemble their parents. Tall parents with black hair often have tall children with black hair. However, they do not look exactly alike. Over 100 years ago, Gregor Mendel, an Austrian monk, became interested in this problem of how parents pass on characteristics to their offspring. He began experimenting on pea plants, which led to some important discoveries about heredity. A few years later, Reginald C. Punnett, an English geneticist, developed a model called the Punnett Square to show the possible ways alleles can combine at fertilization.
Alleles are the different forms a gene may have for a trait. In the Punnett Square, dominant alleles are shown with capital letters and recessive alleles are shown with the same letter in lower case. Using a 2 by 2 square, letters representing the parent's alleles are placed on the outer sides of the large square. Letters inside the smaller squares show the possible allele combinations for their offspring. If one allele is dominant, the recessive allele will be masked in the offspring. If two alleles are the same, then the form is pure. Pure traits have both dominant alleles, or both recessive alleles.
A form of the trait that is a combination of dominant and recessive alleles is called a hybrid trait. The model on the next page shows the results of a cross between pure tall and pure short plants where $\mathbf{T}$ represents the dominant
alleles for tallness and $t$ represents the recessive alleles for shortness. The offspring are pure hybrid tall. The genotypes are shown in the cells of the Punnett Square below, while the effect of the indicated combinations is called the Phenotypes. For example, if the genotype is $\mathbf{T t}$, the phenotype will be tall.

Parent 1


## The Problem

In humans, free earlobes are a dominant trait over attached earlobes. Draw a Punnett square for each possible parent combination. Find the theoretical and experimental probability for the offspring.

## Activity

1. Working in groups, draw Punnett squares using the draw function on the TI-73 for all the possible parent combinations. Let $F$ represent free earlobes allele, which is the dominant trait, and A represent attached earlobes, which is the recessive allele.
2. Draw a 2 by 2 square.
a. With the Plots and $Y=$ functions turned off, and with the Mode in the default setting (as explained in the TI-73 Manual), set the window to $1^{\text {st }}$ quadrant by pressing ZOOM and select 4:Zquadrant1.
b. Press WINDOW and change Ymax to 6.2 so you will have a square window.
c. Press 2nd [FORMAT] and highlight AxesOff by moving the cursor over the word and pressing ENTER.
d. Press GRAPH to go to the graph screen.
e. To use the pen option from the DRAW menu to draw a 2 by 2 square, press DRAW and select 8:Pen.
f. In the graph screen, use the arrow keys to move to the coordinates $(1,1)$.
g. Press ENTER to start drawing.
h. Move horizontally using the arrow keys to coordinates (5, 1), being careful not to overshoot the point since you are leaving a trail.
i. Move vertically up to coordinates $(5,5)$.
j. Finish the square by moving to coordinates $(1,5)$ then back to the starting point of $(1,1)$.
k. Turn the pen off by pressing ENTER.
I. Now, go to the midpoint $(3,1)$ of the lower horizontal segment.
$\mathbf{m}$. Turn the pen back on by pressing ENTER, and then go to midpoint of the upper horizontal segment.
n. Go through same process to connect the midpoints of the vertical segments.

3. Each group of students should have members numbered 1 through 4 . The "Ones" should draw a Punnett Square that is pure dominant (FF, FF). The "Twos" should draw a Punnett Square that is pure recessive (AA, AA). The "Threes" should draw a Punnett Square that is pure hybrid (FF, AA). The "Fours" should draw one of their choice different than the other three. Use the text option from the Draw menu to label the models.
4. Position the cursor above the square to label the top side around coordinates (2, 5.7).
a. Text letters are about 5 pixels tall. A pixel will be one press of the arrow key. Make sure you are at least 6 pixels above the side of the square so that there is enough space for the text.
b. Press DRAW and select the 7:Text( option.
c. After you have moved to the correct position, press 2nd [TEXT], and highlight $F$.
d. Press ENTER, move the cursor down to Done, and then press ENTER to paste $F$ above the square.
e. Move right to the midpoint of the adjacent box and place another $F$ using the same technique as before.
f. On the left vertical side, type A and a second A underneath it. This is the model of the pure hybrid.
g. Complete the inside of the square.

* Answer questions 1 and 2 on student data sheet.


5. Save your drawing before you move on. This may be done with the TI-GRAPH LINK ${ }^{\text {TM }}$ or by saving it as a Pic.
a. To save as a Pic, from the Home screen (2nd [QUIT]), press DRAW $\square$ and select the 1:StorePic option by pressing ENTER.
b. Press the number that you want to use to name this Pic. Note that you may only use the numbers 1 , 2, or 3 and that the old Pic with the name (number) selected will be erased by the new one.
6. Working in pairs, use the coin toss function of the TI-73 to simulate the birth of 40 offspring to a pair of hybrid parents (FA, FA).
a. From the Home screen, press MATH $\square \square$.
b. Select the 6:coin( option.
c. Type the number 2 (to simulate tossing two coins).
d. Repeatedly press ENTER (tossing the two coins).

Which outcome is more likely when you toss a coin: a head or a tail? It is equally likely that a hybrid parent will pass a dominant or recessive allele to its offspring.
A head will be represented by a 1 on the coin toss simulation and will represent the dominant allele, whereas a tail (which we will call 0 ) will represent the recessive allele.

e. Press CLEAR to clean the Home screen. Press ENTER and this will represent the genotypes when sperm and egg join. A 1 means a dominant allele (free earlobes) is passed by one parent and a 0 means a recessive allele (attached earlobes) is passed by the other parent.

Q Record your data on Table 1 (question 3 on the student data sheet) initially using tally marks (XX Tally columns), and then record the frequencies (XX columns).

The example above represents FF, AA, and FA. Remember that $\{1,0\}$ and $\{0,1\}$ are the same combinations.

* Answer questions 4-10 on the student data sheet.

7. Generate a circle graph to compare the probabilities of each gene combination.
a. Create two lists in the List Editor, PAIR (for genotype) and FREQ (for the frequency). See the TI-73 manual for information on naming lists.
b. In the PAIR list, enter the 3 possible pairs. The first element in the pair list must be in quotes since this is a categorical list.
c. Enter the corresponding frequencies in the FREQ list from Table 1.

d. Turn all plots Off by pressing [2nd [PLOT] 4 ENTER.
e. Display the STAT PLOTS menu by pressing 2nd [PLOT].
f. Define Plot1 as a circle graph as shown below.
g. Display the plot by pressing GRAPH. Print one copy of your results if TI-GRAPH LINK ${ }^{\text {TM }}$ is available, or save this graph as a Pic.

8. Turn in your data.
a. To do this, let List 1 (L1) represent group 1's data, List 2 represent group 2's data, and so on. If there are more than six groups, the other groups will have to be named lists.
b. One person in each group should call out the frequencies for each outcome.
c. Record this information on Table 2 (question 11 on the student data sheet) and then add to get a total.
d. Create a list called TFREQ (total frequency).
e. Enter the class data into this list and create a $2^{\text {nd }}$ circle graph on Plot2. Make sure you turn off Plot1 before displaying Plot2.
f. Trace around this graph to verify the data.


Answer questions 12-13 on the student data sheet.
9. Create a third statistical plot (pictograph) for either the group or the class data. Use the following STAT PLOTS selections. The scale tells the calculator the quantity represented by each icon. However, the calculator displays no more than seven icons for each category. So you will need to set the scale according to the greatest frequency.

10. Press GRAPH TRACE and discuss.


## Going Further

1. A family consisted of the mother, father and two children. The mother had attached earlobes and the father had free earlobes. One child had attached and the other had free. Explain how this is possible.
2. Using the TFREQ list, and using the fact that the free earlobe allele is dominant, calculate the percent of the offspring that would have the free earlobes phenotype.
3. Given the following data from a class in Dallas, create a graph representing the genotype distributions.

| Genotype | Frequency |
| :---: | :---: |
| MM | 117 |
| MN | 221 |
| NN | 101 |

4. Create two different Punnett Squares that would create a person with the NN genotype from the above Dallas data.

## Student Data Collection and Analysis Sheet

Name(s) $\qquad$
Date $\qquad$

## Activity 4

## Hello Dolly

1. For each cross between two parents, what is the probability of the offspring receiving any one of the four combinations?
$\qquad$
2. Draw and label all possible Punnett Squares showing combinations of parents and offspring.
3. Complete Table 1.

Table 1

| Genotypes | FF Tally | FF | AA Tally | AA | FA Tally | FA | Total Trials |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Total |  |  |  |  |  |  | 40 |
| Class Total |  |  |  |  |  |  |  |

4. Of the 40 offspring in your sample, how many were pure dominant (FF)?
$\qquad$
5. How many out of the 40 did you expect to be pure dominant? $\qquad$
6. Which of the three gene combinations occurred the most?
7. What is the theoretical probability (what is supposed to happen) of an offspring having pure dominant genes? $\qquad$

What is the theoretical probability of an offspring having hybrid genes?

What is the theoretical probability of an offspring having pure recessive genes? $\qquad$
8. Which gene combination did you expect to occur the most and why?
$\qquad$
$\qquad$
9. Find the experimental probability (from your experiment) of an offspring having pure dominant genes. $\qquad$
Find the experimental probability (from your experiment) of an offspring having hybrid genes. $\qquad$
Find the experimental probability (from your experiment) of an offspring having pure recessive genes.
10. Describe how these results compare to the theoretical probability. $\qquad$
11. Complete Table 2 below.

Table 2

| Genotype | Group1 | Group2 | Group3 | Group4 | Group5 | Group 6 | Tally |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | L 1 | L 2 | L 3 | $\mathrm{L4}$ | $\mathrm{L5}$ | $\mathrm{L6}$ | LTFREQ |
| FF |  |  |  |  |  |  |  |
| AA |  |  |  |  |  |  |  |
| FA |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |

12. Find the experimental probability (using the whole class data) of an offspring having pure dominant genes. $\qquad$
Find the experimental probability (using the whole class data) of an offspring having hybrid genes. $\qquad$
Find the experimental probability (using the whole class data) of an offspring having pure recessive genes.
13. How do these results compare to the theoretical probability?

## Teacher Notes

## Math Strands: Number Sense, and Data Analysis

Students will draw a model of a Punnett Square on the TI-73 and discover all of the possible combinations of Genotypes. Experimental and theoretical probability will be explored.

## Science Strands: Life Science

Collecting data through experimental probability and using the laws of heredity.

## Classroom Management and Safety

Place students in groups of four. A printout of all possible combinations of the model Punnett Square combinations can be done using TI-GRAPH LINK ${ }^{\text {TM }}$ if the classroom is equipped.

## Activity

1. The setting on page 2 for the WINDOW is required to give "nice" values to draw on. They have $\mathbf{X}$-values as a multiple of 94 and $\mathbf{Y}$-values as a multiple of 62 .
2. If the students mess up on the drawing of the Punnett Square, they can start again by selecting the ClrDraw option from the Draw menu or the Catalog and pressing ENTER.
3. When placing the text, the screen is set so that a pixel is 0.1 in value since $\Delta \mathbf{X}$ and $\Delta \mathbf{Y}$ are equal to 0.1 . But with the Text mode you don't see the coordinates, so the students should just count up from the line of the square. One press of the arrow key is one pixel ( 0.1 in value).
4. Students will need to leave the Text placement mode before they save or transfer their drawing of the square so that they don't mess it up with the commands appearing on the screen. If this happens they may "clean up" the screen using the Pt-Off( options from the Draw/Points menu.
5. Explain to the students that ( $\mathrm{FF}, \mathrm{AA}$ ) is the same combination as (AA, FF ). Likewise FA is the same as AF. However, the dominant trait/allele should be listed first. In a combination, the order does not matter. Survey the "Fours" in each group to get their parent combinations and have them display the other three possibilities which are: (FA, FA), (FA, AA), (FF, FA). There are a total of 6 possible parent combinations that could be calculated by taking a combination of 4 traits 2 at a time.
$\mathrm{C}(4,2)=(4 * 3) /(2 * 1)$. This combination can also be calculated on the TI-73 by typing 4 , then (MATH $\square \square$ to the PRB menu. Then select $4: n \mathrm{Cr}$ and type 2 ENTER.
6. To collect the class data, you may try this procedure. You (not the students) enter the group totals of each outcome on a viewscreen calculator and tell the students to record the data on their table.
7. To the right of the list named Pair, insert List 1 (L1). Ask a member of group 1 to give the frequencies in this order (same as on table) FF, AA, FA. Insert List 2 to the right of List 1 if it is not already there. Ask a member of group 2 to give their group frequencies as above. Continue doing this, using lists 3-6 until all groups have been collected. If there are more than 6 groups, the remaining groups could be named GRP7, GRP8, and so forth. After all of the groups data has been entered into the lists, name a list TFREQ for total frequencies. Enter the formula L1+ L2+ L3+ L4+... to get the total frequencies of each outcome for the entire class. The students will need this named list (TFREQ) to enter the data after you have the totals, which can be sent through the data link cable. (See the TI-73 manual for information on linking between calculators.)
8. You can discuss how a small sample compared to the larger sample.
9. Additional information can be found on the Internet at various locations including: http://www.netspace.org/MendelWeb/ and from Access Excellence ${ }^{\circledR}$ at http://www.gene.com/ae/.
10. Topics such as sickle-cell anemia and the Human Genome Project (http://www.ornl.gov/TechResources/Human_Genome/home.html) would be good extensions or lead-ins for this investigation.

## Student Data Collection and Analysis Sheet - Key

1. 1 out of 4 .
2. Drawings.
3. Answers will vary, but check totals.
4. From Table 1.
5. $1 / 4$ of 40 , or 10 .
6. FA.
7. $1 / 2,1 / 4,1 / 2$.
8. FA, because the probability of this outcome is $1 / 2$, whereas the other two outcomes each just have a probability of $1 / 4$.
9. From Table 1.
10. Answers will vary, but the data should be similar.
11. Table 2.
12. See Table 2.
13. Again answers will vary, but now they should be closer to the theoretical.

## Going Further - Key

1. The father has a genotype of FA and the mother has AA.
2. $\frac{F F+F A}{F F+F A+A A} * 100$
3. 


4. NN by NN and NN by MN squares.

