

Arithmetic Sequences

Student Worksheet

7 8 9 10 11 12



TI-30XPlus
MathPrint™



Worksheet



Student



45 min

Dining Table

The world's longest dining table measured 3,189.83m. The table was used to serve the evening meal to 7000 Muslims at the end of Ramadan. The images below show the configuration of seats around a collection of rectangular dining tables in a typical restaurant.



Question: 1.

- Assuming the pattern continues, how many people could be seated at the fourth configuration?
- Explain why the number of seats at successive configurations forms an arithmetic sequence.
- How many people could be seated at the 10th configuration?
- The world record breaking dining table was set out similar to the pattern shown above, determine the approximate space (width) available to each person. (Show your calculations)

There are four ways you can generate these types of sequences on your calculator:

- Recursion (home screen)
- Sequence command (Lists)
- Formulas (memory allocations)
- Functions (efficient use of formulas and memory allocations)

Using your calculator - Recursion

The first term in the dining table sequence is 4, entering this value may seem trivial but is required to initiate the recursion process.

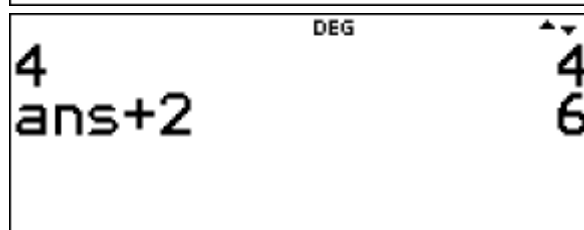


The value '4' is now stored as the answer (ANS); this is the value that will change with each calculation.

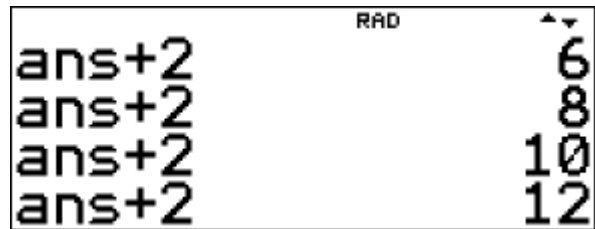
Now type the following:



Notice that the abbreviation 'ans' automatically appears. This represents the configuration for the second table. The value stored in 'ans' is now updated to 6.



Continue pressing **enter** and counting, the screen shown opposite shows this calculation in progress; the most recent calculation is for the number of seats at the 5th table.



Keep counting and pressing **enter** until you reach the configuration for the 10th table.

Using your calculator - Sequence

The recursion approach is quick and easy; however, you have to count carefully!

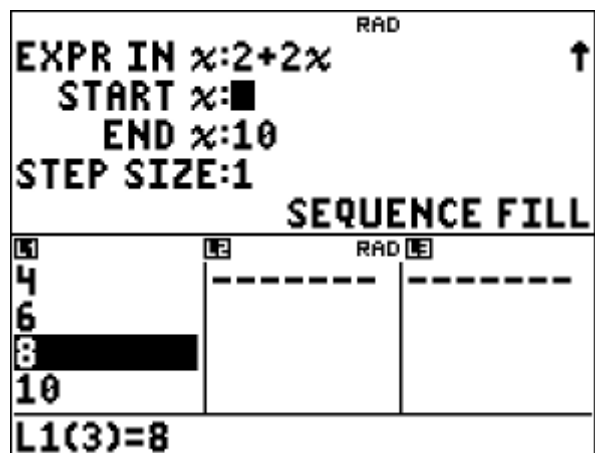
The sequence command can generate the entire sequence and store it in a list. To navigate to the sequence command press:



From here you can select where you want to store the sequence. Navigate to your preferred list, then press:



Enter the formula shown opposite: $2x + 2$.



Start the sequence at $x = 1$ and end with $x = 10$ with a step size of 1, then select: Sequence Fill.

The screen shown opposite has $L1(3) = 8$ highlighted.

The 3 represents the term number in the sequence (table configuration) and the 8 represents the term (quantity of seats), scroll down to see the remaining values.

Using your calculator - Formulas

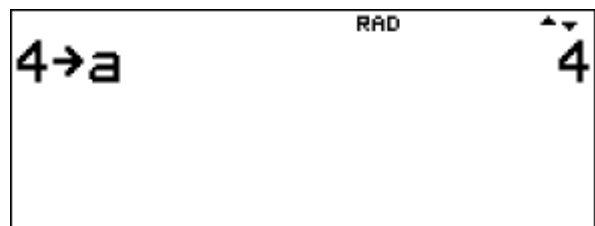
The n^{th} term of an arithmetic sequence can be computed using the formula:

$$a_n = a_1 + (n - 1)d$$

$$a_n = n^{\text{th}} \text{ term} \qquad a_1 = \text{first term}$$

$$n = \text{term number} \qquad d = \text{common difference}$$

In the dining table problem, the first term is 4 (number of seats at the first table), this value can be stored in 'a' on the calculator.



Note: The variable key is a multi-tap key.

Type in the following:



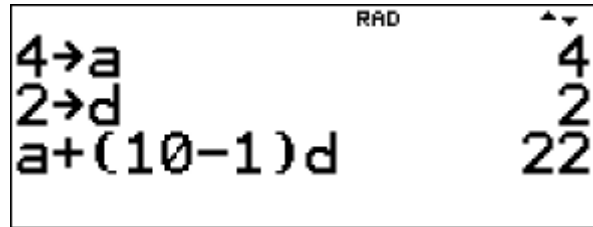
The next value to store is the common difference $d = 2$.

Type in the following:



Suppose you want to calculate the 10th term of the sequence, just enter the formula and use '10' for 'n'.

The advantage of this method is that you can simply recall the previous calculation and change the 10 for another term number. Alternatively, if the first term changes, define a new value for 'a' and then recall the expression and the new term will be recalculated.



Using your calculator - Functions

This approach uses the formula but has an additional advantage, it is even more convenient! Press:



The function editor allows us to define a rule, $f(x)$ has been selected.

Enter the formula as before, but this time use 'x' for the term number, then press enter to lock in the function for $f(x)$, and again to lock in the function for $g(x)$.*

* $g(x)$ could be used for the 'sum' of an arithmetic sequence!

The Table set up can automatically generate a table of values or prompt for any value of x . Match the selections shown opposite and then navigate and accept calculate (calc).

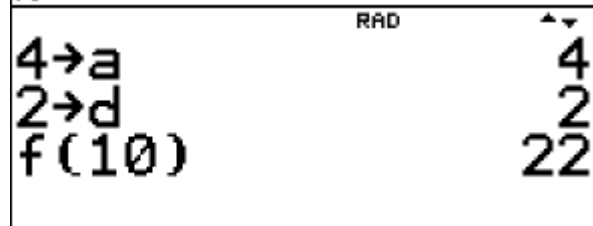
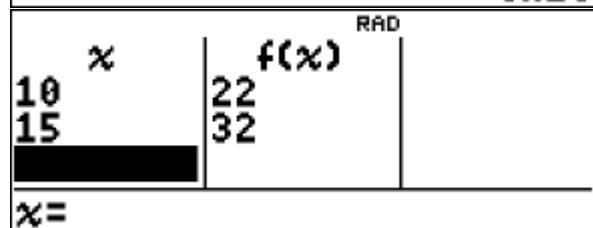
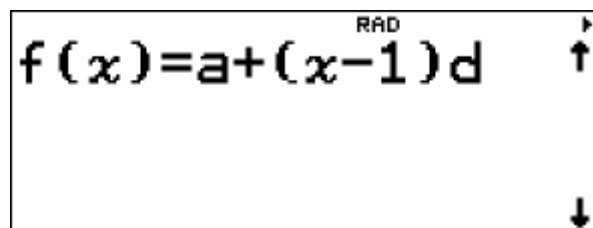
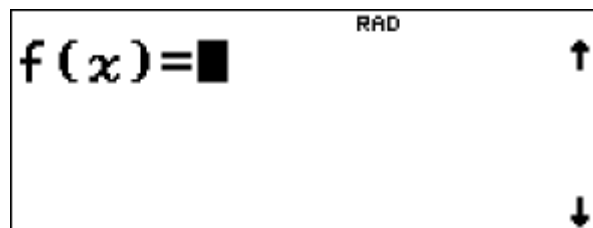
Enter the term number(s) you want to compute and the term will automatically be completed using the stored values for 'a' and 'd'. The table automatically updates when the stored values are changed.

Functions can also be recalled from the home screen.

To access the function, press:



Enter the term number to be calculated and press enter.



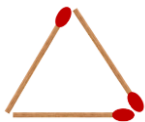
Question: 2.

A restaurant has multiple table bookings and configurations. For each of the following configurations in the restaurant, determine the total number of people that can be seated.

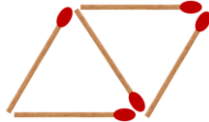
- i) Craig's restaurant has 6 tables set up as the following configurations: 2, 2, 3, 4, 5 and 5. How many people can be seated in total?

Hint: Use the sequence command and generate a list starting at 1 and ending at 6.

- ii) Hayley runs a wedding venue and has 8 tables set up with the following configurations: 6, 6, 7, 7, 8, 8, 9 and 9. How many guests can be seated in total?

Match Stick Patterns

Pattern 1



Pattern 2



Pattern 3

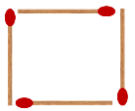


Pattern 4

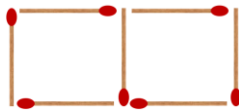
Question: 3.

Matchsticks can be used to form all sorts of patterns. A single box of matches contains precisely 50 matches. The following questions relate to the (above) pattern.

- How many matches in the first pattern?
- How many matches are required for each additional pattern?
- Generate the sequence using a list to help determine quantity of triangles formed using the above pattern, from a single box of matches.
- Cameron has created 99 triangles. How many boxes of matches did he use?



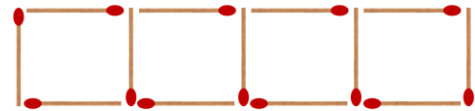
Pattern 1



Pattern 2



Pattern 3



Pattern 4

Question: 4.

A series of squares is formed using matchsticks. Using the pattern above:

- How many matches in the first pattern?
- How many matches are required for each additional pattern?
- Generate the table feature to help determine quantity of squares formed using the above pattern, from a single box of matches.