

Exploring Space Through MATH

Applications in Algebra 1



STUDENT
EDITION

Space Shuttle Ascent – Mass vs. Time

Background

This problem is part of a series that applies algebraic principles in NASA's human spaceflight.

The Space Shuttle Mission Control Center (MCC) and the International Space Station (ISS) Control Center use some of the most sophisticated technology and communication equipment in the world. Teams of highly qualified engineers, scientists, doctors, and technicians, known as flight controllers, monitor the systems and activities aboard the space shuttle and the ISS. They work together as a powerful team, spending many hours performing critical simulations as they prepare to support each mission and crew during normal operations and any unexpected events.

Since its first flight in 1981, the space shuttle has been used to extend research, repair satellites, and help with building the ISS. NASA plans to retire the space shuttle but, space exploration has made major advances due to the success of space shuttle missions. Critical to any space shuttle mission is the ascent into space.

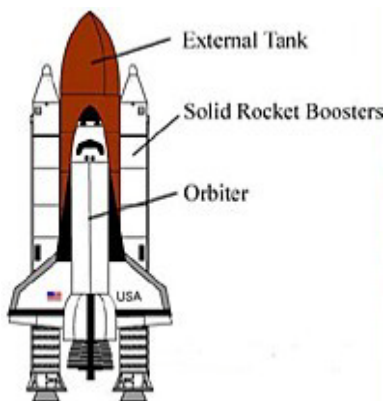


Figure 1: Main components of the space shuttle



Figure 2: Space Shuttle Discovery at liftoff

The ascent phase begins at liftoff and ends when the space shuttle reaches Earth's orbit. The space shuttle must accelerate from zero to approximately 7,850 meters per second (which is approximately 17,500 miles per hour) in eight and a half minutes to reach the minimum altitude required to orbit Earth. It takes a very unique vehicle to accomplish this task.

There are three main components of the space shuttle that enable the launch into orbit (Figure 1). The main component is the orbiter. It not only serves as the crew's home in space and is equipped to dock with the ISS, but it also contains maneuvering engines for finalizing the orbital trajectory, or flight path.



The External Tank (ET), the largest component of the space shuttle, supplies the propellant (liquid oxygen and liquid hydrogen) to the Space Shuttle Main Engines (SSMEs) which are liquid propellant rocket engines. The third component is a pair of Solid Rocket Boosters (SRBs) which are reusable. They are attached to the sides of the ET and provide the main thrust at launch (Figure 2).

One of the flight controllers in the Space Shuttle Mission Control Center is the Booster Engineer. This position, or console, known as Booster, is in charge of monitoring the SSMEs, the SRBs, and the ET during the countdown and the ascent phase, until all of those systems are safe. The components of the space shuttle experience changes in position, velocity, and acceleration during the ascent into space. These changes can be seen by taking a closer look at the entire ascent process (Figure 3).

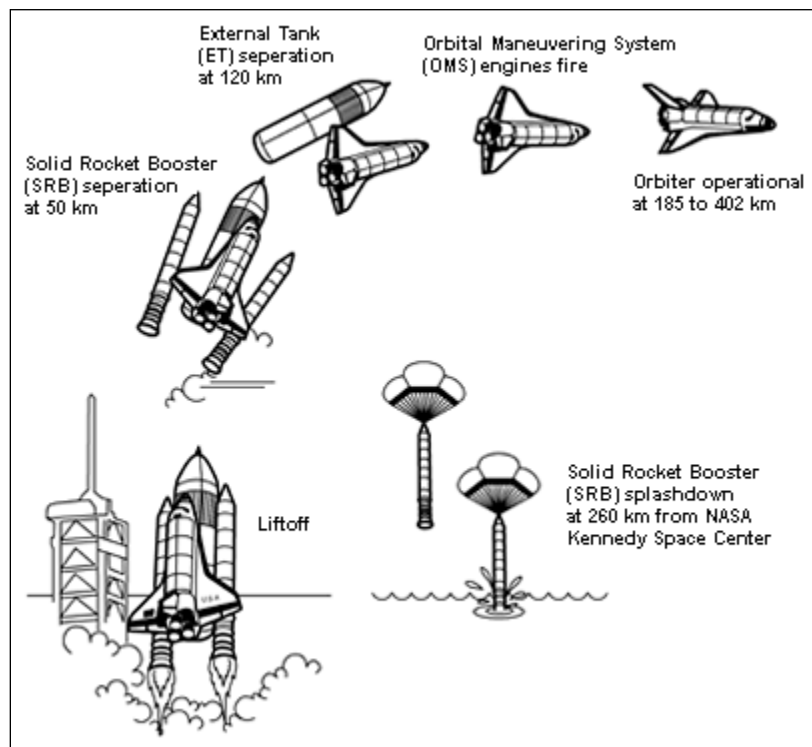


Figure 3: Space shuttle ascent process

The ascent process begins with the liftoff from the launch pad. Propellant burns from the SRBs and the ET causing the space shuttle to accelerate very quickly. This high-rate of acceleration causes a rapid increase in dynamic pressure, known as Q in aeronautics (sometimes called velocity pressure). As the space shuttle breaks the sound barrier, its structure can only withstand a certain level of dynamic pressure before it suffers damage. Before this critical level is reached, the engines of the space shuttle are throttled down to about 67% of full power to avoid damage. About 50 seconds after liftoff, the dynamic pressure reaches its maximum aerodynamic load (Max Q). The air density then drops rapidly due to the thinning atmosphere, and the space shuttle can be throttled to full power without fear of structural damage. The command is given, "Go at throttle up!"

As the space shuttle climbs, the velocity is increasing and the density of the air is decreasing. About 2 minutes after liftoff the atmosphere is so thin that the dynamic pressure drops to near zero. The SRBs, having used their propellant, are commanded by the space shuttle's onboard computer to separate from the ET. The jettisoning of these booster rockets marks the end of the first ascent stage and the beginning of the second. The spent SRBs fall into the ocean and are recovered, refurbished, reloaded with propellant, and reused for several missions. The second stage of ascent lasts about six and a half



minutes, during which time the Booster flight controller continues to monitor the ET and the SSMEs until MECO (Main Engine Cut Off) and ET Separation. The ET re-enters the Earth's atmosphere, breaking up before impact in the ocean, and the space shuttle maneuvers into orbit. This lesson focuses on the first ascent stage, which occurs during the first two minutes after liftoff.

Instructional Objectives

- You will create scatter plots from a data table.
- You will determine the correlation of the data and interpret its meaning.
- You will find linear regression equations.
- You will find the slope and y -intercept of a linear equation.
- You will communicate the meanings of slope and y -intercept as they relate to a real-world problem.

View the video, *Space Shuttle Ascent-Clip_ STS-121*, and reference the Background section to answer questions 1-9.

1. In the launch of the Space Shuttle Discovery what does “auto sequence start” mean?
2. What are the 3 main components of the space shuttle?
3. Which component is the first to ignite? Which component ignites next and what is the result?
4. At about 40 seconds after launch, due to the velocity of Discovery, what occurs?
5. About how many seconds after liftoff do the main engines throttle back to about 67% of rated performance to reduce the structural stress that occurs as the space shuttle breaks the sound barrier?
6. “Discovery Houston, Go at throttle up!” is the command given when the atmosphere is so thin that there is no danger of structural damage due to dynamic pressure. About how many seconds after liftoff does this occur?
7. What occurs at approximately 2 minutes into flight?
8. What happens to the depleted SRBs?
9. What powers Discovery after SRB separation?



Problem

On July 4, 2006, Space Shuttle Discovery was launched from Kennedy Space Center on mission STS-121 to begin a rendezvous with the International Space Station, or ISS. Before each mission, the projected data is compiled to assist in the launch of the space shuttle and to ensure safety and success during the ascent. To complete this data flight design specialists take into consideration a multitude of factors, such as space shuttle mass, propellant used, mass of payload being carried to space and mass of payload returning. They must also factor in atmospheric density, which is changing throughout the year. After running multiple tests, information is compiled in a table showing exactly what should happen each second of the ascent.

Table 1: STS-121 Discovery Ascent data (total mass)

Time (s)	Space Shuttle Total Mass (kg)
0	2,051,113
10	1,935,155
20	1,799,290
30	1,681,120
40	1,567,611
50	1,475,282
60	1,376,301
70	1,277,921
80	1,177,704
90	1,075,683
100	991,872
110	913,254
120	880,377

Table 1 shows the total mass of Discovery for mission STS-121 every 10 seconds from liftoff to SRB separation. Total mass includes the orbiter, SRBs, ET, propellant, and payload. It is during the first stage of the ascent, that the space shuttle is burning the greatest amount of propellant. You can see in the table that the space shuttle has a total mass of 2,051,113 kg at $t = 0$. After 2 minutes its total mass is only 880,377 kg, or 43 % of the original mass. The burning of this vast amount of propellant is needed to get the space shuttle through Earth's atmosphere and into orbit.

10. What happens to the mass as time progresses?
11. If this data were to be graphed with time on the x -axis and mass on the y -axis, which of the following would be characteristic of the graph?
- The graph slopes down and the y -intercept is negative
 - The graph slopes down and the y -intercept is positive
 - The graph slopes up and the y -intercept is negative
 - The graph slopes up and the y -intercept is positive



On your TI-Nspire Handheld open the file titled, *NASA_Shuttle_Ascent-Mass_Time*. Read the directions and review the data on pages 1.1-1.4 embedded in the Nspire document. Create a scatter plot of the mass of the space shuttle vs. time on Nspire page 1.5 and model the data using linear regression. Answer questions 12-17 (found on Nspire pages 1.6 - 2.3) in your group. Discuss answers to be sure everyone understands and agrees on the solutions.

12. Does the line fit the data? Explain
13. What is the correlation of the data?
14. How much propellant does Discovery burn per second? Explain what this represents with regard to the equation.
15. What is the y -intercept of the equation of the line that models the mass versus time data? Explain what this represents in relation to the space shuttle.
16. To gain perspective regarding the magnitude of the propellant consumption of the space shuttle, find the approximate number of each type of object that it would take to equal the mass of the entire space shuttle system at launch. Round to the nearest whole number.

Table 2: Mass of various Objects (also located on Nspire page 2.2)

Object	Approximate mass (kg)	Approximate number of objects to equal the mass of the space shuttle at launch
Statue of Liberty	204,117	
Boeing 747 airplane	158,757	
Fuel tank truck	27,216	
School bus	11,340	

17. A Boeing 767 airplane burns about 24,500 kg of fuel on a 6 hour flight from New York to Los Angeles. Approximately how much time would it take the space shuttle to burn an equivalent amount of propellant?



Table 3 is on page 3.2 in the TI-Nspire document. Complete the scatterplot on page 3.4 using your TI-Nspire handheld and answer questions 18-22 (found on Nspire pages 3.5 – 3.9).

On May 12, 2009, Space Shuttle Atlantis launched from Kennedy Space Center on mission STS-125 to repair the Hubble Space Telescope. Astronauts installed two new instruments, repaired two inactive ones, and performed the component replacements to keep the telescope functioning into at least 2014. Table 3 shows the total mass of Atlantis for mission STS-125 every 10 seconds from liftoff to SRB separation.

Table 3: STS-125 Atlantis Ascent data (total mass)

Time (s)	Space Shuttle Total Mass (kg)
0	2,049,780
10	1,932,475
20	1,795,086
30	1,676,053
40	1,562,508
50	1,468,886
60	1,374,449
70	1,264,663
80	1,163,639
90	1,061,679
100	978,131
110	902,427
120	874,457

18. Does the data appear to be linear? Explain.
19. What is the correlation of the data? (positive, negative, constant, or no correlation)?
20. What is the slope of your equation? Explain what this represents in relation to the space shuttle.
21. What is the y -intercept of the equation of your line that models the mass versus time data? Explain what this means in relation to the space shuttle.
22. Compare the rate of burn of propellant (slope) for missions STS-121 (Discovery) and STS-125 (Atlantis). Which space shuttle has the fastest burn rate and what might be the reason.