## Activity Overview

In this activity, students will measure interior and exterior angles of a triangle and make conjectures about their relationships.

## Topic: Triangles \& Congruence

- Use inductive reasoning to conjecture a theorem about the total measures of a triangle's interior angles.
- Prove that the sum of the measures of the interior angles of a triangle is $180^{\circ}$.
- Prove that the sum of the measures of the exterior angles of a triangle is $360^{\circ}$.


## Teacher Preparation and Notes

- This activity is designed to be used in a high school or middle school geometry classroom.
- The sum of the measures of the three interior angles of a triangle is $180^{\circ}$.
- The sum of the measures of the two remote interior angles of a triangle is equal to the measure of the exterior angle.
- An exterior angle is supplementary to its adjacent interior angle.
- The sum of the measures of three exterior angles of a triangle is $360^{\circ}$.
- This activity is designed to be student-centered with the teacher acting as a facilitator while students work cooperatively. Use the following pages as a framework as to how the activity will progress.
- Notes for using the TI-Nspire ${ }^{\text {TM }}$ Navigator ${ }^{\text {TM }}$ System are included throughout the activity. The use of TI-Navigator is not needed for completing this activity.
- To download the student TI-Nspire document (.tns file) and student worksheet, go to education.ti.com/exchange and enter "8771" in the quick search box.


## Associated Materials

- IntExtAngles_Student.doc
- IntExtAngles.tns


## Suggested Related Activities

To download any activity listed, go to education.ti.com/exchange and enter the number in the quick search box.

- Transversals (TI-Nspire technology) - 10991
- Angles in Polygons (TI-Nspire technology) - 9055
- Remote Interior Angles (TI-Nspire technology) - 10230


## Problem 1 - Interior angles of a triangle

On page 1.3, students will construct a triangle (MENU > Shapes > Triangle) and label the vertices $A, B$, and $C$.

Note: If the vertices are not labeled at the same time that they are created, they may be labeled using the Text tool (MENU > Actions > Text).

Students should measure the three interior angles of the triangle using the Angle tool (MENU > Measurement > Angle).
Note: To measure an angle, press (or enter) three times to select the vertices of the angle and then press (or enter) again to anchor the measurement.

This data should be recorded in the first row of the chart on the student worksheet.

Students should then drag a vertex of the triangle to change the angle measures. Have them try to create different types of triangles (acute, obtuse, right). After recording two more sets of data in the chart on their worksheet, students should make a conjecture about the three interior angles.

Instruct students to use the Text tool to display the expression $A+B+C$ on the screen.

Then have them use the Calculate tool (MENU > Actions > Calculate) to find the sum of the three interior angles of the triangle.

Next, have them drag a vertex and observe the results. Ask: Do the results support your conjecture?


## TI-Nspire Navigator Opportunity: Screen Capture

See Note 1 at the end of this lesson.

## Problem 2 - One exterior angle of a triangle

On page 2.2, students will construct a line through the two lower vertices of the triangle ( $A$ and $C$ ) using the Line tool (MENU > Points \& Lines > Line).

Note: To be certain that the line passes through a vertex, make sure the vertex point is flashing before pressing (or enter).

Have students create a new point on the line to the right of the triangle using the Point On tool. Label it $D$.

Direct students to measure the exterior angle $\angle B C D$ using the Angle tool, and record this measure, along with the measures of the interior angles, in the chart on the student worksheet.

Next, students should drag a vertex of the triangle to change the angle measures, and add two more sets of data to the chart.

Students should make some observations about the exterior angle and its relationship to the other angles displayed in the chart.

Have them make calculations as needed to test their conjectures. If desired, prompt students to calculate the sums of pairs of angles in the chart.

Once again, students should drag a vertex and observe the results. Ask: Do the results support your conjectures?


## TI-Nspire Navigator Opportunity: Quick Poll

See Note 2 at the end of this lesson.

Advance to page 2.4 where the construction is replicated. The Lists \& Spreadsheet application on page 2.5 is set up to capture the angle measurements displayed on page 2.4.
On page 2.5, have students press © ©tri) $+\odot$ to capture and view the first set of data.

Returning to page 2.4, tell students to drag a vertex of the triangle to change the angle measures, and press (atr) $+\varnothing$ to capture another set of data.

They should continue dragging a vertex and pressing @tri) +. until they have collected at least five data sets. (There is no need for students to return to page 2.5 during this process.)

On page 2.5, students will inspect the collected data. The formula in Column E calculates the sum of the two remote interior angles ( $\angle A B C$ and $\angle C A B$ ). Press (Atr) $+\mathbf{R}$ to execute the formula. Ask students to compare the resulting values to those in other columns of the spreadsheet. They should observe that Columns D and E contain the same values.

The formula in Column $F$ finds the sum of the exterior angle and its adjacent interior angle ( $\angle B C D$ and $\angle B C A$ ). Ask: How can this result be interpreted? (The angles are supplementary.)


## Problem 3 - Three exterior angles of a triangle

On page 3.2, students will construct a ray (MENU > Points \& Lines > Ray) from point $A$ through point $B$ as shown.

Next, they should measure one exterior angle at each vertex.

Note: It is not necessary to create an additional point on the line before measuring the angle.

Have them record the measures of the three exterior angles into the chart on the student worksheet.

Then they can drag a vertex of the triangle and record more data into the chart.

Instruct students to make a conjecture about the three exterior angles.
Then have them calculate the sum of the three exterior angles.
Tell students to drag a vertex and observe the results. Ask: Do the results support your conjectures?


TI-Nspire Navigator Opportunity: Screen Capture or Live Presenter
See Note 3 at the end of this lesson.

## Additional Problems

Ask students to find the missing angle measures in each of the diagrams below.
1.

3.

4.


Solutions

1. $\angle B=59^{\circ}, \angle B C D=140^{\circ}$
2. $\angle B=44^{\circ}, \angle B C A=109^{\circ}$
3. $\angle B C A=81^{\circ}$, int $\angle A=42^{\circ}$, ext $\angle A=138^{\circ}$
4. $\angle B C A=93^{\circ}$, ext $\angle A=150^{\circ}, \angle A B C=57^{\circ}$, ext $\angle B=123^{\circ}$

## TI-Nspire Navigator Opportunities

## Note 1

## Problem 1, Screen Capture

Use Screen Capture to ensure that students all selected the correct Text box and variables for their calculation. This will ensure they are able to see the correct sum of the interior angles.

## Note 2

Problem 2, Quick Poll
Ask students to submit the sum of $\angle A B C$ and $\angle C A B$ and the exterior angle measurement. All students should enter the same two numbers. Otherwise, they have made a mistake in their construction.

## Note 3

Problem 3, Screen Capture or Live Presenter
As the class is discussing the results of the sum of the exterior angles, have different students move vertices around in the construction. This will show that regardless of the shape of the construction, the exterior angles always sum to $360^{\circ}$.

