

Student Activity

Name _____

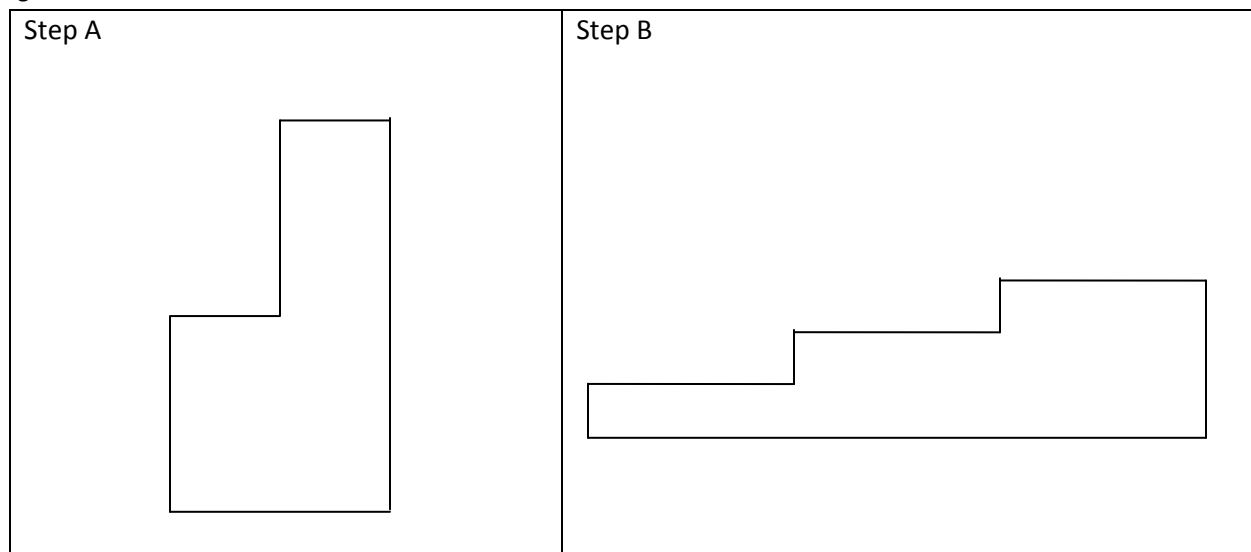
Date _____

Slope: One Step at a Time (Day 1)

Objective: In this activity, you will explore the concept of slope by exploring the steepness of different staircases and graphing these on the TI-73 calculator.

To build staircases that are easy to climb, carpenters take into consideration the vertical distance and the horizontal distance (tread) of each step.

Figure 1



1. Which staircase would be steeper to climb? Explain why?

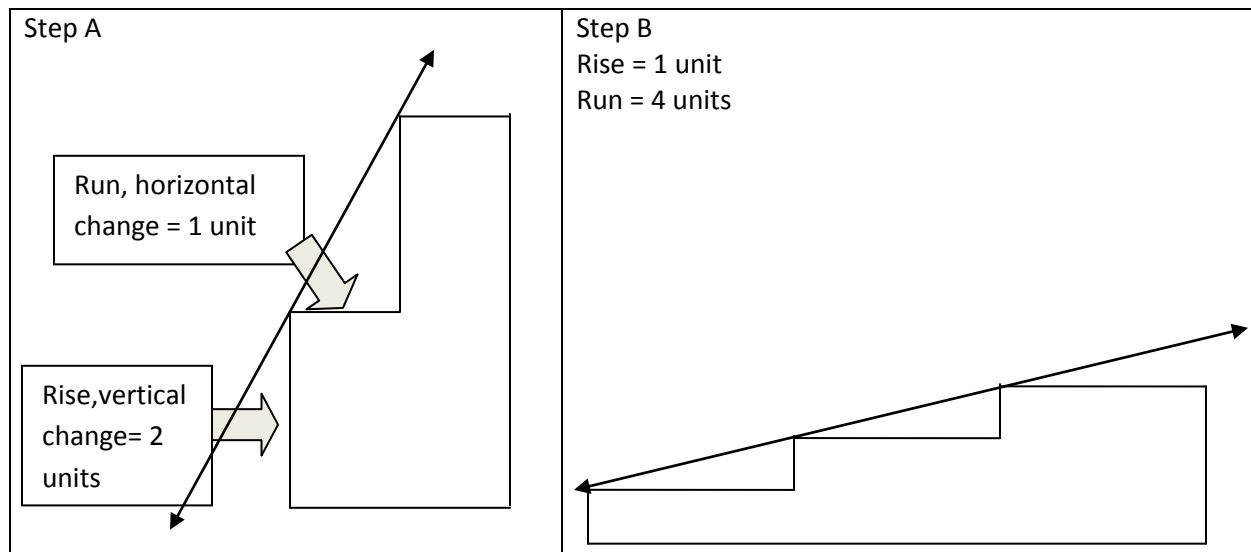
2. Measure the vertical distance and horizontal distance of a step on 2 different staircases before class tomorrow. In the table, enter the lengths in inches to the nearest one-fourth inch

Staircase	Vertical Distance	Horizontal Distance
1		
2		

Slope: One Step at a Time (Day 2)

To build staircases that are easy to climb, carpenters take into consideration the vertical distance and the horizontal distance (tread) of each step. The ratio of the rise to the run provides a measure of the steepness of the staircase. See Figure 2.

Figure 2



For Step A the ratio of the rise to the run is $2/1$ or 2.

For Step B the ratio of the rise to the run is $1/4$ or .25

3. What do you notice about the ratios for Step A and Step B in relation to the steepness of the stairs?

Answers may include:

4. Using your TI-73 Explorer Calculator, determine the ratio of the rise to the run for each of the staircases you brought measurements for.

Staircase 1:

Staircase 2:

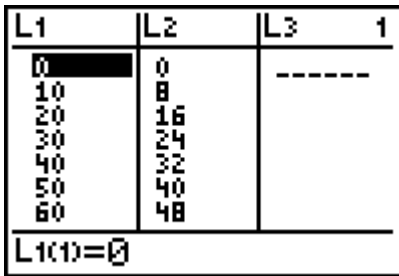

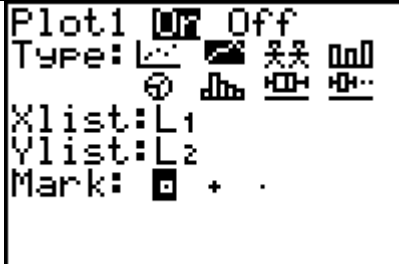
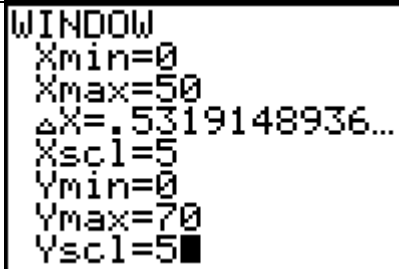
5. Which staircase was steeper based upon the ratios. Why?

Carpenters build steps with a ratio of the rise to the run between 0.45 and 0.60. Did your steps fall within this range?

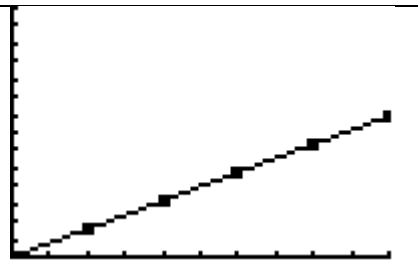
Look at Figure 1, Step A and Step B. A line has been drawn on each staircase that touches each step. The steepness of this line is also the slope of the line as it represents the vertical change/horizontal change.

$$\text{Slope} = \frac{\text{Vertical change}}{\text{Horizontal change}}$$

Next, we will use the TI-73 calculator to set up a table of coordinates and to graph the line that would touch each of the steps in your staircases.

<p>1. Clear the Home screen and press 2nd MEM ClrAllLists. Press ENTER then CLEAR.</p>																																	
<p>2. Press LIST</p> <p>Enter coordinates for your first stair case. Move to L1 and enter the x-coordinates in order, pressing ENTER after each entry.</p> <p>Move to L2 and do the same for the y-coordinates. An example for a staircase with a rise of 8 and a run of 10 is to the right.</p> <p>Tip: You must have the coordinates matched in L1 and L2. Otherwise your graph will not run correctly.</p>	 <table border="1" data-bbox="1029 667 1425 898"> <thead> <tr> <th>L1</th> <th>L2</th> <th>L3</th> <th>1</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>-----</td> <td></td> </tr> <tr> <td>10</td> <td>8</td> <td></td> <td></td> </tr> <tr> <td>20</td> <td>16</td> <td></td> <td></td> </tr> <tr> <td>30</td> <td>24</td> <td></td> <td></td> </tr> <tr> <td>40</td> <td>32</td> <td></td> <td></td> </tr> <tr> <td>50</td> <td>40</td> <td></td> <td></td> </tr> <tr> <td>60</td> <td>48</td> <td></td> <td></td> </tr> </tbody> </table> <p>L1(1)=0</p>	L1	L2	L3	1	0	0	-----		10	8			20	16			30	24			40	32			50	40			60	48		
L1	L2	L3	1																														
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10	8																																
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40	32																																
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60	48																																
<p>3. To graph the line, press 2nd [PLOT] and see if Plots 2 and 3 are off. If not, select 4:PlotsOff and press ENTER.</p>	 <pre> STAT PLOTS 1:Plot1...Off L1 L2 2:Plot2...Off L3 L4 3:Plot3...Off L1 L2 4↓PlotsOff </pre>																																
<p>4. Select On and press ENTER. Press ↓ to move to Type, use the arrow keys to choose the connected line graph, and press ENTER. Move down to Xlist and choose the list that your x-coordinate data is in by pressing 2nd [STAT] moving to your list, and pressing ENTER. Do the same for Ylist. Move down to Mark, choose the first mark, and press ENTER.</p>	 <pre> Plot1 On Off Type: [Line] [Scatter] [Line] [Line] [Square] [Circle] [Triangle] [Diamond] Xlist:L1 Ylist:L2 Mark: [Square] + . </pre>																																
<p>5. In order to see the graph, you need to set the viewing window before graphing. Press WINDOW and choose the Xmin, Xmax, Ymin, Ymax, Xscl and Yscl values based upon the numbers in the x and y list.</p> <p>Tip: Do not change the ΔX or $\Delta Y =$ value. The calculator adjusts this value automatically.</p>	 <pre> WINDOW Xmin=0 Xmax=50 Xscl=5 Ymin=0 Ymax=70 Yscl=5 </pre>																																

6. Press **GRAPH** to see the line.



7. Repeat 2 through 6 for Staircase B. This time put your x -coordinate data in L3 and your y -coordinate data L4, turn off **Plot 1** and turn on **Plot 2**.

6. Compare the steepness of the lines. Which Staircase had the steepest line.

7. What comparison did you see between the steepness of the lines and the slope of the line?

8. Extension: Create one more graph on your calculator of a staircase that has a slope between 0.45 and 0.60, the recommended range for staircases. Repeat 2 through 6 for Staircase C. This time put your x -coordinate data in L5 and your y -coordinate data L6, turn off **Plot 1** and **Plot 2** and turn on **Plot 3**.

Rise =

Run =

Slope =

Adapted from Friel, S. (Ed.). (2001). *Navigating through Algebra in Grades 6-8*, pp. 47-48. Reston, VA: National Council of Teachers of Mathematics.