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## Part 1 - Introduction

1. Consider the integral $\int \sqrt{2 x+3} d x$. Let $\boldsymbol{u}=\mathbf{2 x + 3}$.

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| :---: | :---: | :---: | :---: |
| $\begin{aligned} f(x) & =\sqrt{2 \cdot x+3} \\ u & =2 \cdot x+3 \\ \mathrm{X} \quad \mathrm{~d} u & =\mathrm{du}=\mathrm{=} \\ \mathrm{X} \quad g(u) & =? \\ \mathrm{X} \quad \int g(u) \mathrm{d} u & =? \\ \mathrm{X} \quad \int f(x) \mathrm{d} x & =? \end{aligned}$ |  |  |  |
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2. Now try $\int \sin (x) \cos (x) d x$ by letting $\boldsymbol{u}=\boldsymbol{\operatorname { s i n }}(\boldsymbol{x})$.
3. With the same integral, use $\boldsymbol{u}=\boldsymbol{\operatorname { c o s }}(\boldsymbol{x})$. How does this result compare to the previous result?
4. $\sin (x) \cos (x)$ can be rewritten as $\frac{1}{2} \sin (2 x)$ using the Double Angle formula.

What is the result when you integrate $\int \frac{1}{2} \sin (2 x) \mathrm{d} x$ using substitution?

## Part 2 - Common Feature

Find the result of the following integrals using substitution. Check your work using the Notes pages in the .tns document.
5. $\int \frac{x+1}{x^{2}+2 x+3} d x$
6. $\int \sin (x) e^{\cos (x)} d x$
7. $\int \frac{x}{4 x^{2}+1} d x$
8. What do these integrals have in common that makes them suitable for the substitution method?

## Extension

Use trigonometric identities to rearrange the following integrals and then use the substitution method to integrate.
9. $\int \tan (x) d x$
10. $\int \cos ^{3}(x)$

