## Math TODAY ${ }^{\text {™ }}$

 Student Edition

## World population milestones

## USA SNAPSHOTS ${ }^{\circledR}$

A look at statistics that shape the nation


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## Activity Overview:

The USA TODAY Snapshot "World population milestones" shows the growth of the world population. Additional data from the United Nations Population Division will allow you to explore real-life data that will be modeled by a logistic function. You will explore the end behavior of this model and explain what this means about world population estimates. Derivatives will be used to determine when world population was increasing most rapidly during this time period.

## Focus Questions:

- Determine the logistic model for the world population data from 1950 through 2050. Use this model to determine the population in 1987 and compare this to the population shown in the Snapshot "World population milestones."
- What is the limiting behavior of the logistic model? Explain what this means.
- During which year was the world population increasing most rapidly?


## World population milestones

## Procedure:

## Activity 1

Determine the logistic model for the world population data from 1950 through 2050. Use this model to determine the population in 1987 and compare this to the population shown in the Snapshot "World population milestones."

## Step 1

Enter the data from the table below into your calculator and draw a scatter plot.

| Year | World population (billions) |
| :--- | :---: |
| 1950 | 2.5 |
| 1955 | 2.8 |
| 1960 | 3.0 |
| 1965 | 3.3 |
| 1970 | 3.7 |
| 1975 | 4.1 |
| 1980 | 4.4 |
| 1985 | 4.8 |
| 1990 | 5.3 |
| 1995 | 5.7 |
| 2000 | 6.1 |
| 2005 | 6.5 |
| 2010 | 6.8 |
| 2015 | 7.2 |
| 2020 | 7.5 |
| 2025 | 7.9 |
| 2030 | 8.1 |
| 2035 | 8.4 |
| 2040 | 8.6 |
| 2045 | 8.8 |
| 2050 | 8.9 |

Source: United Nations Population Division

## Step 2

Use your calculator to determine the logistic regression model for the world population data set.

## Step 3

Determine the world population in 1987 (logistic model): $\qquad$

## Step 4

Explain how this value compares to the population shown in the Snapshot.

## Data Source:

United Nations Population Division, World Population Prospects

## Materials:

- TI-83 Plus family or TI-84 Plus family


## Additional Information:

- www.un.org/esa/population/unpop. htm


## World population milestones

## Activity 2

Explain the limiting behavior of the logistic model and what this means.

## Step 1

Explore the graph of the logistic model to determine the behavior of the world population as the years increase without bound.

## Step 2

Use trace or the table feature of the calculator to estimate the limiting value and explain the meaning of this value.

Limiting value:

## Activity 3

Determine during which year the world population increased most rapidly.

## Step 1

Turn off Plot 1 and Y 1 (the logistic model).

## Step 2

Use the numerical derivative feature of the calculator to determine the graph of the derivative.

## Step 3

Determine the maximum value of the derivative graph.
Step 4
Record the year during which the world population increased most rapidly

