

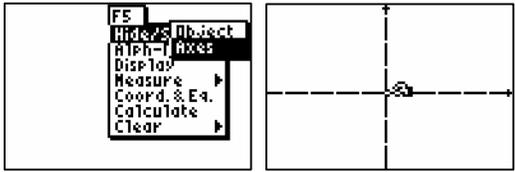
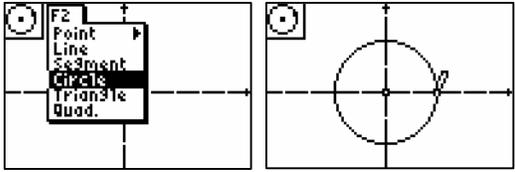
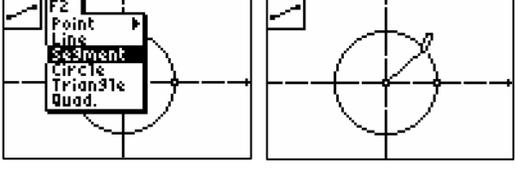
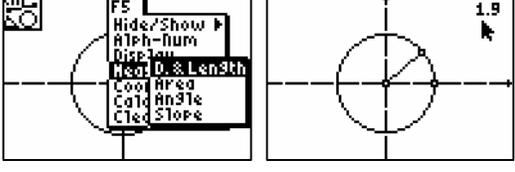
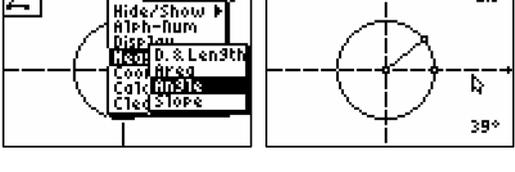
# Investigating the Sine and Cosine Functions – Part 1

Name: \_\_\_\_\_

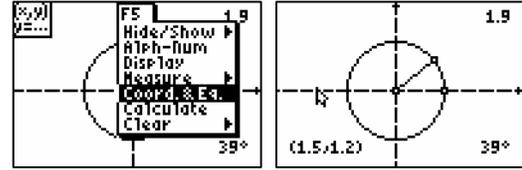
Period: \_\_\_\_\_

Date: \_\_\_\_\_

## Set-Up

<ul style="list-style-type: none"> <li>Press <b>[APPS]</b>. Move down to <b>5: Cabri Jr</b> and press <b>[ENTER]</b>.</li> <li>Press <b>[Y=]</b> for the F1 menu and select <b>New</b>.</li> </ul>	
<ul style="list-style-type: none"> <li>Press <b>[GRAPH]</b> for F5 and select <b>Hide/Show &gt; Axes</b>.</li> <li>Move to the origin and press <b>[ALPHA]</b> to drag the origin to the center of your screen.</li> <li>Press <b>[ENTER]</b> when you have reached the spot where you want to drop the origin.</li> </ul>	
<ul style="list-style-type: none"> <li>Press <b>[WINDOW]</b> for F2 and select <b>Circle</b>.</li> <li>Draw a circle with its center at the origin and a radius of your choice. (Press <b>[ENTER]</b> to mark the radius on the x-axis).</li> </ul>	
<ul style="list-style-type: none"> <li>Press F2 again and select <b>Segment</b> to draw a segment from the center of the circle to a point on the circle in quadrant I.</li> </ul>	
<ul style="list-style-type: none"> <li>Press F5 and choose <b>Measure &gt; D &amp; Length</b> to measure the radius of the circle.</li> <li>Drag and drop this length off to the upper right hand side of your screen so it is out of your way.</li> </ul>	
<ul style="list-style-type: none"> <li>Measure the angle formed by the x-axis and the segment you drew in quadrant I by pressing F5 and choosing <b>Measure &gt; Angle</b>.</li> <li>Drop this length off to the lower right hand side of your screen so it is out of the way.</li> </ul>	

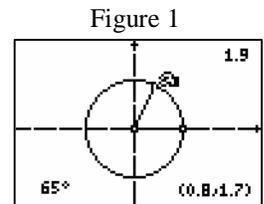
- Press F5 again and select **Coord & Eq.** Move to the point where the terminal side of the angle touches the circle and press **ENTER** to label the coordinates.
- Again, drag and drop the coordinates off to the bottom left of your screen so they are out of the way as shown.



## Collecting Data

What is the radius of your circle? \_\_\_\_\_

- Move to the point whose coordinates you found in the last step above.
- Press **ALPHA** when the point is highlighted to select and drag the point. (See figure 1.)
- You are going to collect data by dragging this point around your circle. As you move the point record the measure of the **angle** in the 1<sup>st</sup> column below, the **x-coordinate** in column 2 (We will use this column later), and the **y-coordinate** in column 3.
- You are going to choose two points from each quadrant along with each of the four **quadrantal angles**.
- Remember that as you move into quadrants III and IV, Cabri Jr. will give the angle as a measure between  $0^\circ$  and  $180^\circ$ . It is your job to use your knowledge of the coordinate axes and reference angles to convert this angle to an appropriate measure between  $180^\circ$  and  $360^\circ$ .



Angle Measure	X-Coordinate	Y-Coordinate
$0^\circ$		
$90^\circ$		
$180^\circ$		
$270^\circ$		
$360^\circ$		

## Investigating the Relationship

You are now going to examine the relationship between the **y-coordinate** and the **angle measure** around the circle.

Press **[STAT]** > **Edit**.

Enter the **angle measures** from above into **[L1]** and the **y-coordinates** into **[L2]**.

We are now going to define **[L3]** as **the y-coordinate divided by the radius** of the circle. To do this move to **[L3]** so that the name of the list is highlighted and press **[ENTER]**. Press **[L2]** **[÷]** the value you found to be the radius of your circle (figure 2). Then press **[ENTER]**.

L1	L2	3
0	0	-----
39	1.2	
92	1.7	
90	1.9	
124	1.6	
151	1.9	
180	0	
L3=L2/1.9		

Figure 2

Press **[2nd]** **[Y=]**. Turn plot one on by pressing **[1]** and then pressing **[ENTER]** when On is highlighted as shown in figure 3.

Plot1	Plot2	Plot3
On	Off	
Type: [ ]	[ ]	[ ]
Xlist: L1		
Ylist: L3		
Mark: [ ]	[ ]	[ ]

Figure 3

Define your x-list to be **[L1]** and your y-list to be **[L3]**.

Press **[WINDOW]** and set your window to fit your data as shown in figure 4.

WINDOW
Xmin=0
Xmax=360
Xscl=90
Ymin=-2
Ymax=2
Yscl=1
Xres=1

Figure 4

Now press **[GRAPH]** and sketch the scatter plot that you see on the axes below. What is special about the result?



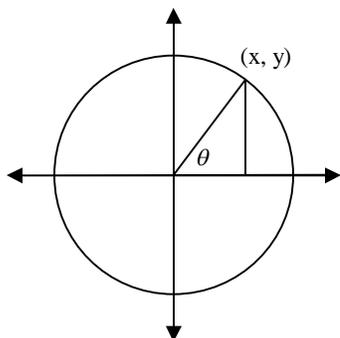
What trig function is represented above? \_\_\_\_\_

## Questions

1. Based on your results, define  $\sin \theta$  for any point along the circle.

$$\sin \theta =$$

2. Label the opposite, adjacent, and hypotenuse for the following triangle and use the diagram to explain your answer in question #1.



3. According to your answer to #1 and the graph you found, in which quadrant(s) is the sine function positive?
4. As you recall, a **quadrantal angle** is an angle whose terminal side lies on the x or y - axis. Using your conjecture in question #1, give the sine for the following **quadrantal angles**:

$$\begin{aligned}\sin 0^\circ &= \underline{\hspace{2cm}} \\ \sin 90^\circ &= \underline{\hspace{2cm}} \\ \sin 180^\circ &= \underline{\hspace{2cm}} \\ \sin 270^\circ &= \underline{\hspace{2cm}} \\ \sin 360^\circ &= \underline{\hspace{2cm}}\end{aligned}$$

5. What is the equation for the unit circle? What are the radius and center of the unit circle?

Equation: \_\_\_\_\_ Center: \_\_\_\_\_ Radius: \_\_\_\_\_

6. If you are given a point on the unit circle, what do you know about the sine of the angle whose terminal side passes through that point?

$$\sin \theta =$$

## Investigating the Sine and Cosine Functions – Part 2

### Investigating the Relationship

You are now going to examine the relationship between the **x-coordinate** and the **angle measure** around the circle. Make a prediction for what the result will represent?

Leaving the angle measures in [L1], enter the **x-coordinates** into [L2] as you did with the y-coordinates previously in Part I.

This time we are going to define [L3] as the **x-coordinates divided by the radius** of the circle. Remember to move to [L3] so that the name of the list is highlighted and press **ENTER**. Press [L2]  $\div$  the value you found to be the radius of your circle. Then press **ENTER**.

Make sure that Plot One is turned on and define your x-list to be [L1] and your y-list to be [L3] as you did previously.

Using the same window as in part one, press **GRAPH** and sketch the scatter plot that you see on the axes below.



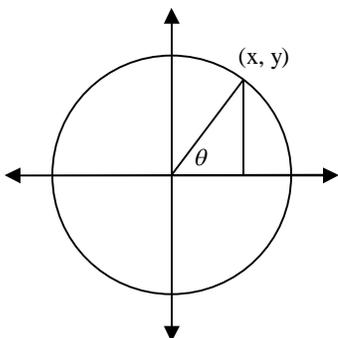
Was your prediction correct?

## Questions

1. Based on your results, define  $\cos \theta$  for any point along the circle.

$$\cos \theta =$$

2. Label the opposite, adjacent, and hypotenuse for the following triangle and use the diagram to explain your answer in question #1.



3. According to your answer to #1 and the graph you found, in which quadrant(s) is the cosine function positive?

4. Find the cosine for the following **quadrantal angles**:

$$\begin{aligned}\cos 0^\circ &= \underline{\hspace{2cm}} \\ \cos 90^\circ &= \underline{\hspace{2cm}} \\ \cos 180^\circ &= \underline{\hspace{2cm}} \\ \cos 270^\circ &= \underline{\hspace{2cm}} \\ \cos 360^\circ &= \underline{\hspace{2cm}}\end{aligned}$$

5. If you are given a point on the unit circle, what do you know about the cosine of the angle whose terminal side passes through that point?

$$\cos \theta =$$

