# Functions & Graphs Test 2A



Name:

9 10 11 12









## Question: 1

A possible equation for the graph of the curve shown is:

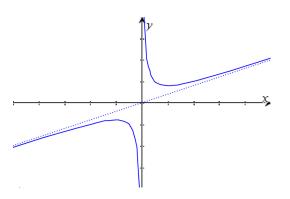
a) 
$$y = \frac{ax^2 + b}{x}$$
,  $a > 0$  and  $b > 0$ 

b) 
$$y = \frac{ax^2 + b}{x}$$
,  $a < 0$  and  $b < 0$ 

c) 
$$y = \frac{ax^2 + b}{x}$$
,  $a < 0$  and  $b > 0$ 

d) 
$$y = \frac{ax^3 + b}{x^2}$$
,  $a > 0$  and  $b > 0$ 

e) 
$$y = \frac{ax^3 + b}{x^2}$$
,  $a < 0$  and  $b < 0$ 



# Question: 2

Which one of the following functions does **not** have range:  $[-\pi, \pi]$ 

a) 
$$y = \left| x - \frac{\pi}{2} \right| - \left| x + \frac{\pi}{2} \right|$$

b) 
$$y = 2\sin^{-1}(x)$$

c) 
$$y = 2\sin^{-1}(x-2)$$

d) 
$$y = \tan^{-1}(x)$$

e) 
$$y = 2\cos^{-1}(x) - \pi$$

## **Question: 3**

y = f(x) has a local maximum at (2,-4), the function  $y = \frac{1}{f(x)}$  will have:

- a local maximum at (2,4)
- b) a local maximum at  $\left(2, -\frac{1}{4}\right)$
- a local minimum at (2,4)
- d) a local minimum at  $\left(2, -\frac{1}{4}\right)$
- a local minimum  $\left(\frac{1}{2}, -\frac{1}{4}\right)$

## Question: 4

The graph y = cosec(2x) has asymptotes:

a) 
$$x = n\pi$$

b) 
$$x = 2n\pi$$

b) 
$$x = 2n\pi$$
 c)  $x = \frac{2(n-1)\pi}{4}$  d)  $x = \frac{n\pi}{4}$  e)  $x = \frac{n\pi}{2}$ 

d) 
$$x = \frac{n\pi}{4}$$

e) 
$$x = \frac{n\pi}{2}$$

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## **Question: 5**

The graph of  $y = \frac{1}{2a^2 + ax - x^2}$  where a is a non-zero real constant, has asymptotes at:

a) 
$$x = 2a$$
 only

b) 
$$x = -a$$
 only

c) 
$$x = a$$
 and  $x = -2a$  only

d) 
$$x = -a$$
 and  $x = 2a$  only

e) 
$$x = -a$$
,  $x = 2a$  and  $y = 0$ .

# Question: 6

The graph of  $y = 2 \tan^{-1} \left( \frac{x}{2} \right)$  has asymptotes at

a) 
$$x = \pm 2$$

b) 
$$y = \pm 2$$

$$x = \pm 2$$
 b)  $y = \pm 2$  c)  $x = \pm \frac{\pi}{2}$  d)  $y = \pm \frac{\pi}{2}$  e)  $y = \pm \pi$ 

d) 
$$y = \pm \frac{\pi}{2}$$

e) 
$$y = \pm \pi$$

# **Question: 7**

Given  $f(x) = (x-a)^2(x+a)^2$ ,  $g(x) = \frac{1}{f(x)}$  and a > 1 which statement is **not** true:

a) 
$$f'(0) = 0$$

b) 
$$f'(a) = 0$$

c) 
$$g'(0) = 0$$

d) 
$$g'(a) = 0$$

a) 
$$f'(0) = 0$$
 b)  $f'(a) = 0$  c)  $g'(0) = 0$  d)  $g'(a) = 0$  e)  $0 < g(0) < 1$ 

# **Question: 8**

If  $f(x) = \frac{ax^2 + bx + c}{x + 5}$  has an asymptote y = 2x - 4 then

a) 
$$a = 2$$
  
 $b = 5$   
b)  $a = 2$   
 $b = -5$   
c)  $a = 2$   
 $b = 6$   
d)  $a = -2$   
 $b = 4$   
e)  $a = 2$   
 $b = -4$ 

b) 
$$a=2$$

c) 
$$a=2$$
  
 $b=6$ 

$$a = -2$$
d)  $b = 4$ 

$$a = 2$$

## **Question: 9**

If  $f(x) = \frac{1}{x^2 + hx + c}$  has two asymptotes of the form x = m and x = n then it follows:

a) 
$$b > 2\sqrt{c}$$
 or   
  $b < -2\sqrt{c}$  b)  $b > c$  c)  $b < c$  d)  $b < -2c$  e)  $b > 2c$ 

b) 
$$b > c$$

c) 
$$b < c$$

$$d) \qquad b < -2c$$

e) 
$$b > 2c$$

#### Question: 10

Given  $a \neq b \neq c \neq d \neq 0$ , a possible equation for the graph shown is:

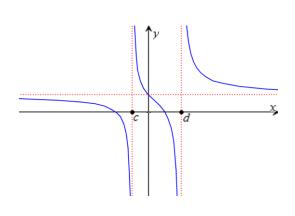
a) 
$$y = \frac{(x+a)(x-b)}{(x+c)(x-d)}$$

b) 
$$y = \frac{(x-a)(x-b)}{(x-c)(x-d)}$$

c) 
$$y = \frac{(x+a)^2(x+b)}{(x-c)(x-d)}$$

d) 
$$y = -x^3 + \frac{1}{(x-c)(x-d)} + 1$$

e) 
$$y = \frac{a(x+b)}{(x+c)(x-d)}$$



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