

**Part 1 – Explore Integrating In  $x$** Problem of the Day:  $\int \ln x dx$ .

One can quickly find the solution to the indefinite integral by entering in a CAS system. Do this now and complete the equation.

$$\int \ln x dx =$$

Yet, more important than the answer is how can we get it without the use of technology. List the techniques for integration that you know. Which technique will give a result similar to the one above?

Recall the formula for integration by parts:  $\int uv'dx = uv - \int vu'dx$ .

Make your choices for  $u$  and  $v'$ , calculate  $u'$  and  $v$ , and record the results below. Hint: when making your choice for  $u$ , remember the mnemonic device **LIPET**.

**L** – log (or natural log)

**I** – inverse

**P** – polynomial

**E** – exponential

**T** – trigonometric

$$u =$$

$$u' =$$

$$v' =$$

$$v =$$

Complete the process obtaining the result we got before.

Check your answer by differentiating the result.

Finally, confirm your solution graphically. Graph  $y = \ln(x)$  and your result. With a partner, discuss how the two graphs relate to each other.

**Part 2 – Extension/Homework**

Integrate each of the following. Show all work. Verify your answers using the handheld.

1.  $\int \tan^{-1} x dx$

2.  $\int \ln(2x) dx$

3.  $\int xe^x dx$

4.  $\int x^2 e^x dx$

5.  $\int x \sin x dx$