

Slope-Intercept Form

What You'll Learn

- To write linear equations in slope-intercept form
- To graph linear equations

... And Why

To use a graph to relate total earnings to sales, as in Example 5

Check Skills You'll Need

Evaluate each expression.

1. $6a + 3$ for $a = 2$

3. $\frac{1}{4}x + 2$ for $x = 16$

5. $8 - 5n$ for $n = 3$

GO for Help Lessons 1-2 and 2-3

2. $-2x - 5$ for $x = 3$

4. $0.2x + 2$ for $x = 15$

6. $-4p + 9$ for $p = 2$

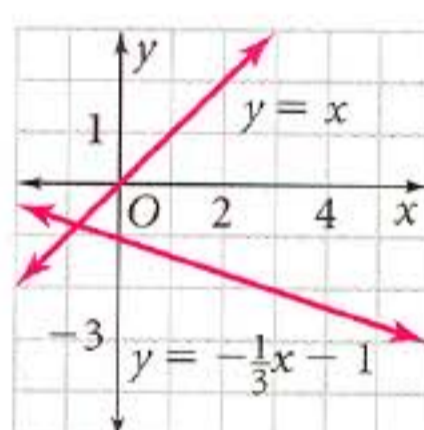
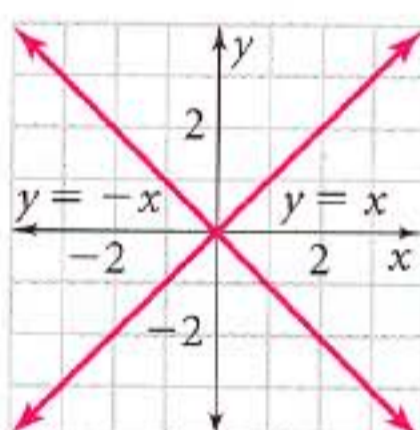
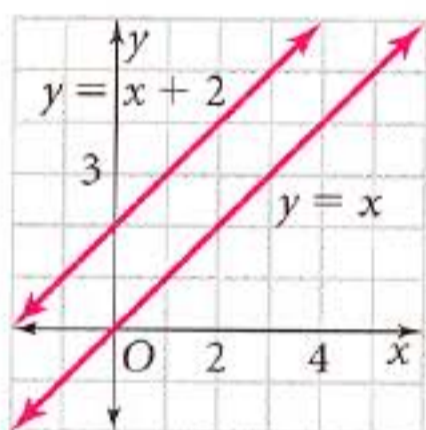
New Vocabulary • linear equation • parent function • linear parent function • y-intercept • slope-intercept form

1 Writing Linear Equations

Vocabulary Tip

The word linear contains the word "line".

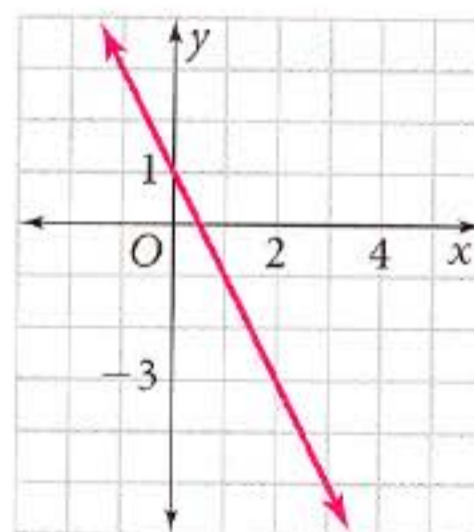
An equation whose graph is a line is a **linear equation**. A variable in a linear equation cannot be raised to a power other than 1. So $y = 2x$ is a linear equation but $y = x^2$ or $y = 2^x$ are not. All linear equations are related.



The functions shown above all graph as lines. A **parent function** is the simplest equation of a function. The equation $y = x$ or $f(x) = x$ is the **linear parent function** for all equations that graph as lines.

The equation of a line gives important information about its graph. Consider the table and graph of the equation $y = -2x + 1$.

x	$-2x + 1$	y
0	$-2(0) + 1$	1
1	$-2(1) + 1$	-1
2	$-2(2) + 1$	-3



Two points on the line are $(0, 1)$ and $(2, -3)$. The slope is $\frac{1 - (-3)}{0 - 2} = -\frac{4}{2}$ or -2 . The **y-intercept** is the y -coordinate of the point where a line crosses the y -axis. Since $y = -2x + 1$ crosses the y -axis at $(0, 1)$, the y -intercept is 1.

If you know the slope of a line and its y -intercept, you can write the equation of the line. The letter m refers to the *slope*.



Key Concepts



Test-Taking Tip

As you do homework, make a list of formulas you can use later to study for quizzes and tests.

Definition

Slope-Intercept Form of a Linear Equation

The **slope-intercept form** of a linear equation is $y = mx + b$.

↑ ↑
slope y-intercept

1 EXAMPLE Identifying Slope and y-Intercept

What are the slope and y-intercept of $y = 3x - 5$?

$y = mx + b$ Use the slope-intercept form.

$y = 3x + (-5)$ Think of $y = 3x - 5$ as $y = 3x + (-5)$.

- The slope is 3; the y-intercept is -5 .

Quick Check

- a. Find the slope and y-intercept of $y = \frac{7}{6}x - \frac{3}{4}$.
b. **Critical Thinking** For the equation in Example 1, what happens to the graph of the line and to the equation if the y-intercept is moved down 3 units?

2 EXAMPLE Writing an Equation

Write an equation of the line with slope $\frac{3}{8}$ and y-intercept 6.

$y = mx + b$ Use the slope-intercept form.

- $y = \frac{3}{8}x + 6$ Substitute $\frac{3}{8}$ for m and 6 for b .

Quick Check

- 2 Write an equation of a line with slope $m = \frac{2}{5}$ and y-intercept $b = -1$.

3 EXAMPLE Writing an Equation From a Graph

Multiple Choice Which equation models the linear function shown in the graph?

- (A) $y = -\frac{3}{4}x + 2$ (B) $y = -\frac{4}{3}x + 2$
(C) $y = 2x - \frac{4}{3}x$ (D) $y = 2x - \frac{3}{4}$

Find the slope. Two points on the line are $(0, 2)$ and $(4, -1)$.

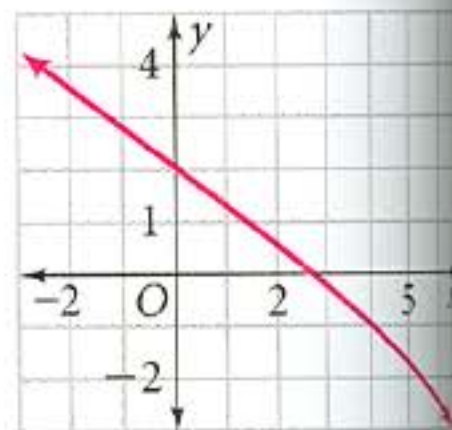
$$\text{slope} = \frac{-1 - 2}{4 - 0} = -\frac{3}{4}$$

The y-intercept is 2. Write an equation in slope-intercept form.

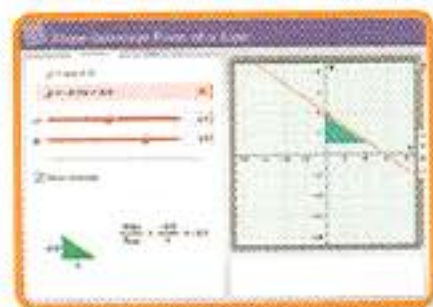
$$y = mx + b$$

$$y = -\frac{3}{4}x + 2 \quad \text{Substitute } -\frac{3}{4} \text{ for } m \text{ and } 2 \text{ for } b.$$

- The equation is $y = -\frac{3}{4}x + 2$. So the answer is A.



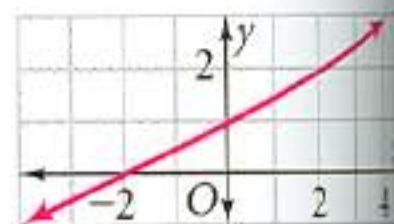
Online active math



For: Slope-Intercept Activity
Use: Interactive Textbook, 6-2

Quick Check

- 3 a. Write the equation of the line using the points $(0, 1)$ and $(2, 2)$.
b. **Critical Thinking** Does the equation of the line change if you use $(-2, 0)$ instead of $(2, 2)$? Explain.



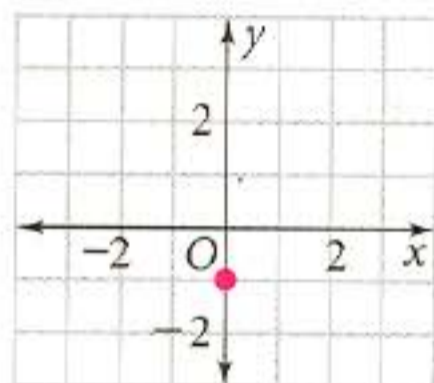
Each point on the graph of an equation is an ordered pair that makes the equation true. The graph of a linear equation is a line that indicates all the solutions of the equation. You can use the slope and y -intercept to graph a line.

4 EXAMPLE Graphing Equations

Graph $y = 3x - 1$.

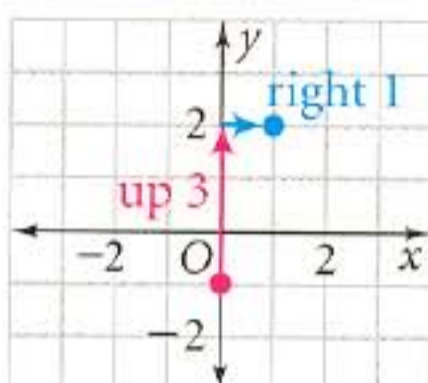
Step 1

The y -intercept is -1 . So plot a point at $(0, -1)$.



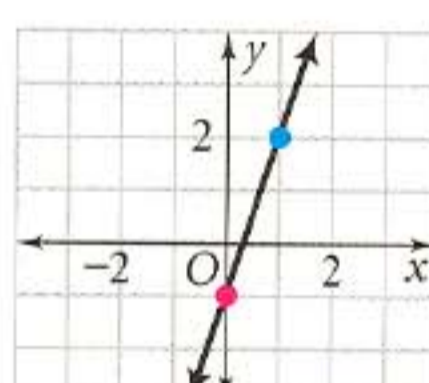
Step 2

The slope is 3, or $\frac{3}{1}$. Use the slope to plot a second point.



Step 3

Draw a line through the two points.



Quick Check

4 Graph $y = \frac{3}{2}x - 2$.

When you graph equations for real-world situations, use scales on the x - and y -axes that are reasonable for the situation. Recall that you can avoid having a large blank space in a graph by using a zigzag line to show a break in a scale.

5 EXAMPLE Real-World Problem Solving

Commission The base pay of a water-delivery person is \$210 per week. He also earns 20% commission on any sale he makes. The equation $t = 210 + 0.2s$ relates total earnings t to sales s . Graph the equation.

Step 1 Identify the slope and y -intercept.

$$t = 210 + 0.2s$$

$$t = 0.2s + 210$$

Rewrite the equation in slope-intercept form.

↑ slope ↑ y -intercept

Step 2 Plot two points. First plot $(0, 210)$, the y -intercept. Then use the slope to plot a second point.

The slope is 0.2, which equals $\frac{2}{10}$, or $\frac{20}{100}$. Plot a second point 20 units above and 100 units to the right of the y -intercept.

Step 3 Draw a line through the points.



Real-World Connection

Between 1990 and 1999, the sales of bottled water in the United States increased 107.6%, which means that sales more than doubled.



Quick Check

5 Suppose the base pay of the delivery person is \$150, and his commission on each sale is 30%. The equation relating his total earnings t to sales s is $t = 150 + 0.3s$. Graph the equation.

EXERCISES

For more exercises, see *Extra Skill and Word Problem Practice*.

Practice and Problem Solving

A Practice by Example

Example 1
(page 318)



Example 2
(page 318)

Example 3
(page 318)

Example 4
(page 319)

Example 5
(page 319)

Find the slope and y-intercept of each equation.

1. $y = -2x + 1$

2. $y = -\frac{1}{2}x + 2$

3. $y = x - \frac{5}{4}$

4. $y = 5x + 8$

5. $y = \frac{2}{3}x + 1$

6. $y = -4x$

7. $y = -x - 7$

8. $y = -0.7x - 9$

9. $y = -\frac{3}{4}x - 5$

Write an equation of a line with the given slope and y-intercept.

10. $m = \frac{2}{9}, b = 3$

11. $m = 3, b = \frac{2}{9}$

12. $m = \frac{9}{2}, b = 3$

13. $m = 0, b = 1$

14. $m = -1, b = -6$

15. $m = -\frac{2}{3}, b = 5$

16. $m = 0.3, b = 4$

17. $m = 0.4, b = 0.6$

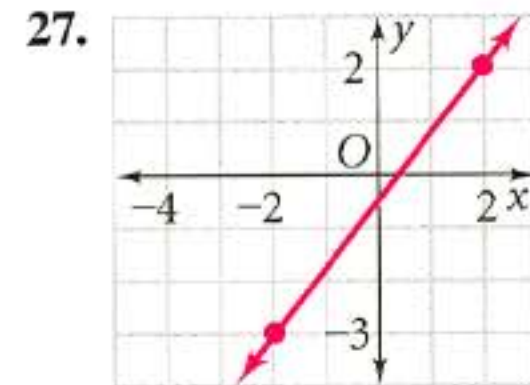
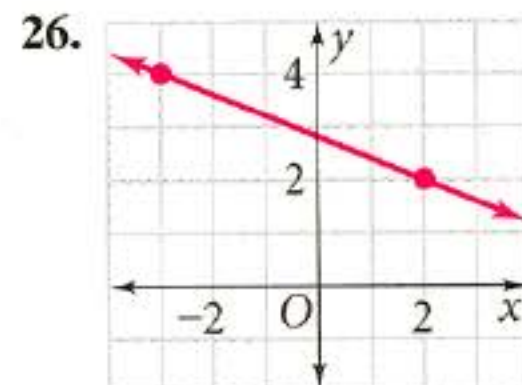
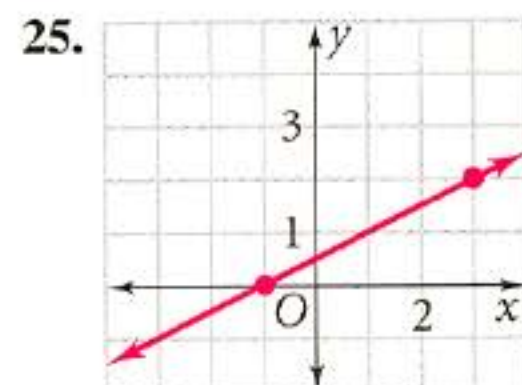
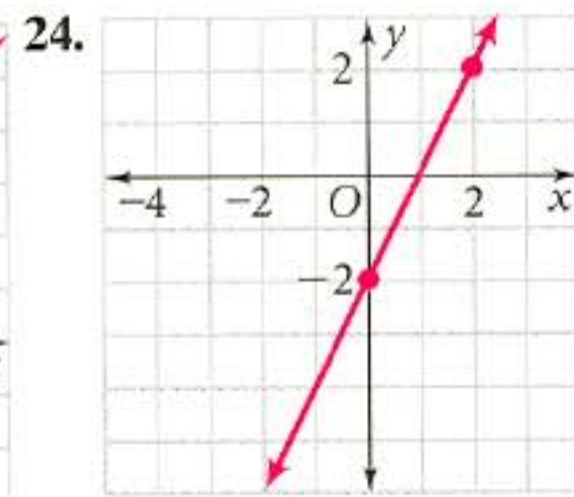
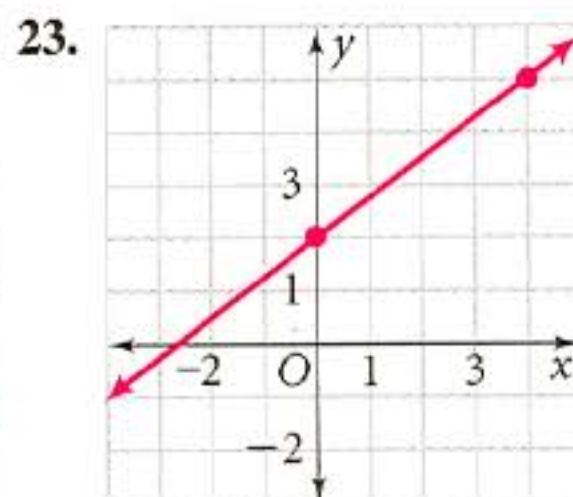
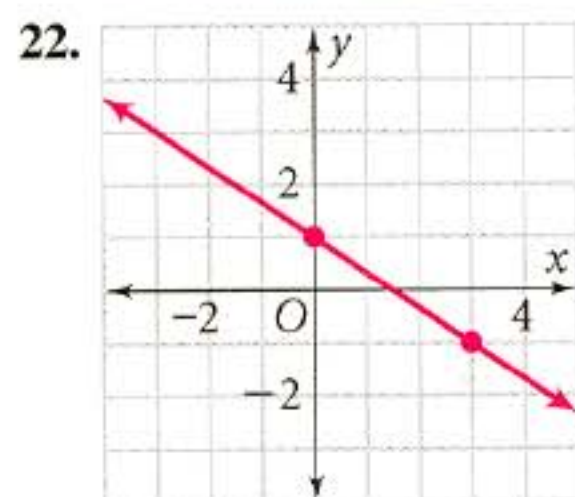
18. $m = -7, b = \frac{1}{3}$

19. $m = -\frac{1}{5}, b = -\frac{2}{5}$

20. $m = -\frac{1}{4}, b = \frac{5}{4}$

21. $m = \frac{8}{3}, b = \frac{2}{3}$

Write the slope-intercept form of the equation for each line.



Use the slope and y-intercept to graph each equation.

28. $y = \frac{1}{2}x + 4$

29. $y = \frac{2}{3}x - 1$

30. $y = -5x + 2$

31. $y = 2x + 5$

32. $y = x + 4$

33. $y = -x + 2$

34. $y = 4x - 3$

35. $y = -\frac{3}{2}x$

36. $y = \frac{2}{5}x - 3$

37. $y = -\frac{2}{3}x + 2$

38. $y = -\frac{4}{5}x + 4$

39. $y = -0.5x + 2$

40. **Retail Sales** A music store is offering a coupon promotion on its CDs. The regular price for CDs is \$14. With the coupon, customers are given \$4 off the total purchase. The equation $t = 14c - 4$, where c is the number of CDs and t is the total cost of the purchase, models this situation.

a. Graph the equation.

b. Find the total cost for a sale of 6 CDs.

B Apply Your Skills

Find the slope and y-intercept of each equation.

41. $y - 2 = -3x$

42. $y + \frac{1}{2}x = 0$

43. $y - 9x = \frac{1}{2}$

44. $y = 3x - 9$

45. $2y - 6 = 3x$

46. $-2y = 6(5 - 3x)$

47. $y - d = cx$

48. $y = (2 - a)x + a$

49. $2y + 4n = -6x$

Use the slope and y-intercept to graph each equation.

50. $y = 7 - 3x$

51. $2y + 4x = 0$

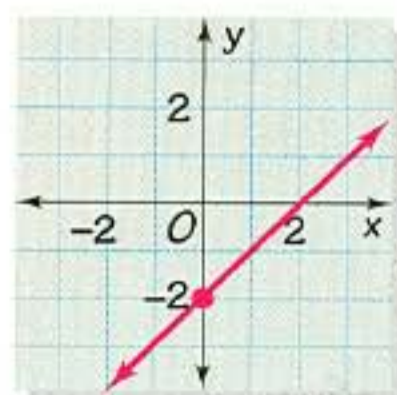
52. $3y + 6 = -2x$

53. $y + 2 = 5x - 4$

54. $4x + 3y = 2x - 1$

55. $-2(3x - 4) + y = 0$

56. **Error Analysis** Fred drew the graph at the right for the equation $y = -2x + 1$. What error did he make?



57. a. A candle begins burning at time $t = 0$. Its original height is 12 in. After 30 min the height of the candle is 8 in. Draw a graph showing the change in the height of the candle.

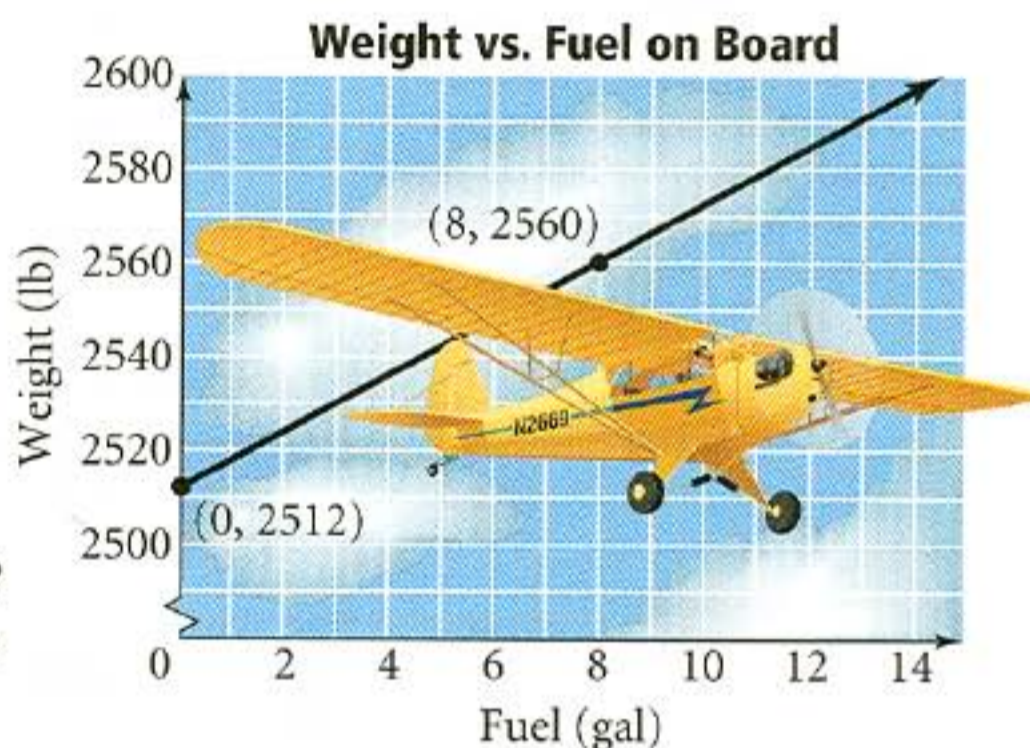
b. Write an equation that relates the height of the candle to the time it has been burning.

c. How many minutes after the candle is lit will it burn out?

58. **Airplane Fuel** The graph shows the relationship between the number of gallons of fuel in the tank of an airplane and the weight of the airplane. The equation $y = 6x + 2512$, where x is the number of gallons of fuel and y is the weight of the airplane, models this situation.

a. What does the slope represent?

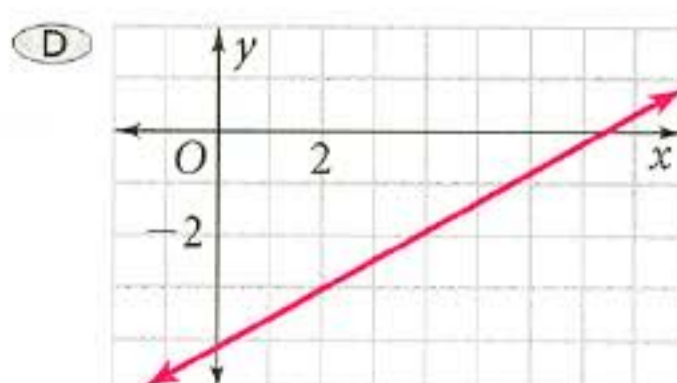
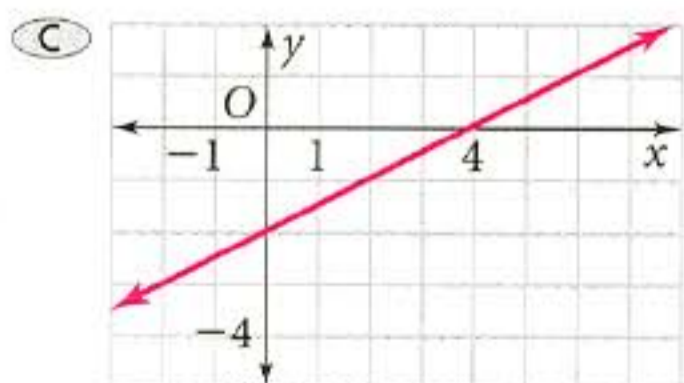
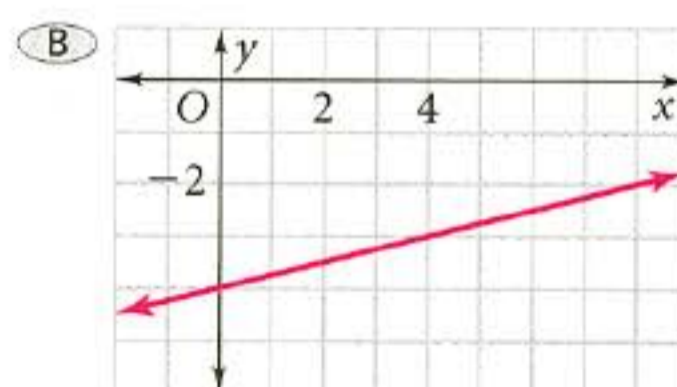
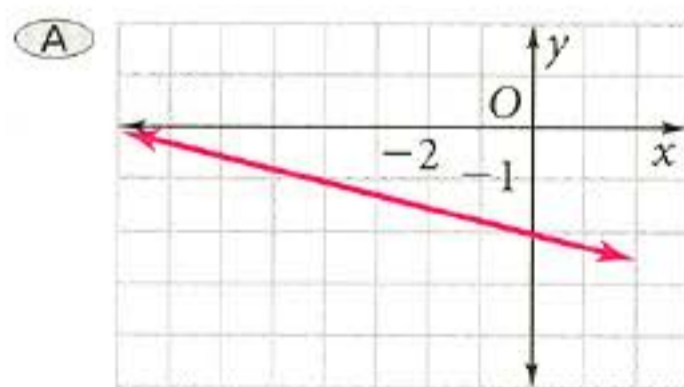
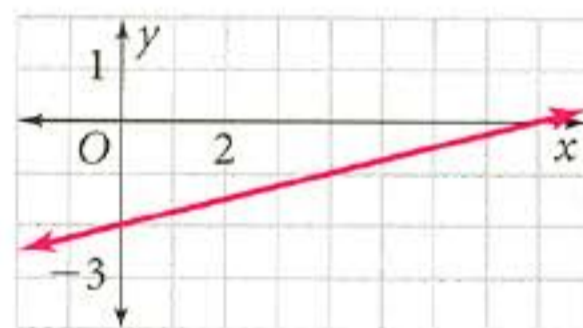
b. Use the equation to predict the weight of the plane when the tank contains 25 gallons of fuel.



Is the ordered pair on the graph of the given equation?

59. $(-3, 4); y = -2x + 1$ 60. $(-6, 5); y = -\frac{1}{2}x + 2$ 61. $(0, -1); y = x - \frac{5}{4}$

62. **Multiple Choice** At the right is the graph of $y = \frac{1}{4}x - 2$. Which of the graphs below represents the linear function if the slope is doubled and the y-intercept stays the same?



Real-World Connection

Careers Airport ground crews direct airplanes to and from their gates.

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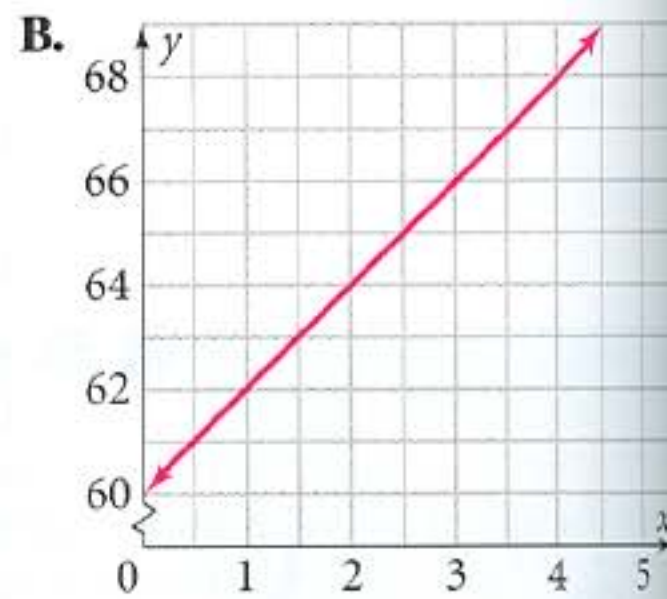
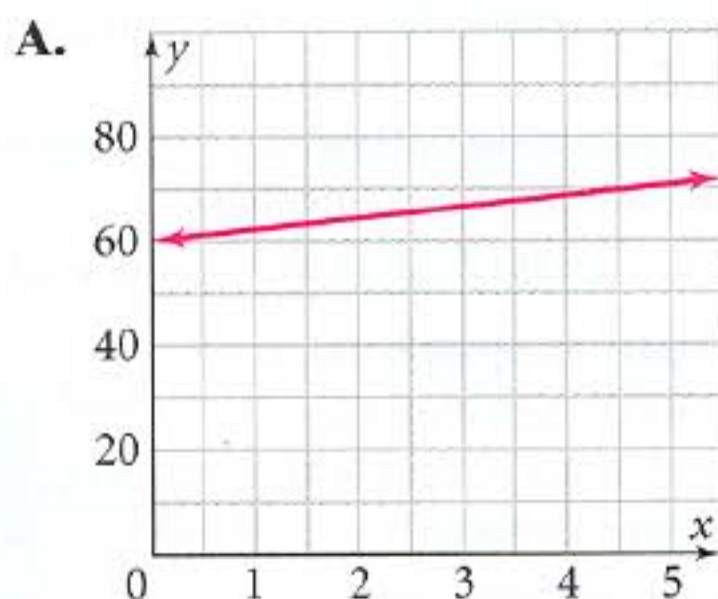
Real-World Connection

In the United States, although 35% of households have pet cats and 37% have pet dogs, there are about 25% more pet cats than pet dogs.

63. **Pet Care** When the Bryants leave town for a vacation, they put their dog Tyco in a kennel. The kennel charges \$15 for a first-day flea bath and \$5 per day. The equation $t = 15 + 5d$ relates the total charge t to the number of days d .
- Rewrite the equation in slope-intercept form.
 - Graph the equation.
 - Explain why the line you graph should lie only in Quadrant I.

64. **Writing** Explain the steps you would use to graph $y = \frac{3}{4}x + 5$.

65. **Critical Thinking** Which graphed line has the greater slope? Explain.



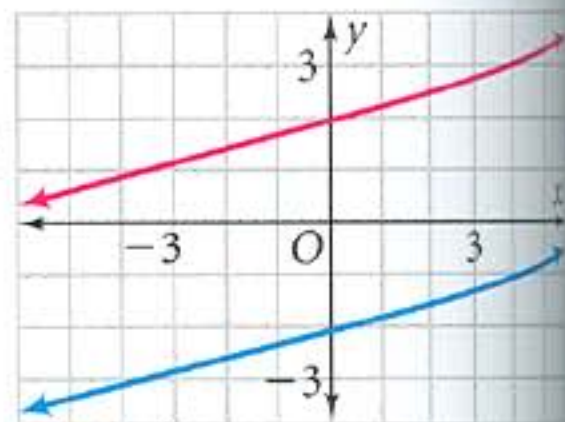
Given two points on a line, write the equation of the line in slope-intercept form.

66. $(3, 5), (5, 9)$ 67. $(5, -13), (2, -1)$ 68. $(-4, 10), (6, 5)$
 69. $(8, 7), (-12, 2)$ 70. $(-7, 4), (11, -14)$ 71. $(-1, -9), (2, 0)$

72. **Graphing Calculator** Suppose you want to graph the equation $y = \frac{5}{4}x - 3$. Enter each key sequence and display the graph.

- a. $\boxed{Y=}$ $\boxed{5}$ $\boxed{\div}$ $\boxed{4}$ $\boxed{X,T,\theta,n}$ $\boxed{-}$ $\boxed{3}$ b. $\boxed{Y=}$ $\boxed{(}$ $\boxed{5}$ $\boxed{\div}$ $\boxed{4}$ $\boxed{)}$ $\boxed{X,T,\theta,n}$ $\boxed{-}$ $\boxed{3}$
 c. Which equation gives you the graph of $y = \frac{5}{4}x - 3$? Explain.

73. a. What is the slope of each line?
 b. What is the y-intercept of each line?
 c. **Geometry** The lines in the graph are parallel. What appears to be true about the slopes of parallel lines?



74. **Open-Ended** Write a linear equation. Identify the slope and y-intercept. Then graph your equation.

Challenge

Find the value of a such that the graph of the equation has the given slope.

75. $y = 2ax + 4; m = -1$ 76. $y = -\frac{1}{2}ax - 5; m = \frac{5}{2}$ 77. $y = \frac{3}{4}ax + 3; m = \frac{9}{16}$

78. a. **Geometry** Graph these equations on the same grid.
 $y = 3$ $y = -3$ $x = 2$ $x = -2$
 b. What geometric figure did you draw? Justify your answer.
 c. Draw a diagonal of the figure. What is the equation of this line? Explain.

79. **Recreation** A group of mountain climbers begin an expedition with 265 lb of food. They plan to eat a total of 15 lb of food per day.
- Write an equation in slope-intercept form relating the remaining food supply r to the number of days d .
 - Graph your equation.
 - The group plans to eat the last of their food the day their expedition ends. Use your graph to find how many days they expect the expedition to last.

Multiple Choice

80. Which equation has the same y -intercept as $y = 4x - 3$?
 A. $y - 3 = x$ B. $y = 8x + 3$ C. $3 - y = 4x$ D. $y = -3 + 8x$
81. Which of the following is the equation of the line that has the same slope as $y = -\frac{3}{2}x + 2$ and the same y -intercept as $y = 3x - 2$?
 F. $y - 2 = -\frac{3}{2}x$ G. $-\frac{3}{2}x = y + 2$
 H. $y + 2 = -\frac{3}{2}$ J. $-\frac{3}{2}x = y + 3$
82. A software company started with 2 employees. In 6 months, the company had 7 employees. The number of employees increased at a steady rate. Which equation models the relationship between the number of employees n and the number of months m since the company started?
 A. $n = \frac{5}{6}m + 2$ B. $m = 2n + \frac{5}{6}$
 C. $n = \frac{6}{5}m + 2$ D. $m = \frac{5}{6}n + 2$

Short Response

83. A line passes through the points $(0, 3)$ and $(1, 5)$. Graph this line and find an equation for the line in slope-intercept form. Show your work.

Mixed Review

Lesson 6-1



Review page 166

Find the slope of the line that passes through each pair of points.

84. $(-2, 8), (5, -1)$ 85. $(0, 0), (-6, 5)$ 86. $(4, 6), (2, -3)$ 87. $(1, 2), (2, 1)$
88. The greeting card industry sells over 6 billion cards annually. Women purchase 80% of all greeting cards sold. How many cards do women purchase annually?

A Point in Time



On August 30, 1984, Astronaut Judith A. Resnik became the second American woman in space, on the shuttle *Discovery's* first voyage. Resnik was an electrical engineer with a Ph.D. from the University of Maryland. Prior to her mission, she helped to design and develop a remote manipulator system. This required skill in writing linear equations. Her job during *Discovery's* six-day voyage was to manipulate a robotic arm and to extend and retract the shuttle's solar power array. Resnik died tragically in the *Challenger* disaster in 1986.



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