Problem 1 – A general trigonometric function

Using the *Transformation Graphing* app, press **Y** and enter the general sine function in **Y**₁,

$$Y_1 = A * \sin(B * X + C) + D.$$

Complete the table.

Α	В	С	D	zero1	zero2	min	max
1	1	0	0				
4	1/2	3	1				

Problem 2 – The effect of the coefficients A, B, C, and D

Examining A

• Set B = 1 and C = D = 0 and change the value of A. Try 4 different values of A.

Α	В	С	D	zero1	zero2	min	max
	1	0	0				
	1	0	0				
	1	0	0				
	1	0	0				

- How did the appearance of the graph change?
- Which graph features changed? Which did not change?
- Write equations to describe the relationship between *A* and the features that did change.
- When *B* = 1 and *C* = *D* = 0, _____

The value of *A* is the **amplitude**. It is equal to half of the difference between its maximum and minimum values.

- Calculate the amplitude from the minimum and maximum values in the table above.
- Compare the results to the values of A. What do you notice?

Examining B

Α	В	С	D	zero1	zero2	min	max
1		0	0				
1		0	0				
1		0	0				
1		0	0				

- Try 4 different values of B. How did the appearance of the graph change?
- Which graph features changed? Which did not change?
- Describe the relationship between *B* and the features that did change.

Examining C

Α	В	С	D	zero1	zero2	min	max
1	1		0				
1	1		0				
1	1		0				
1	1		0				

- Try 4 different values of C. How did the appearance of the graph change?
- Which graph features changed? Which did not change?
- What is the effect of an increasing sequence of values for C on the graph?
- What is the effect of a decreasing sequence of values for *C* on the graph?

Examining D

Α	В	С	D	zero1	zero2	min	max
1	1	0					
1	1	0					
1	1	0					
1	1	0					

- Try 4 different values of D. How did the appearance of the graph change?
- Try an increasing sequence of values for *D* such as 0, 1, 2, 3, 4... What is the effect on the graph?
- Try a decreasing sequence of values for D such as 0, -1, -2, -3, -4... What is the effect on the graph?
- Describe the effect of the value of *D* on the graph. How does changing *D* change the graph features?

Problem 3 – A closer look at amplitude, period, and frequency

In Y_1 , enter the general cosine function, A * cos(B * X + C) + D.

amplitude: half of the vertical distance from minimum value to maximum value

period: horizontal distance from one peak (maximum point) to the next

frequency: number of cycles per 2π interval

- Write a formula to find the frequency f given the period p.
- Use the formula to complete the table on the next page.

A	В	С	D	max point	min point	next max point	amplitude	period	frequency
1	1	0	0	(0, 1)	(3.14, -1)		½*(1 – (–1)) 2	$6.28 - 0$ 6.28 2π	
	1	0	0						
	1	0	0						
1		0	0						
1		0	0						
1	1		0						
1	1		0						
1	1	0							
1	1	0							
1	1	0							

- Based on the results in the table, determine and record each relationship:
 - o A and the amplitude
 - o B and the frequency
 - o B and the period